

Emergent quantum materials

Chun Ning Lau, Fengnian Xia, and Linyou Cao, Guest Editors

The term quantum materials refers to materials whose properties are principally defined by quantum mechanical effects at macroscopic length scales and that exhibit phenomena and functionalities not expected from classical physics. Some key characteristics include reduced dimensionality, strong many-body interactions, nontrivial topology, and noncharge state variables of charge carriers. The field of quantum materials has been a topical area of modern materials science for decades, and is at the center stage of a wide range of modern technologies, ranging from electronics, photonics, energy, defense, to environmental and biomedical sensing. Over the past decade, much research effort has been devoted to the development of quantum materials with phenomena and functionalities that manifest at high temperature and feature unprecedented tunability with atomic-scale precision. This thriving research field has witnessed a number of seminal breakthroughs and is now poised to rise to the challenges in a new age of quantum information science and technology. This issue summarizes and reviews recent progress in selected topics, and also provides perspective for the future directions of emergent quantum materials in the years to come.

Introduction

Throughout human history, major advances in technology have been usually accompanied by a revolution in materials. Examples include the invention of bronze tools after the stone age, the displacement of bronze by iron, the development of the metallurgy of steel and aluminum that has been stimulated by and has fueled the industrial revolution, and the optimization and surface passivation of silicon that enabled much of the multibillion-dollar technological sector in the present day. Today, similarly disruptive advances in quantum materials may germinate from the burgeoning field of quantum information science (QIS), which utilizes quantum degrees of freedom for information storage and processing.¹ Technologies to manipulate and harness quantum states are poised to revolutionize current paradigms of computation, sensing, storage, and communications.

The term “quantum materials” is fairly broad, encompassing all materials whose properties are largely determined by quantum mechanical principles and phenomena. A key distinction of quantum materials from other materials lies in the manifestation of quantum mechanical effects at macroscopic length scales. In fact, all materials are composed of basic quantum particles and quasiparticles (i.e., electrons, holes, spins, and phonons) on the foundation of quantum mechanical principles at microscopic length scales; for example, the

wave-particle duality of basic quantum particles or quasiparticles, and uncertainty in energy/momentum of basic particles or quasiparticles. However, the quantum mechanical effects manifested at the molecular and atomic scale of classical materials are overwhelmed by the classical statistical mechanics of a large particle ensemble in macroscopic length scales. Generally, quantum materials are characterized by at least one, and often several, of the following attributes.

The first attribute is the quantum confinement of basic quantum particles and quasiparticles (i.e., electrons, holes, excitons, spins, and phonons) due to the reduced dimensionality of materials. Quantum confinement occurs when the physical dimension of the materials is comparable to or smaller than the characteristic length scale of quantum particles. The definition of characteristic length scale varies with quantum particles, for instance, as the physical extension of excitonic wave function (excitonic Bohr radius) for excitons and as mean scattering-free paths for electrons, holes, spins, and phonons. Quantum confinement leads to properties that are either dramatically modified from the bulk or entirely new properties not found in the parent materials, such as the size-dependent energy-level spacing of charges in semiconductor nanocrystals that form the basis of quantum dot displays,² and the controlled entangled spin states in semiconductor quantum dots that are now a promising platform for quantum computation.³

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Another common attribute of quantum materials is strong many-body interactions, such as electron–electron, electron–phonon, exciton–exciton, and spin–valley interactions. For instance, the strong Coulomb interactions among charges, which, together with competing degrees of freedom such as spin and valley (local minima in the electronic band structure), gives rise to collective phenomena that are not expected from the noninteracting single-particle picture. These emergent phenomena include some of the most spectacular manifestations of collective behaviors of charges and atoms, including superconductivity, magnetism, and charge-density waves. They also underlie some of the most studied but long-standing mysteries in materials research, such as high-temperature superconductivity and heavy fermion systems.

A third characteristic shared by many quantum materials is the important role played by topology and the Berry phase (the Berry phase is a geometric phase of the wave function acquired by a charge when it adiabatically completes a closed path in certain parameter spaces). These topological quantum materials have topologically nontrivial electronic structures, giving rise to exotic properties that are topologically protected. Examples include the quantum spin Hall effect (QSH) in two-dimensional (2D) topological insulators (TIs), in which helical edge states (a pair of counter-propagating spin-polarized edge states) circulate along the edges of otherwise insulating bulk; and the quantum anomalous Hall effect (QAHE) in insulators that, in the presence of magnetization and large spin–orbit coupling, host quantized Hall conductance in a zero magnetic field.

Last, quantum materials enable the utilization of noncharge degrees of freedom of charge carriers, such as spin, valley, and pseudospin. Creation, transport, and manipulation of these nontraditional state variables has been a flourishing area of research, with technological applications beyond Moore’s Law scaling of integrated circuits, high-density storage (exemplified by the spectacular success of magnetic random-access memory [MRAM]), low-energy electronics, and quantum computation.

Here, we briefly discuss some of the most promising quantum material systems that have recently emerged as topical research areas. In most of these systems, more than one of these previously discussed attributes, are present, intertwining to give rise to novel phenomena and enabling devices to usher in new scientific and technological paradigms of computation, sensing, and communications (**Figure 1**).

Two-dimensional materials

Two-dimensional materials⁴ have constituted one of the most active frontiers of materials research in the past decade, opening the door for exploring the mechanical, optical, thermal, and electronic properties of atoms that are confined to atomically thin layers and with promise as the future generation of electronic and optoelectronic materials and applications. Starting with the isolation of graphene on insulating substrates,⁵ the family of 2D materials has since been broadened to include insulators, semiconductors, superconductors, ferromagnets, and charge-density wave materials.

The allure of 2D materials partly lies in their extremely reduced dimensionality—as a material’s thickness is reduced to a single or few atomic layers (**Figure 2a**), its properties are dramatically altered from those of the bulk. As a result of the reduced dimensionality, 2D materials often feature strong quantum confinement and reduced Coulomb screening. The quantum confinement gives rise to discrete energy levels, and the reduced Coulomb screening can significantly enhance the effects of charge interactions. From an intuitive perspective, the enhanced charge interaction results from the fact that the charges simply do not have as much available “space” to avoid one another (in fact, they “have lost” an entire dimension). The strong quantum confinement and reduced Coulomb screening collectively enable the exceedingly strong exciton binding energy in 2D materials, in particular, 2D semiconductors, which is often more than one order of magnitude stronger than that of conventional semiconductors. Such strong binding energy makes excitons, a quasiparticle consisting of electrostatically bound electrons and holes, robust enough to become a viable carrier for quantum information processing. This will be discussed further in the section on strongly correlated quantum materials.

