

RESEARCH ARTICLE

Force tracking smooth adaptive admittance control in unknown environment

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Abstract

In this research, a force tracking smoothing adaptive admittance controller is proposed that grants precise contact forces (performance necessary for many critical interaction tasks such as polishing) for unknown interaction environments (e.g., leather or thin and soft materials). First, an online indirect adaptive update strategy is proposed for generating the reference trajectory required by the desired tracking force, considering the uncertainty of the interaction. The sensor noise amplitude is environment dynamics and the necessity condition for traditional admittance controller to achieve ideal steady-state force tracking. Then, a pre-PD controller is introduced to increase the parameter convergence rate while ensuring the steady-state force tracking accuracy and enhancing the robustness of the system. The robustness boundary is also analyzed to provide assurance for the stability of the system. Finally, we verify the effectiveness of the proposed method in simulations. Simultaneously, an experiment is conducted on the AUBO-i5 serial collaborative robot, and the experimental results proved the excellent comprehensive performance of the control framework.

1. Introduction

In recent years, research in the field of robotics has made rapid progress thanks to the unremitting efforts of many researchers [1–3]. Among them, the contact interaction between robots and unknown physical environments is becoming an important part of robot applications, such as surface treatment of thin-walled parts [4–6], medical rehabilitation and physiotherapy [7–9], physical human-robot interaction [10–14], and humanoid robots [15, 16]. It is well known that the essential problem of the interaction between the robot and the physical environment is to control the magnitude of the interaction force to prevent it from reaching the unbearable range of the control object and directly leading to the failure of the task or even more serious consequences. Such force overshoot may be due to measurement or communication delays, uncertainties in the robot/environment dynamics model, and discontinuities in controller inputs. To solve this thorny problem, researchers have proposed some active compliance control methods.

Hybrid position/force control [17] and impedance control [18–20] are the most widely used compliance control schemes, and they can be distinguished by the relationship between position and force. The hybrid position/force control defines the entire workspace as two task subspaces, which are called position control subspace and force control subspace, and the position controller and the force controller act on the corresponding subspaces, separately. The proper division of the task subspace is the most important step in the overall control strategy, and it depends on prior knowledge of the environment structure and geometry. However, it is difficult to obtain accurate environmental geometry information in advance, which limits the application of the robot in unknown physical environments. In particular,

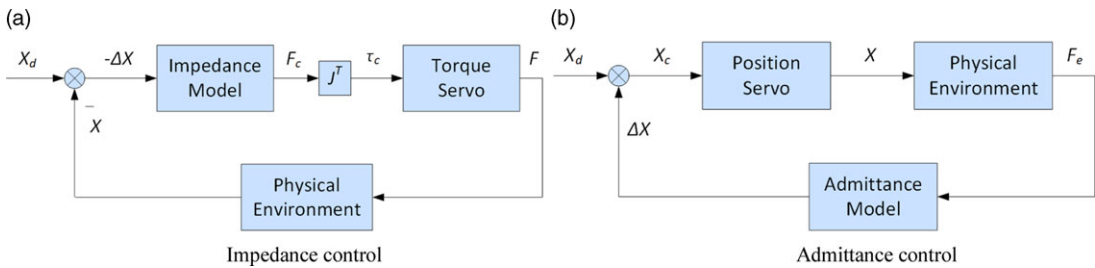


Figure 1. The implementation comparison of impedance and admittance control.

the hybrid position/force control strategy does not consider the physical coupling between the robot and the interaction environment and yields better control performance only when more accurate external force signals are obtained. Also, it cannot consider both force control and position control in the same direction [21]. In addition, switching different control modes according to the division of the subspace will also lead to some unstable responses.

In contrast, impedance control couples the inherently independent robot and the interaction environment by establishing the dynamic relationship between the interaction force error and the position error [22, 23]. Thus, impedance control performs better in terms of “flexibility” and “adaptability” [24]. “Flexibility” means that the target impedance parameters can be designed flexibly to make the robot have the compliance required for the task. “Adaptability” has two aspects. At first, impedance control is adapted to different phases of the operational task. Specifically, the robot can employ a unified impedance model in free space, contact space, and transition space of contact interaction without the need to switch other control modes. Then, impedance control can be adapted to a variety of unknown environments, which also reflects the inherent robustness of impedance control.

