

deferred reversion as above is lessened by the value of the survivorship payable if a life  $n$  years older than  $A$  dies in the lifetime of  $B$ , multiplied into the value of £1 payable if  $A$  lives  $n$  years; hence the true value is equal to

$$\left( A_n \overset{\circ}{I} \overset{\circ}{I} - \frac{1}{I} \overline{A_n B} \overset{\circ}{I} \overset{\circ}{I} \right) \frac{a_n}{ar^n}.$$

PROBLEM II.—To determine the present value of a reversion of £1 payable on the death of  $A$ , provided he dies before another life,  $B$ , or *within*  $n$  years after him.

*Solution.*—The value of this contingent reversion is manifestly very nearly equal to the value of an absolute reversion on the single life of  $A$ , as the assurance will not be paid only in the event of his surviving  $B$  by at least  $n$  years, as in the foregoing problem. Consequently

$$A \overset{\circ}{I} \overset{\circ}{I} - \frac{a_n}{ar^n} \left( A_n \overset{\circ}{I} \overset{\circ}{I} - \frac{1}{I} \overline{A_n B} \overset{\circ}{I} \overset{\circ}{I} \right)$$

will be equal to the required value,

$$A \overset{\circ}{I} \overset{\circ}{I} - \frac{a_n}{ar^n} \left( A_n \overset{\circ}{I} \overset{\circ}{I} \right) + \frac{a_n}{ar^n} \left( \frac{1}{I} \overline{A_n B} \overset{\circ}{I} \overset{\circ}{I} \right);$$

and since

$$A \overset{\circ}{I} \overset{\circ}{I} - \frac{a_n}{ar^n} \left( A_n \overset{\circ}{I} \overset{\circ}{I} \right) = \frac{1}{I} \overset{\circ}{I} \overset{\circ}{I}$$

equals the value of a temporary reversion or assurance on the life of  $A$ , it is obvious that the value of the contingent reversion required by the problem will be

$$\frac{1}{I} \overline{A_n B} \overset{\circ}{I} \overset{\circ}{I} + \left( \frac{1}{I} \overline{A_n B} \overset{\circ}{I} \overset{\circ}{I} \right) \frac{a_n}{ar^n}.$$

Q. E. D.

The rule in words at length will consequently be—“To the value of a temporary assurance on the life of  $A$ , add the value of a reversion contingent on  $B$  surviving a life  $n$  years older than  $A$ , multiplied into the present value of £1 payable if  $A$  lives  $n$  years.”

ON A NEW EXPRESSION FOR THE VALUE OF THE ANNUAL PREMIUM FOR A LIFE ASSURANCE.

*To the Editors of the Assurance Magazine.*

GENTLEMEN,—In your last Number, p. 332, the very striking analogy was pointed out which subsists between a whole life assurance, and an assurance which is certainly payable at a specified age if it have not before become due. I may perhaps be pardoned for stating that this analogy had been previously shown by me, in proof of which I beg to refer you to “Tables and Formulæ for the Computation of Life Contingencies,” p. 95, Corollary.

I am satisfied that a good many curious if not useful relations amongst different benefits remain yet to be shown. *E. g.*:—To express the annual premium for a life assurance in terms of the single premium.

If  $a$  denote the present value of the annuity, and  $A$  that of the assurance, we have

$$A = v - (1 - v)a;$$

whence

$$a = \frac{v - A}{1 - v}, \text{ and } 1 + a = \frac{1 - A}{1 - v}.$$

Now the annual premium is equal to

$$\frac{1 - (1 - v)(1 + a)}{1 + a};$$

in which, substituting for  $1 + a$  its value as found above, we have for the annual premium

$$\frac{A(1 - v)}{1 - A},$$

a very compact expression.

I am, Gentlemen,

*Baker Street, Lloyd Square,*  
19 Sept., 1851.

Your most obedient servant,

P. GRAY.

[NOTE.—We owe our able correspondent an apology: on turning to his work we find the fact to be as he states it. The corollary in question had entirely escaped our observation.—*Ed. A. M.*]

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