Combining these effects with additional degrees of freedom, such as spin, valley, and layer, results in many specular phenomena in quantum materials, including emergent quantum phases such as magnetism, superconductivity, or correlated insulators that are not found in their bulk counterparts. In many cases, two or more of these quantum phases manifest in the same material and are tunable *in situ* by charge injection via electrical gating or other ways. Two-dimensional quantum materials are also extremely attractive from the standpoint of providing unprecedented quality

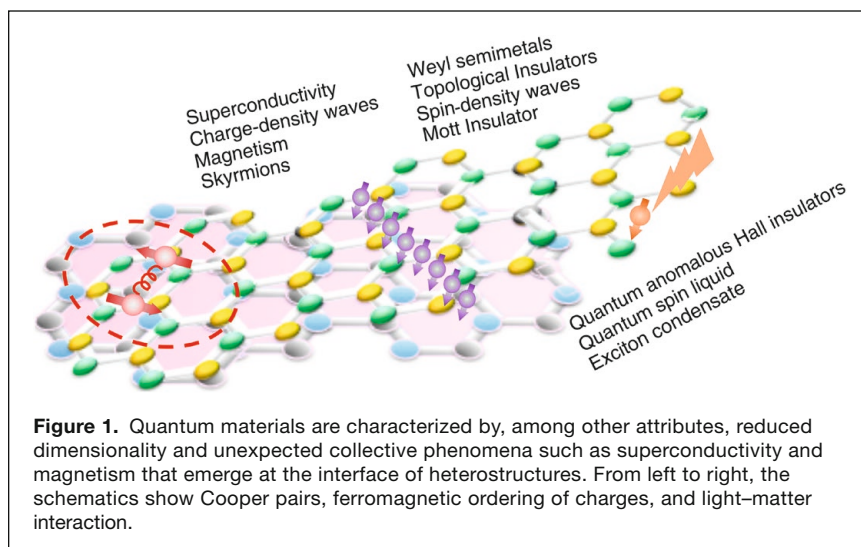
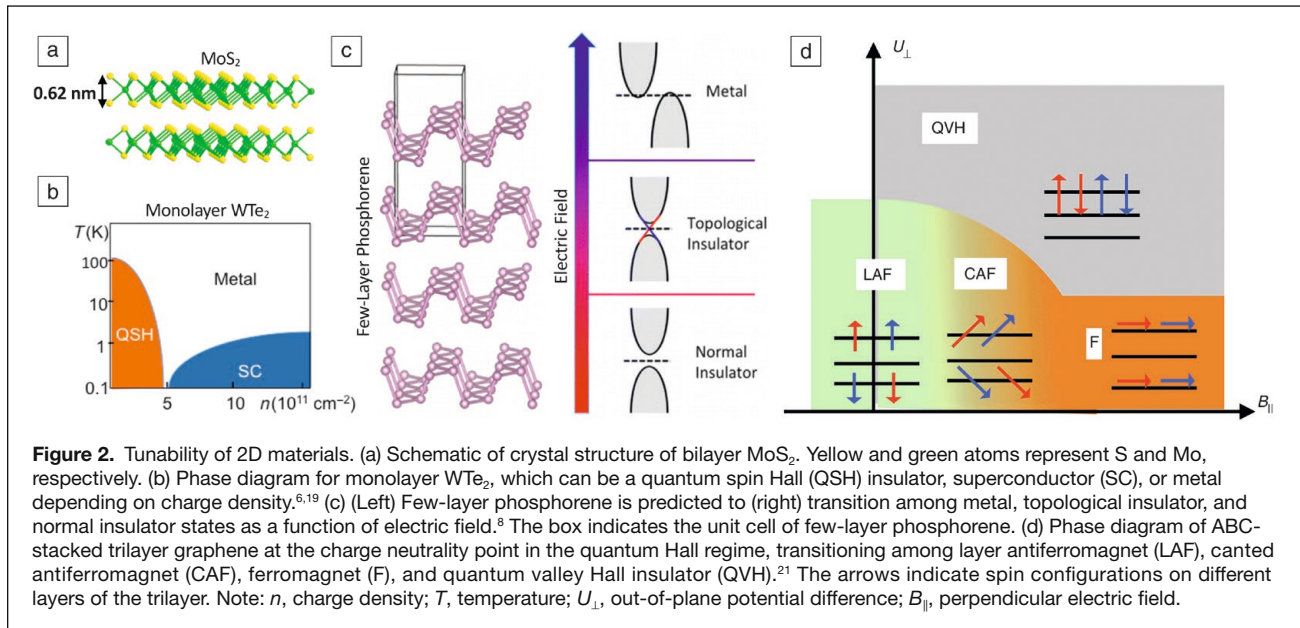


Figure 1. Quantum materials are characterized by, among other attributes, reduced dimensionality and unexpected collective phenomena such as superconductivity and magnetism that emerge at the interface of heterostructures. From left to right, the schematics show Cooper pairs, ferromagnetic ordering of charges, and light–matter interaction.



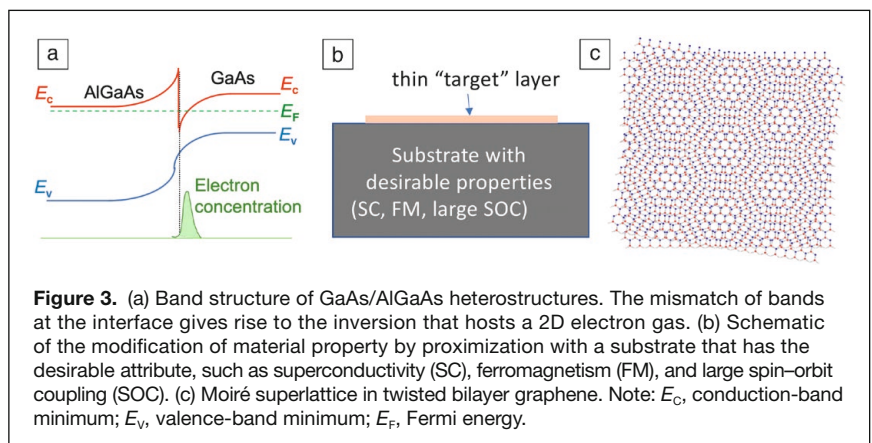
and tunability. First, many 2D materials have an exceedingly high charge mobility, which exceeds several million cm²/Vs in graphene,⁶ and reaches up to 25,000 cm²/Vs in few-layer black phosphorus.⁷ Such high mobilities are particularly pertinent for applications that require long lifetimes for charge or spin. For instance, spin lifetimes as long as 12 ns have been demonstrated.^{8,9} Second, 2D materials are extremely tunable, as many of the properties can be controlled via electrostatic gates that can tune charge density and the out-of-plane electric field, as well as via in-plane and out-of-plane magnetic fields. For instance, while bulk WTe₂ is a semimetal, monolayer WTe₂ is a QSH insulator at low doping and becomes a superconductor when the charge density exceeds 5×10^{12} cm⁻² (Figure 2b).^{10–16} In highly doped atomically thin MoS₂, Ising superconductivity is observed, in which the spin-valley locking leads to an in-plane critical field that greatly exceeds the paramagnetic limit.¹⁷ Few-layer black phosphorus has been predicted and shown to undergo transitions among normal insulator, topological insulator, and semimetal as a function of out-of-plane electric field (Figure 2c).^{18,19} In bilayer and ABC-stacked trilayer graphene, transitions among layered antiferromagnet, layer polarized valley–Hall insulator, and conventional metal by changing charge density n and out-of-plane potential bias U_{\perp} (Figure 2d).^{20–22} Bilayer CrI₃ can be ferromagnetic, antiferromagnetic, or paramagnetic depending on doping level and magnetic field.^{23–25}

Third, the electronic states in 2D materials are surface states, and thus are more easily manipulated and coupled to mechanical, optical, or scanned probes. They are nature’s thinnest elastic membranes,^{26,27} and can ripple,²⁸ wrinkle,^{29,30} and sustain elastic strains up to 25%.³¹

They are excellent optoelectronic materials and provide ultrafast and broadband photoresponse.^{32–38} Finally, they enable creation of twist, Moiré, or stacked heterostructures with tailored electronic properties that are otherwise inaccessible (see also the next section on ‘Heterostructures and interfaces’).