As shown in Fig. 1, there are two general categories depending on whether the robot’s inner loop is position or torque-controlled: position-based impedance control (admittance control) and dynamic-based impedance control, which usually appear in pairs. Since the inner loop of admittance control is position control, it can be implemented on most industrial robots with a position control interface, and its control performance mainly depends on the accuracy of the position control [25]. At present, robot position control can achieve high control accuracy, so it has better robustness [26, 27]. Therefore, the follow-up research in this article is based on the discussion of admittance control.

Force tracking has attracted many researchers in the last decades [28–31]. For the situation where the environmental dynamics parameters are known, the traditional force control strategies can achieve good performance. But for the unknown interactive environment, the control performance depends mainly on the accuracy of the environmental dynamic parameters with which the robot interacts. Given this, the research on adaptive controllers plays an extremely important role in improving the control performance of robot interaction tasks. To address this critical issue, Horak *et al.* [32] describe four current mainstream interaction models and their differences and proposed accordingly: Projected Gauss-Seidel method, which applies to all solvers. It plays an important role in solving the coupling system of the robot interaction environment. Ott *et al.* [33] enhance the robustness of the impedance controller in unknown environments by switching the controller online by sensing the dynamic interactive environment and considering different adaptation scenarios of impedance and admittance control. Seraji *et al.* [34] design two adaptive environment identification algorithms to deal with the uncertainty of environmental parameters. The first scheme uses the model-reference adaptive control to generate the reference position online based on the force tracking error, and the second scheme uses the indirect adaptive strategy to estimate the environmental dynamics parameters online by designing the Lyapunov function. Jung *et al.* [35] propose a simple algorithm for determining reference trajectories in the presence of unknown environments. This algorithm was developed based on force sensor data to replace unknown stiffnesses and combined with an impedance function resulting in a force tracking impedance model. Roveda *et al.*

[36] design the extended Kalman filter and the Kalman filter for estimating the environmental stiffness and the robot's base position, respectively. Then, they propose a closed-loop system to track the target force by compensating for the base deformation, and its consistent stability is verified. Valency *et al.* [37] study feedback methods for implementing impedance control and reveal a fundamental conflict between impedance accuracy and uncertainty robustness. And then, they propose a novel and practical approach to promote system robustness and maintain accurate impedance tracking.

The above research has improved the overall performance of impedance-controlled robots from different perspectives and greatly improved the compliance of the robots. However, the ability of robots to perform tasks in unknown environments is still limited. In particular, few researches have considered both the dynamic characteristics of the interaction environment, the transient convergence rate, and steady-state tracking characteristics, which results in limited global adaptability of the impedance-controlled robot.

In response to the above challenges, this research proposes a smooth adaptive admittance controller (SAAC) considering these issues simultaneously to ensure the global performance of the robot.

The contributions of this research can be summarized as follows:

- a. Environmental dynamics are considered in the optimal interaction analysis, which is described as an unknown linear system.
- b. A pre-PD controller has been introduced to improve the admittance model, combined with an indirect adaptive update strategy to enhance the force control performance of the robot control system to cope with unknown interaction environments.
- c. The stability and robustness of the proposed method are proven for stable and reliable force tracking execution.
- d. The adaptive parameters are adjusted in real time by a task-oriented algorithm without the need for training data, which ensures the precise force interaction between the robot and any unknown environment.

The rest of this article is organized as follows: Section 2 introduces the system model and compliance control strategy. Section 3 shows the overall control framework of this research. Section 4 gives the simulation results, and Section 5 gives the experimental results. Finally, Section 6 concludes the research.