Heterostructures and interfaces

In a heterostructure, two dissimilar materials are adjoined together to form a new material system. At the interface of the two dissimilar materials, the mismatch in work functions, Fermi velocities, electronic bands, magnetic ordering, and lattice constants results in a plethora of new phenomena. One of the oldest and most intensely studied phenomena is the discontinuity in conduction and valence bands of semiconductors with different doping or bandgap sizes, which leads to the formation of a quantum well, 2D electron gas (2DEG) or 2D hole gas at the interface of semiconductor heterostructures (Figure 3a). Remarkably, a 2DEG may even emerge at the interface of insulators, such as in the case of LaAlO₃/SrTiO₃.^{39–43}



where both of the parent materials are insulators (with bandgaps of 5 eV and 3.5V, respectively). Under the right conditions, a number of surprising phenomena have been observed at this interface, including high mobility transport, quantum oscillations, superconductivity, ferromagnetism, and giant photoconductivity.

Apart from the misalignment of band structures, other important factors at the interface are interfacial charge transfer (e.g., mismatch in work functions) and lattice mismatch. For instance, bulk FeSe is a superconductor with intrinsic transition temperature $T_c \sim 9$ K; amazingly, for a FeSe monolayer on SrTiO₃ substrate, its T_c skyrocketed by as much as an order of magnitude, to ~ 100 K.^{44,45} The exact mechanism of such a dramatic enhancement in T_c is still under debate, but it is clearly an interfacial effect, likely related to charge transfer from SrTiO₃ and interfacial phonon coupling; understanding this system could provide guiding principles for rational design of high- T_c superconductors.

Additionally, the 1.8% lattice mismatch between graphene and hexagonal BN (hBN) leads to a Moiré superlattice with a unit cell that is as large as 200 nm;² therein the disproportion between flux quantum and the large unit cell of the Moiré superlattice^{46–49} leads to the celebrated Hofstadter butterfly fractal spectrum.⁵⁰

An important effect in heterostructures is the proximity effect, that is, the “endowment” of new properties onto a thin overlayer material by the proximity of a second material (Figure 3b). For example, spin–orbit coupling (SOC) is small in pristine graphene, but can be made much larger by proximitized graphene with transition-metal dichalcogenide layers,^{51–63} thus allowing the creation of devices with controlled, spatially varying SOC. The anomalous Hall effect, typically present only in ferromagnetic materials, is observed in graphene on ferromagnetic insulators.⁶⁴ Another example is the opening of an energy gap in the otherwise gapless electronic structure of pristine graphene, by aligning it with hBN and breaking the inversion symmetry of the lattice.⁴⁷ In a technologically relevant case, proximitizing a topological insulator with a superconductor gives rise to the formation of Majorana zero modes at the interface. Majorana fermions in solid state systems are quasiparticle excitations with half-integer spins that are their own antiparticles; because they obey non-Abelian statistics, they are seen as one of the most promising routes to realize topological quantum computing. Such Majorana zero modes have been realized in heterostructures consisting of superconductor-coupled QSH or nanowire systems that have large SOC.^{65–67}

The immense potential for heterostructure creation is further highlighted by the rise of “twistronics,”^{68–71} which uses the relative twist angle between two atomic layers to tailor the electronic, thermal, and optoelectronic properties (Figure 3c). This is exemplified by the breakthrough in twisted bilayer graphene, which hosts electronic phases, including superconductivity, the QAHE, and correlated insulating state at different charge densities.^{70–74} Strictly speaking, twisted bilayer

graphene is not a heterostructure; however, twistronics can be extended to twisted bilayers of different materials. For example, exotic quantum phases are expected in twisted heterobilayers, such as WSe₂/MoSe₂; many of these phases have nontrivial topological characteristics, such as QSH, QAH, and topological superconductors.^{75–77} Thus, by judicious choice of materials and device architecture, there are almost limitless possibilities for exploration of new phenomena and rational design of quantum devices.

Topological quantum materials

Topology is a mathematical concept that refers to the properties of an object that are unaffected by continuous deformation of shape, such as twisting, bending, or stretching. For example, an orange is topologically equivalent to a banana, but both are distinct from a bagel. In the 1970s, this mathematical concept was adopted by physicists to understand, for example, the quantum Hall (QH) effect in 2D systems and phase transitions in superfluids. In 2016, the Nobel Prize in Physics was awarded to Kosterlitz, Thouless, and Haldane for their “theoretical discoveries of topological phase transitions and topological phases of matter.”

The earliest and most studied topological phenomenon is the QH effect.⁷⁸ In a high magnetic field, electron orbitals confined to two dimensions coalesce to form Landau levels that are energetically separated by cyclotron gaps. When the chemical potential is located between Landau levels, the bulk is insulating; at the sample’s edge, however, dissipationless one-dimensional (1D) edge states form, giving rise to zero longitudinal resistance and Hall conductance that is quantized in integer multiples of e^2/h , where e is the electron charge and h is Planck’s constant (Figure 4a). It can be shown that the QH states can be mapped into a topologically nontrivial Hilbert space, with a topological invariant number, called the Chern number, which is determined by the integral of the Berry phase over the Brillouin zone. In QH systems, the time-reversal symmetry (TRS) is broken by an external magnetic field.

It is, however, possible to generate QH-like edge states without breaking the TRS.^{79–88} This groundbreaking idea was first proposed by Kane and Mele,⁷⁹ and also independently by Bernevig and Zhang,^{82,89} and experimentally realized in topological insulators found in CdTe/HgTe/CdTe quantum wells.^{90,91} Due to the large SOC in HgTe, the bulk electronic band has an inverted gap, that is, the hole-like valence band is energetically located above the electron-like conduction band. CdTe, however, has a normal gap. At the interface, the inverted bands in HgTe must connect smoothly to the normal bands of CdTe, thus leading to crossing of these bands at the surface (Figure 4b), in this case, the edge. The edge states are gapless and enable metallic transport; since their presence is protected by the topology of the system, their conduction is immune from scattering due to disorder or defects, similar to those at the edges of QH systems. These states are called quantum spin Hall insulator states in a 2D topological insulator (TI).

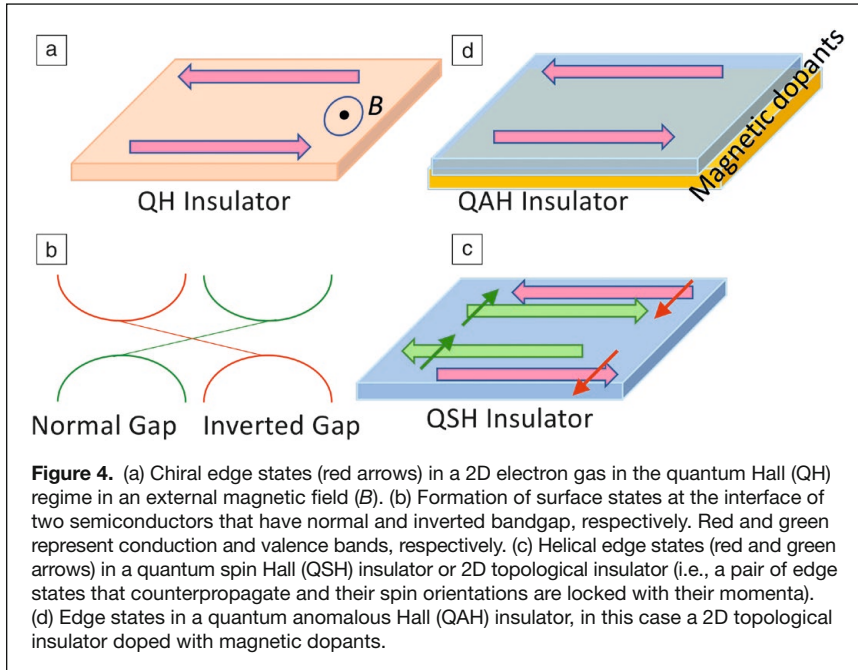


Figure 4. (a) Chiral edge states (red arrows) in a 2D electron gas in the quantum Hall (QH) regime in an external magnetic field (B). (b) Formation of surface states at the interface of two semiconductors that have normal and inverted bandgap, respectively. Red and green represent conduction and valence bands, respectively. (c) Helical edge states (red and green arrows) in a quantum spin Hall (QSH) insulator or 2D topological insulator (i.e., a pair of edge states that counterpropagate and their spin orientations are locked with their momenta). (d) Edge states in a quantum anomalous Hall (QAH) insulator, in this case a 2D topological insulator doped with magnetic dopants.

There are, however, important differences between the edge states in a TI and in a QH system. QH edge states are chiral (i.e., propagating clockwise or counterclockwise in the sample). In contrast, due to the preserved TRS, the QSH edge states in a TI come in pairs that are time-reversed partners (i.e., an edge state with spin up propagates clockwise and another with spin down propagates counterclockwise [Figure 4c]). These states are known as helical edge states or have spin–momentum locking. One of the most important applications of QSH states is topological quantum computation—coupling the helical edge states to s -wave superconductors creates Majorana zero modes at the interface, which are the building block of fault-tolerant quantum computers.

In another major breakthrough in the area, researchers realized that, instead of an external magnetic field, TRS can also be explicitly broken by proximitizing with a magnetic layer or doping a TI film with magnetic elements^{92–95} (Figure 4d). For instance, in Cr-doped $(\text{Bi,Sb})_2\text{Te}_3$ thin films, quantized Hall conductance of e^2/h is observed at an external magnetic field $B = 0$.^{95–97} In this the so-called quantum anomalous Hall (QAH) insulator, the edge states are chiral, similar to that of a QH state (Figure 4d). A significant technical challenge is the low operating temperature ($T \sim 30$ mK in initial experiments, ~ 1 K in subsequent works with further material optimization⁹⁸). More recently, a robust QAHE has been observed in intrinsic materials, including in the antiferromagnetic layered TI MnBi_2Te_4 ,⁹⁹ in twisted bilayer graphene⁷³ and in aligned hBN/trilayer graphene Moiré superlattice.¹⁰⁰ QAH insulators are highly promising platforms for dissipationless spintronics with tunable domain walls or domain boundaries that can be manipulated by an electric field.

Today, the study of topological materials, including, but not limited to, topological insulators, topological crystalline

insulators, Weyl semimetals, and topological superconductors, is a thriving and ever-expanding field, while the concept of topologically protected transport has been extended to the fields of photonics, phononics, mechanics, and magnonics. Topological materials are now ubiquitous, with many more novel phenomena and applications that await exploration.

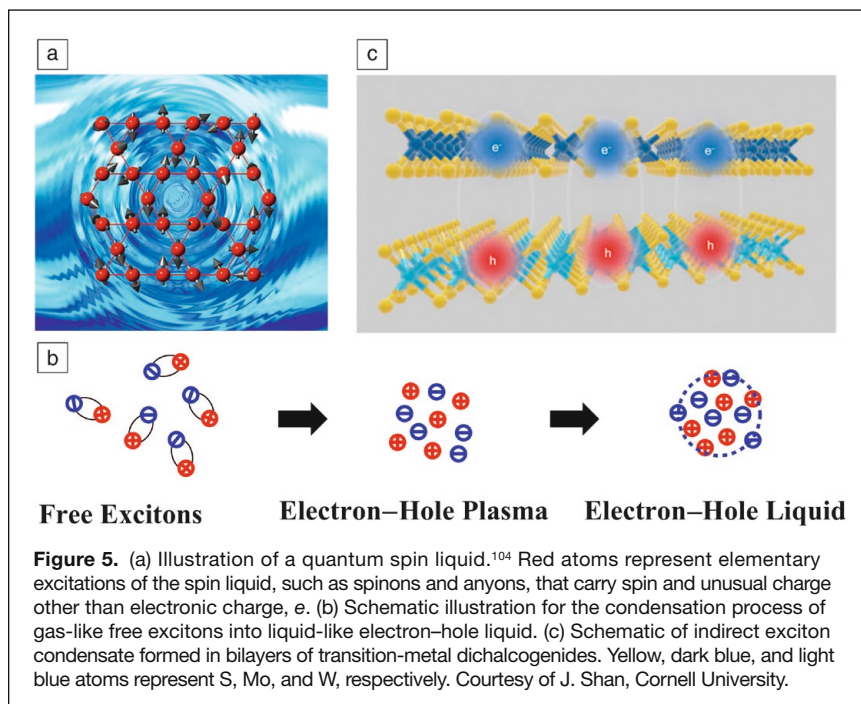
Strongly interacting quantum materials

Strong many-body interactions are at the heart of the most spectacular of correlated phases that depend on the collective behaviors of charges and atoms. Here, we will briefly touch upon two systems not discussed in the previous sections: quantum spin liquid and exciton condensates.

A quantum spin liquid is an exotic phase of quantum magnetism.^{101–103} For ferromagnets and antiferromagnets, the semiclassical picture is the establishment of long-range order of aligned or anti-aligned neighboring spins

below the transition temperature (Curie or Néel temperature). In a quantum spin liquid, however, the strong interactions among spins prevents long range spin coherence even at the lowest temperature (Figure 5a).¹⁰⁴ They exhibit massive quantum superposition and an unusually high degree of entanglement. This many-body quantum entanglement can support a variety of nonlocal excitations that depend on the collective behaviors of a large number of spins and charges. One of the most famous examples is so-called spinons, which are spin-1/2 quasiparticles with charge 0. Another example is the anyon, found in fractional QH states in 2DEGs, an excitation that behaves as if it carries a charge of a fraction of e ; anyons obey non-Abelian statistics (i.e., they pick up a nontrivial Berry phase when circling each other). Prospective applications of this rather exotic state of matter include topological quantum computation and unconventional high-temperature superconductivity. There has been much excitement and progress in this area, though many questions, both experimental and theoretical, await answers.