2. System model and compliance control

2.1. Environmental dynamics model

As shown in Fig. 2, the environmental dynamics model is defined as

$$F_e(t) = K_e(t)(X_e(t) - X(t)) \quad (1)$$

where F_e is the interaction force between the robot and the unknown environment, K_e is the environment stiffness, X_e is the equilibrium position of the environment, X is the current position of the robot. It is important to emphasize that the environmental mass M_e and damping B_e are not considered. (as in many works, such as in [34, 38])

2.2. Traditional admittance control

The purpose of the admittance control is to establish the dynamic relationship between the robot interaction force error E_f and the difference ΔX between the desired position X_d of the robot and the commanded position X_c . The traditional admittance model is

$$E_f(t) = F_d(t) - F_e(t) = M [\ddot{X}_d(t) - \ddot{X}_c(t)] + B [\dot{X}_d(t) - \dot{X}_c(t)] + K [X_d(t) - X_c(t)] \quad (2)$$

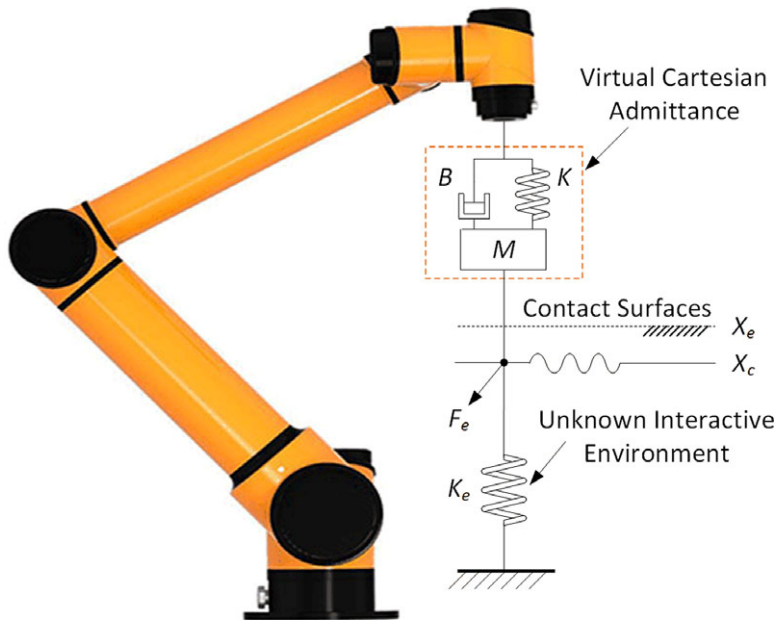


Figure 2. The graphic representation of robots interacting with an unknown environment.

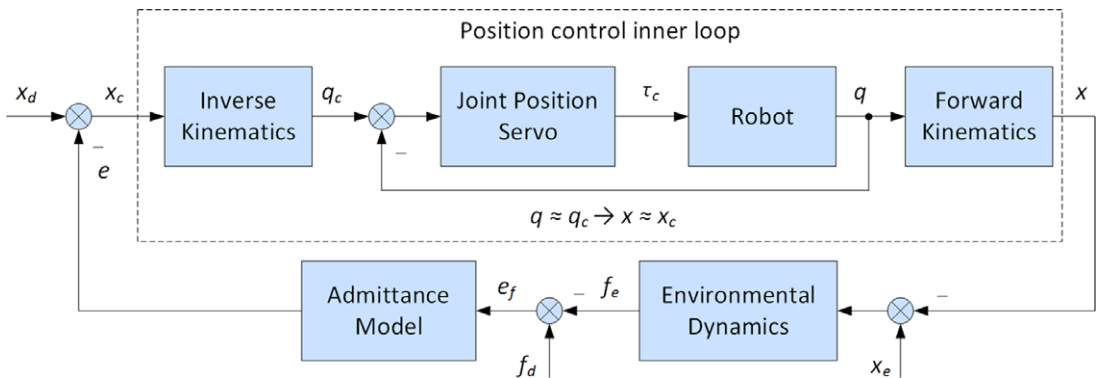


Figure 3. The schematic diagram of AC.

where $M \in R^{n \times n}$, $B \in R^{n \times n}$, and $K \in R^{n \times n}$ are diagonal mass, damping, and stiffness matrix of the admittance model. $F_d \in R^n$ and $F_e \in R^n$ represent the desired tracking force and the actual interaction force between the robot and the unknown environment. At present, robot position control technology is quite mature, so $X \approx X_c$ is considered correct.