Excitons are bound pairs of electrons and holes. As a composite particle of two fermions, an exciton is a boson and obeys Bose–Einstein statistics. Excitons, therefore, have the ability to form a condensate (i.e., with macroscopic occupation of the lowest energy state). Direct excitons consist of an electron in the conduction band and a hole from the valence band from the same 2D layer. For indirect excitons, in contrast, the constituent electrons and holes originate from different layers, and their lifetime is generally much longer due to the physical separation of the electrons and holes. When the density is low, excitons behave like free gas molecules with weak interaction among neighboring excitons. A boson condensate that formed in this low-density regime is called a Bose–Einstein condensate (BEC). In the high-density regime,



the excitons are similar to Cooper pairs in superconductors—the electrons and holes may be physically separated over considerable distance, and the wave function of the macroscopic ground state consists of many spatially overlapping electron–hole pairs. A condensate of these excitons is the so-called Bardeen–Cooper–Schrieffer (BCS) type, named after the BCS theory for conventional superconductors. Experimentally, exciton condensation of both BEC and BCS types has been realized in coupled quantum wells based on GaAs.^{105,106}

Both BEC and BCS exciton condensations occur in energy/momentum space. There is another type of exciton condensation in real space that is similar to the condensation of a classical gas into a liquid (i.e., condensation of gas-like excitons into electron–hole plasma or a liquid-like state, electron–hole liquid) (Figure 5b).

More recently, 2D materials and heterostructures provide new opportunities for the studies of exciton condensation, due to their super strong exciton binding energy that often exceeds that of traditional semiconductors by an order of magnitude. Such strong binding energy makes possible excitonic quantum information processing. Recent studies have demonstrated the room-temperature phase transition of excitons, including exciton Mott transition and electron–hole liquid (Figure 5b), hole liquid,¹⁰⁷ exciton Bose–Einstein condensation in graphene, and 2D semiconductors^{43,108} with transition temperature as high as 100 K (Figure 5c).¹⁰⁹ These new excitonic phases or states feature macroscopic quantum coherency and bear great promise for applications in QIS.

In this issue

In this issue of *MRS Bulletin*, we have selected a few topics from the broadly defined field of quantum materials and present

some of the most important developments at the intersection of materials science and condensed-matter physics.

In their article¹¹⁰ in this issue, Li and Chen focus on the unique role of thermal-transport properties in quantum materials. They review the insights thermal transport can provide for the exploration of emergent quantum phenomena, particularly those with charge neutral excitations that are difficult to probe by electrical transport. Thermal-transport probes of quantum spin liquid, pairing symmetry of an unconventional superconductor, and Berry curvature in Weyl semimetals are discussed.

Butov’s article¹¹¹ reviews the Bose–Einstein condensation of indirect excitons and quantum phenomena observed in the condensate, including interference dislocation, periodic spatial modulation greater than lengths up to 1 mm, long-range spin textures, and Berry phase and long-range coherent spin transport.

In their article, Torres et al.¹¹² emphasize spintronics and magnetism in 2D materials and heterostructures, including 2D magnets, spin-charge conversion, spin–orbit torque, and long-distance spin transport.

The article by Song et al.¹¹³ discusses high- T_c superconductivity at the interface. Compared with bulk superconductors, the interface at material heterojunctions provides an ideal platform for the investigation of many-body physics and the search for high- T_c superconducting phenomena.

Finally, the article by Wang et al.¹¹⁴ covers a wide range of topological materials, including topological insulators, QAH insulators, Weyl semimetals, and Chern magnetic insulators. They also discuss future opportunities in the discovery of new quantum phenomena and potential applications.

Conclusion

The field of quantum materials is vast and recently fast moving, with discoveries of new materials and phenomena announced weekly. It is impossible to do justice to this field in a single issue. Here, we have touched upon just a few topics and material systems, while emphasizing that the scope for materials discovery and tailored device design is almost limitless. Undoubtedly, many challenges lie ahead, such as scalable and cost-effective manufacturing, uniformity, and interface control of heterostructures, raising operating temperatures (particularly for quantum computation building blocks), and integration with conventional Si-based devices. It is the belief and hope of the authors that, after being on the center stage for the advent of the digital age, quantum materials are now again poised to usher in a new age of quantum information science and technology.

Acknowledgments

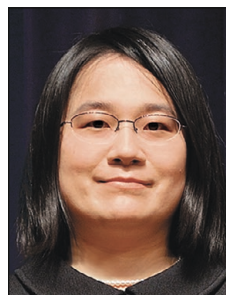
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References

1. *Quantum Materials for Energy Relevant Technology* (Report of the office of Basic Energy Sciences workshop on quantum materials, Office of Science, US Department of Energy, 2016), https://science.osti.gov/-/media/bes/pdf/reports/2016/BRNQM_rpt_Final_12-09-2016.pdf.
2. D. Bera, L. Qian, T.-K. Tseng, P.H. Holloway, *Materials* **3**, 2260 (2010).
3. D. Loss, D.P. DiVincenzo, *Phys. Rev. A* **57**, 120 (1998).
4. S.Z. Butler, S.M. Hollen, L. Cao, Y. Cui, J.A. Gupta, H.R. Gutierrez, T.F. Heinz, S.S. Hong, J. Huang, A.F. Ismach, E. Johnston-Halperin, M. Kuno, V.V. Plashnitsa, R.D. Robinson, R.S. Ruoff, S. Salahuddin, J. Shan, L. Shi, M.G. Spencer, M. Terrones, W. Windl, J.E. Goldberger, *ACS Nano* **7**, 2898 (2013).
5. K.S. Novoselov, A.K. Geim, S.V. Morozov, D. Jiang, Y. Zhang, S.V. Dubonos, I.V. Grigorieva, A.A. Firsov, *Science* **306**, 666 (2004).
6. A.S. Mayorov, D.C. Elias, I.S. Mukhin, S.V. Morozov, L.A. Ponomarenko, K.S. Novoselov, A.K. Geim, R.V. Gorbachev, *Nano Lett.* **12**, 4629 (2012).
7. J. Yang, S. Tran, J. Wu, S. Che, T. Taniguchi, K. Watanabe, H. Baek, D. Smirnov, R. Chen, C.N. Lau, *Nano Lett.* **18**, 229 (2018).
8. M. Drögeler, C. Franzen, F. Volmer, T. Pohlmann, L. Banszerus, M. Wolter, K. Watanabe, T. Taniguchi, C. Stampfer, B. Beschoten, *Nano Lett.* **16**, 3533 (2016).
9. J. Xu, T. Zhu, Y.K. Luo, Y.-M. Lu, R.K. Kawakami, *Phys. Rev. Lett.* **121**, 127703 (2018).
10. X. Qian, J. Liu, L. Fu, J. Li, *Science* **346**, 1344 (2014).
11. F. Zheng, C. Cai, S. Ge, X. Zhang, X. Liu, H. Lu, Y. Zhang, J. Qiu, T. Taniguchi, K. Watanabe, S. Jia, J. Qi, J.-H. Chen, D. Sun, J. Feng, *Adv. Mater.* **28**, 4845 (2016).
12. Z. Fei, T. Palomaki, S. Wu, W. Zhao, X. Cai, B. Sun, P. Nguyen, J. Finney, X. Xu, D.H. Cobden, *Nat. Phys.* **13**, 677 (2017).
13. S. Tang, C. Zhang, D. Wong, Z. Pedramrazi, H.-Z. Tsai, C. Jia, B. Moritz, M. Claassen, H. Ryu, S. Kahn, J. Jiang, H. Yan, M. Hashimoto, D. Lu, R.G. Moore, C.-C. Hwang, C. Hwang, Z. Hussain, Y. Chen, M.M. Ugeda, Z. Liu, X. Xie, T.P. Devereaux, M.F. Crommie, S.-K. Mo, Z.-X. Shen, *Nat. Phys.* **13**, 683 (2017).
14. S. Wu, V. Fatemi, Q.D. Gibson, K. Watanabe, T. Taniguchi, R.J. Cava, P. Jarillo-Herrero, *Science* **359**, 76 (2018).
15. V. Fatemi, S. Wu, Y. Cao, L. Bretheau, Q.D. Gibson, K. Watanabe, T. Taniguchi, R.J. Cava, P. Jarillo-Herrero, *Science* **362**, 926 (2018).
16. E. Sajadi, T. Palomaki, Z. Fei, W. Zhao, P. Bement, C. Olsen, S. Luescher, X. Xu, J.A. Folk, D.H. Cobden, *Science* **362**, 922 (2018).
17. J.M. Lu, O. Zheliuk, I. Leermakers, N.F.Q. Yuan, U. Zeitler, K.T. Law, J.T. Ye, *Science* **350**, 1353 (2015).
18. Q. Liu, X. Zhang, L.B. Abdalla, A. Fazio, A. Zunger, *Nano Lett.* **15**, 1222 (2015).
19. J. Kim, S.S. Baik, S.H. Ryu, Y. Sohn, S. Park, B.-G. Park, J. Denlinger, Y. Yi, H.J. Choi, K.S. Kim, *Science* **349**, 723 (2015).
20. J. Velasco, L. Jing, W. Bao, Y. Lee, P. Kratz, V. Aji, M. Bockrath, C.N. Lau, C. Varma, R. Stillwell, D. Smirnov, F. Zhang, J. Jung, A.H. MacDonald, *Nat. Nanotechnol.* **7**, 156 (2012).
21. Y. Lee, D. Tran, K. Myhro, J. Velasco Jr., N. Gillgren, C.N. Lau, Y. Barlas, J.M. Pouchiro, D. Smirnov, F. Guinea, *Nat. Commun.* **5**, 5656 (2014).
22. P. Maher, C.R. Dean, A.F. Young, T. Taniguchi, K. Watanabe, K.L. Shepard, J. Hone, P. Kim, *Nat. Phys.* **9**, 154 (2013).
23. B. Huang, G. Clark, D.R. Klein, D. MacNeill, E. Navarro-Moratalla, K.L. Seyler, N. Wilson, M.A. McGuire, D.H. Cobden, D. Xiao, W. Yao, P. Jarillo-Herrero, X. Xu, "Electrical Control of 2D Magnetism in Bilayer CrI₃," preprint, submitted arXiv:1802.06979 (2018).
24. S. Jiang, L. Li, Z. Wang, K.F. Mak, J. Shan, "Controlling Magnetism in 2D CrI₃ by Electrostatic Doping," preprint, submitted arXiv:1802.07355 (2018).
25. S. Jiang, J. Shan, K.F. Mak, *Nat. Mater.* **17**, 406 (2018).
26. V.M. Pereira, A.H. Castro Neto, *Phys. Rev. Lett.* **103**, 046801 (2008).
27. H. Vandeparre, M. Pineaiva, F. Brau, B. Roman, J. Bico, C. Gay, W. Bao, C.N. Lau, P.M. Reis, P. Damman, *Phys. Rev. Lett.* **106**, 224301 (2011).
28. W.Z. Bao, F. Miao, Z. Chen, H. Zhang, W.Y. Jang, C. Dames, C.N. Lau, *Nat. Nanotechnol.* **4**, 562 (2009).
29. W. Bao, K. Myhro, Z. Zhao, Z. Chen, W. Jang, L. Jing, F. Miao, H. Zhang, C. Dames, C.N. Lau, *Nano Lett.* **12**, 5470 (2012).
30. H. Zhang, J.-W. Huang, J. Velasco Jr., K. Myhro, M. Maldonado, D. Tran, Z. Zhao, F. Wang, Y. Lee, G. Liu, W. Bao, C.N. Lau, *Carbon* **69**, 336 (2014).
31. C. Lee, X.D. Wei, J.W. Kysar, J. Hone, *Science* **321**, 385 (2008).
32. F. Xia, T. Mueller, Y.-M. Lin, A. Valdes-Garcia, P. Avouris, *Nat. Nanotechnol.* **4**, 839 (2009).
33. X. Wang, P. Wang, J. Wang, W. Hu, X. Zhou, N. Guo, H. Huang, S. Sun, H. Shen, T. Lin, M. Tang, L. Liao, A. Jiang, J. Sun, X. Meng, X. Chen, W. Lu, J. Chu, *Adv. Mater.* **27**, 6575 (2015).