To simplify the expression, this research investigates the one-dimensional case by using the symbols e_f, f_d, f_e, x_d, x_c , and x instead of E_f, F_d, F_e, X_d, X_c , and X . Thus, Eq. (2) can be reformulated as follows:

$$e_f(t) = f_d(t) - f_e(t) = m\ddot{e}(t) + b\dot{e}(t) + ke(t) \tag{3}$$

where $e(t) = x_d(t) - x_c(t)$.

Similarly, using k_e, x_e instead of K_d, X_e , Eq. (1) can be simplified as

$$f_e(t) = k_e(x_e(t) - x(t)) \tag{4}$$

The detailed schematic diagram of admittance control is shown in Fig. 3.

To simplify the analysis, the environmental stiffness k_e is assumed to be time-invariant, yields

$$e_f(t) = m \left[\ddot{x}_d(t) - \ddot{x}_e(t) + \frac{\dot{f}_d(t) - \dot{e}_f(t)}{k_e} \right] + b \left[\dot{x}_d(t) - \dot{x}_e(t) + \frac{f_d(t) - e_f(t)}{k_e} \right] + k \left[x_d(t) - x_e(t) + \frac{f_d(t) - e_f(t)}{k_e} \right] \tag{5}$$

Laplace transform of Eq. (5) can be obtained

$$k_e e_f(s) = (ms^2 + bs + k) [k_e(x_d(s) - x_e(s)) + f_d(s) - e_f(s)] \tag{6}$$

The environmental position x_e and the desired tracking force f_d are assumed to change like step functions such that their Laplace transforms become $x_e(s) = x_e/s$ and $f_d(s) = f_d/s$ with constant x_e and f_d . Then, Eq. (6) is simplified and Eq. (7) can be obtained from the final value theorem.

$$e_{ss} = \lim_{s \rightarrow 0} s e_f(s) = \lim_{s \rightarrow 0} \frac{s(ms^2 + bs + k) [k_e(x_d(s) - x_e(s)) + f_d(s)]}{ms^2 + bs + k + k_e} = \frac{k [k_e(x_d - x_e) + f_d]}{k + k_e} \tag{7}$$

If one makes the steady-state tracking error asymptotically stable, the reference trajectory x_d needs to meet the following conditions:

$$x_d = x_e - \frac{f_d}{k_e} \tag{8}$$

However, the equilibrium position x_e and stiffness k_e of the environment cannot be accurately known, and it is difficult to measure during the robot’s task execution. Therefore, the indirect adaptive update strategy will be used to estimate the environmental dynamics parameters, and then to obtain the reference trajectory required by the desired tracking force.

3. Overall control framework

3.1. Adaptive admittance control

In order to obtain the reference trajectory x_d of the robot, an indirect adaptive update strategy is used in this research to estimate the environmental stiffness parameter k_e and the environmental equilibrium position x_e online. Assuming that the estimated values of environmental stiffness k_e and environmental equilibrium position x_e are \hat{k}_e and \hat{x}_e , the estimated external force \hat{f}_e is

$$\hat{f}_e = \hat{k}_e(\hat{x}_e - x) = \hat{k}_e \hat{x}_e - \hat{k}_e x = \hat{k}_x - \hat{k}_e x \tag{9}$$

Defining $\varnothing = \begin{bmatrix} \varnothing_1 \\ \varnothing_2 \end{bmatrix} = \begin{bmatrix} \hat{k}_e - k_e \\ \hat{k}_x - k_x \end{bmatrix}$ and substituting into Eq. (9), yields

$$\hat{f}_e - f_e = \hat{k}_e \hat{x}_e - k_e x_e - \hat{k}_e x + k_e x = \hat{k}_x - k_x + (k_e - \hat{k}_e) x = [-x \quad 1] \varnothing \tag{10}$$