34. D. Kufer, G. Konstantatos, *Nano Lett.* **15**, 7307 (2015).
35. N. Youngblood, C. Chen, S.J. Koester, M. Li, *Nat. Photonics* **9**, 247 (2015).
36. H. Yuan, X. Liu, F. Afshinmanesh, W. Li, G. Xu, J. Sun, B. Lian, A.G. Curto, G. Ye, Y. Hikita, Z. Shen, S.-C. Zhang, X. Chen, M. Brongersma, H.Y. Hwang, Y. Cui, *Nat. Nanotechnol.* **10**, 707 (2015).
37. M. Engel, M. Steiner, P. Avouris, *Nano Lett.* **14**, 6414 (2014).
38. C.-H. Liu, Y.-C. Chang, T.B. Norris, Z. Zhong, *Nat. Nanotechnol.* **9**, 273 (2014).
39. A. Ohtomo, H.Y. Hwang, *Nature* **427**, 423 (2004).
40. S. Gariglio, N. Reyren, A.D. Caviglia, J.M. Triscone, *J. Phys. Condens. Matter* **21**, 164213 (2009).
41. M. Ben Shalom, M. Sachs, D. Rakhmilevitch, A. Palevski, Y. Dagan, *Phys. Rev. Lett.* **104**, 126802 (2010).
42. Ariando, X. Wang, G. Baskaran, Z.Q. Liu, J. Huijben, J.B. Yi, A. Annadi, A.R. Barman, A. Rusydi, S. Dhar, Y.P. Feng, J. Ding, H. Hilgenkamp, T. Venkatesan, *Nat. Commun.* **2**, 188 (2011).
43. G.W. Burg, N. Prasad, K. Kim, T. Taniguchi, K. Watanabe, A.H. MacDonald, L.F. Register, E. Tutuc, *Phys. Rev. Lett.* **120**, 177702 (2018).
44. S. He, J. He, W. Zhang, L. Zhao, D. Liu, X. Liu, D. Mou, Y.-B. Ou, Q.-Y. Wang, Z. Li, L. Wang, Y. Peng, Y. Liu, C. Chen, L. Yu, G. Liu, X. Dong, J. Zhang, C. Chen, Z. Xu, X. Chen, X. Ma, Q. Xue, X.J. Zhou, *Nat. Mater.* **12**, 605 (2013).
45. D. Huang, J.E. Hoffman, *Annu. Rev. Condens. Matter Phys.* **8**, 311 (2017).
46. L.A. Ponomarenko, R.V. Gorbachev, G.L. Yu, D.C. Elias, R. Jalil, A.A. Patel, A. Mishchenko, A.S. Mayorov, C.R. Woods, J.R. Wallbank, M. Mucha-Kruczynski, B.A. Piot, M. Potemski, I.V. Grigorieva, K.S. Novoselov, F. Guinea, V.I. Fal'ko, A.K. Geim, *Nature* **497**, 594 (2013).
47. B. Hunt, J.D. Sanchez-Yamagishi, A.F. Young, M. Yankowitz, B.J. LeRoy, K. Watanabe, T. Taniguchi, P. Moon, M. Koshino, P. Jarillo-Herrero, R.C. Ashoori, *Science* **340**, 1427 (2013).
48. C.R. Dean, L. Wang, P. Maher, C. Forsythe, F. Ghahari, Y. Gao, J. Katoch, M. Ishigami, P. Moon, M. Koshino, T. Taniguchi, K. Watanabe, K.L. Shepard, J. Hone, P. Kim, *Nature* **497**, 598 (2013).
49. P. Wang, B. Cheng, O. Martynov, T. Miao, L. Jing, T. Taniguchi, K. Watanabe, V. Aji, C.N. Lau, M. Bockrath, *Nano Lett.* **15**, 6395 (2015).
50. D.R. Hofstadter, *Phys. Rev. B* **14**, 2239 (1976).
51. A. Avsar, J.Y. Tan, T. Taychatanapat, J. Balakrishnan, G.K.W. Koon, Y. Yeo, J. Lahiri, A. Carvalho, A.S. Rodin, E.C.T. O'Farrell, G. Eda, A.H. Castro Neto, B. Özyilmaz, *Nat. Commun.* **5**, 4875 (2014).
52. M. Gmitra, J. Fabian, *Phys. Rev. B* **92**, 155403 (2015).
53. M. Gmitra, J. Fabian, *Phys. Rev. Lett.* **119**, 146401 (2017).
54. J.Y. Khoo, A.F. Morpurgo, L. Levitov, *Nano Lett.* **17**, 7003 (2017).
55. L.A. Benítez, J.F. Sierra, W. Saverio Torres, A. Arrighi, F. Bonell, M.V. Costache, S.O. Valenzuela, *Nat. Phys.* **14**, 303 (2018).
56. Z. Wang, D.-K. Ki, H. Chen, H. Berger, A.H. MacDonald, A.F. Morpurgo, *Nat. Commun.* **6**, 8339 (2015).
57. Z. Wang, D.-K. Ki, J.Y. Khoo, D. Mauro, H. Berger, L.S. Levitov, A.F. Morpurgo, *Phys. Rev. X* **6**, 041020 (2016).
58. B. Yang, M.-F. Tu, J. Kim, Y. Wu, H. Wang, J. Alicea, R. Wu, M. Bockrath, J. Shi, *2D Mater.* **3**, 031012 (2016).
59. B. Yang, M. Lohmann, D. Barroso, I. Liao, Z. Lin, Y. Liu, L. Bartels, K. Watanabe, T. Taniguchi, J. Shi, *Phys. Rev. B* **96**, 041409 (2017).
60. S. Zihlmann, A.W. Cummings, J.H. Garcia, M. Kedves, K. Watanabe, T. Taniguchi, C. Schönenberger, P. Makk, *Phys. Rev. B* **97**, 075434 (2018).
61. T. Wakamura, F. Reale, P. Palczynski, S. Guéron, C. Mattevi, H. Bouchiat, *Phys. Rev. Lett.* **120**, 106802 (2018).
62. J.O. Island, X. Cui, C. Lewandowski, J.Y. Khoo, E.M. Spanton, H. Zhou, D. Rhodes, J.C. Hone, T. Taniguchi, K. Watanabe, L.S. Levitov, M.P. Zaletel, A.F. Young, *Nature* **571**, 85 (2019).
63. D. Wang, S. Che, G. Cao, R. Lyu, K. Watanabe, T. Taniguchi, C.N. Lau, M. Bockrath, *Nano Lett.* **19**, 7028 (2019).
64. Z. Wang, C. Tang, R. Sachs, Y. Barlas, J. Shi, *Phys. Rev. Lett.* **114**, 016603 (2015).
65. M.Z. Hasan, C.L. Kane, *Rev. Mod. Phys.* **82**, 3045 (2010).
66. X.-L. Qi, S.-C. Zhang, *Rev. Mod. Phys.* **83**, 1057 (2011).
67. S. Masatoshi, A. Yoichi, *Rep. Prog. Phys.* **80**, 076501 (2017).
68. R. Bistritzer, A.H. MacDonald, *Proc. Natl. Acad. Sci. U.S.A.* **108**, 12233 (2011).
69. J.M.B. Lopes dos Santos, N.M.R. Peres, A.H. Castro Neto, *Phys. Rev. Lett.* **99**, 256802 (2007).
70. Y. Cao, V. Fatemi, S. Fang, K. Watanabe, T. Taniguchi, E. Kaxiras, P. Jarillo-Herrero, *Nature* **556**, 43 (2018).
71. Y. Cao, V. Fatemi, A. Demir, S. Fang, S.L. Tomarken, J.Y. Luo, J.D. Sanchez-Yamagishi, K. Watanabe, T. Taniguchi, E. Kaxiras, R.C. Ashoori, P. Jarillo-Herrero, *Nature* **556**, 80 (2018).

72. X. Lu, P. Stepanov, W. Yang, M. Xie, M.A. Aamir, I. Das, C. Urgell, K. Watanabe, T. Taniguchi, G. Zhang, A. Bachtold, A.H. MacDonald, D.K. Efetov, *Nature* **574**, 653 (2019).
73. M. Serlin, C.L. Tschirhart, H. Polshyn, Y. Zhang, J. Zhu, K. Watanabe, T. Taniguchi, L. Balents, A.F. Young, *Science* **367**, 900 (2020).
74. M. Yankowitz, S. Chen, H. Polshyn, K. Watanabe, T. Taniguchi, D. Graf, A.F. Young, C.R. Dean, *Science* **363**, 1059 (2019).
75. F. Wu, T. Lovorn, E. Tutuc, I. Martin, A.H. MacDonald, *Phys. Rev. Lett.* **122**, 086402 (2019).
76. F. Wu, T. Lovorn, E. Tutuc, A.H. MacDonald, *Phys. Rev. Lett.* **121**, 026402 (2018).
77. F. Xue, A.H. MacDonald, *Phys. Rev. Lett.* **120**, 186802 (2018).
78. R.E. Prange, S.M. Girvin, Eds., *The Quantum Hall Effect* (Springer-Verlag, New York, 1987).
79. C.L. Kane, E.J. Mele, *Phys. Rev. Lett.* **95**, 226801 (2005).
80. Z. Fei, T. Palomaki, S. Wu, W. Zhao, X. Cai, B. Sun, P. Nguyen, J. Finney, X. Xu, D.H. Cobden, *Nat. Phys.* **13**, 677 (2017).
81. S. Wu, V. Fatemi, Q.D. Gibson, K. Watanabe, T. Taniguchi, R.J. Cava, P. Jarillo-Herrero, *Science* **359**, 76 (2018).
82. B.A. Bernevig, T.L. Hughes, S.-C. Zhang, *Science* **314**, 1757 (2006).
83. G.M. Gusev, Z.D. Kvon, O.A. Shegai, N.N. Mikhailov, S.A. Dvoretzky, J.C. Portal, *Phys. Rev. B* **84**, 121302 (2011).
84. I. Knez, R.-R. Du, G. Sullivan, *Phys. Rev. Lett.* **107**, 136603 (2011).
85. M. König, S. Wiedmann, C. Brüne, A. Roth, H. Buhmann, L.W. Molenkamp, X.-L. Qi, S.-C. Zhang, *Science* **318**, 766 (2007).
86. T. Li, P. Wang, H. Fu, L. Du, K.A. Schreiber, X. Mu, X. Liu, G. Sullivan, G.A. Csáthy, X. Lin, R.-R. Du, *Phys. Rev. Lett.* **115**, 136804 (2015).
87. A. Roth, C. Brüne, H. Buhmann, L.W. Molenkamp, J. Maciejko, X.-L. Qi, S.-C. Zhang, *Science* **325**, 294 (2009).
88. K. Suzuki, Y. Harada, K. Onomitsu, K. Muraki, *Phys. Rev. B* **87**, 235311 (2013).
89. B.A. Bernevig, S.C. Zhang, *Phys. Rev. Lett.* **96**, 106802 (2006).
90. M. König, S. Wiedmann, C. Brüne, A. Roth, H. Buhmann, L.W. Molenkamp, X.L. Qi, S.C. Zhang, *Science* **318**, 766 (2007).
91. A. Roth, C. Brüne, H. Buhmann, L.W. Molenkamp, J. Maciejko, X.-L. Qi, S.-C. Zhang, *Science* **325**, 294 (2009).
92. R. Yu, W. Zhang, H.J. Zhang, S.C. Zhang, X. Dai, Z. Fang, *Science* **329**, 61 (2010).
93. M. Onoda, N. Nagaosa, *Phys. Rev. Lett.* **90**, 206601 (2003).
94. F.D.M. Haldane, *Phys. Rev. Lett.* **61**, 2015 (1988).
95. C.-Z. Chang, J. Zhang, X. Feng, J. Shen, Z. Zhang, M. Guo, K. Li, Y. Ou, P. Wei, L.-L. Wang, Z.-Q. Ji, Y. Feng, S. Ji, X. Chen, J. Jia, X. Dai, Z. Fang, S.-C. Zhang, K. He, Y. Wang, L. Lu, X.-C. Ma, Q.-K. Xue, *Science* **340**, 167 (2013).
96. C.-Z. Chang, W. Zhao, D.Y. Kim, H. Zhang, B.A. Assaf, D. Heiman, S.-C. Zhang, C. Liu, M.H.W. Chan, J.S. Moodera, *Nat. Mater.* **14**, 473 (2015).
97. J.G. Checkelsky, R. Yoshimi, A. Tsukazaki, K.S. Takahashi, Y. Kozuka, J. Falson, M. Kawasaki, Y. Tokura, *Nat. Phys.* **10**, 731 (2014).
98. M. Mogi, R. Yoshimi, A. Tsukazaki, K. Yasuda, Y. Kozuka, K.S. Takahashi, M. Kawasaki, Y. Tokura, *Appl. Phys. Lett.* **107**, 182401 (2015).
99. Y. Deng, Y. Yu, M.Z. Shi, Z. Guo, Z. Xu, J. Wang, X.H. Chen, Y. Zhang, *Science* **367**, 895 (2020).
100. G. Chen, A.L. Sharpe, E.J. Fox, Y.-H. Zhang, S. Wang, L. Jiang, B. Lyu, H. Li, K. Watanabe, T. Taniguchi, Z. Shi, T. Senthil, D. Goldhaber-Gordon, Y. Zhang, F. Wang, "Tunable Correlated Chern Insulator and Ferromagnetism in Trilayer Graphene/Boron Nitride Moiré Superlattice," preprint, submitted arXiv:1905.06535 (2019).
101. J. Knolle, R. Moessner, *Annu. Rev. Condens. Matter Phys.* **10**, 451 (2019).
102. L. Savary, L. Balents, *Rep. Prog. Phys.* **80**, 016502 (2016).
103. C. Broholm, R.J. Cava, S.A. Kivelson, D.G. Nocera, M.R. Norman, T. Senthil, *Science* **367**, eaay0668 (2020).
104. T. Imai, Y.S. Lee, *Phys. Today* **69**, 30 (2016).
105. L.V. Butov, *Solid State Commun.* **127**, 89 (2003).
106. J.P. Eisenstein, *Annu. Rev. Condens. Matter Phys.* **5**, 159 (2014).
107. Y. Yu, A.W. Bataller, R. Younts, Y. Yu, G. Li, A.A. Puretzky, D.B. Geohegan, K. Gundogdu, L. Cao, *ACS Nano* **13**, 10351 (2019).
108. X. Liu, K. Watanabe, T. Taniguchi, B.I. Halperin, P. Kim, *Nat. Phys.* **13**, 746 (2017).
109. Z. Wang, D.A. Rhodes, K. Watanabe, T. Taniguchi, J.C. Hone, J. Shan, K.F. Mak, *Nature* **574**, 76 (2019).
110. M. Li, G. Chen, *MRS Bull.* **45** (5), 348 (2020).
111. L.V. Butov, *MRS Bull.* **45** (5), 380 (2020).
112. W.S. Torres, J.F. Sierra, L.A. Benítez, F. Bonell, J.H. García, S. Roche, S.O. Valenzuela, *MRS Bull.* **45** (5), 357 (2020).
113. C.-L. Song, X.-C. Ma, Q.-K. Xue, *MRS Bull.* **45** (5), 366 (2020).
114. K.L. Wang, Y. Wu, C. Eckberg, G. Yin, Q. Pan, *MRS Bull.* **45** (5), 373 (2020). □



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