A control strategy is designed based on the “prediction error” $\hat{f}_e - f_e$ to dynamically adjust \hat{k}_e and \hat{x}_e , such that when $t \rightarrow \infty, \hat{f}_e \rightarrow f_e$. When $\hat{f}_e = f_e$, yields

$$f_e = \hat{k}_e \hat{x}_e - \hat{k}_e x = \hat{k}_e \left(x_d + \frac{f_d}{k_e} \right) - \hat{k}_e x = f_d + \hat{k}_e(x_d - x) \tag{11}$$

So

$$f_d - f_e = e_f = -\hat{k}_e(x_d - x) \tag{12}$$

Substituting Eqs. (12), (3) is expressed as

$$m\ddot{e} + b\dot{e} + (k + \hat{k}_e) e = 0 \tag{13}$$

Thus, when $\hat{f}_e \rightarrow f_e$, either $\hat{k}_e \rightarrow -k$ or $e \rightarrow 0$. The former case $\hat{k}_e \rightarrow -k$ is well avoided, since k_e is greater than zero, and \hat{k}_e is a strictly positive definite estimation. The latter case $e \rightarrow 0$ means $x \rightarrow x_d$, that is $f_e \rightarrow f_d$.

Remark: In above derivation, \hat{k}_e and \hat{x}_e do not have to converge to the true values of the environmental model parameters, but only one utilizes \hat{k}_e and \hat{x}_e to designed an adaptive update law such that $f_e \rightarrow f_d$ when $\hat{f}_e \rightarrow f_e$.

Based on the above theoretical derivation, the corresponding Lyapunov function is designed as

$$V = \varnothing^T P \varnothing \tag{14}$$

where P is the positive real diagonal matrix defined in advance.

Taking the first-time derivative of V yields

$$\dot{V} = 2\varnothing^T P \dot{\varnothing} \tag{15}$$

From the second method of Lyapunov and LaSalle’s invariance principle, we know that the condition for system stability is $\dot{V} \leq 0$. Thus, based on Eq. (4), we design $\dot{\varnothing} = -P^{-1} \begin{bmatrix} -x \\ 1 \end{bmatrix} (\hat{f}_e - f_e)$, and substituting it into the Eq. (15) yields:

$$\dot{V} = -2 \begin{bmatrix} \hat{k}_e - k_e & \hat{k}_x - k_x \end{bmatrix} \begin{bmatrix} -x \\ 1 \end{bmatrix} (\hat{f}_e - f_e) = -2(\hat{f}_e - f_e)^2 \leq 0 \tag{16}$$

Thus, the system is stable, and the environmental dynamics parameters can be calculated as follows:

$$\hat{k}_e(t) = \hat{k}_e(0) + \alpha \int_0^t x (\hat{f}_e - f_e) dt \tag{17}$$

$$\hat{x}_e(t) = \hat{x}_e(0) - \beta \int_0^t \frac{\hat{f}_e - f_e}{\hat{k}_e(t)} \left(\frac{\alpha}{\beta} x \hat{x}_e(t) + 1 \right) dt \tag{18}$$

where $\alpha = P_{11}^{-1}$, $\beta = P_{22}^{-1}$, P_{11} , P_{22} are positive scalar constants. f_e is obtained from a 6-axis force sensor installed at the end of the robot, and \hat{f}_e is calculated from \hat{k}_e and \hat{x}_e .

Finally, the reference trajectory can be obtained as

$$\hat{x}_d(t) = \hat{x}_e(t) - \frac{f_d(t)}{\hat{k}_e(t)} \tag{19}$$

In summary, the whole indirect adaptive update strategy is carried out based on the main line of estimating \hat{k}_e and \hat{x}_e to obtain \hat{x}_d . The Lyapunov function is designed based on \varnothing and $\dot{\varnothing}$ is designed according to the stability criterion of the second method of Lyapunov to obtain the update law of \hat{k}_e and \hat{x}_e , so as to accomplish our desired goal: the accurate estimation of the desired trajectory \hat{x}_d to obtain the excellent force tracking performance of the robot.

The schematic diagram of adaptive admittance control (AAC) based on the indirect adaptive update strategy is shown in Fig. 4. However, due to the uncertainty of the environmental dynamics model, the steady-state tracking error will still exist. Therefore, a smooth adaptive admittance controller (SAAC) based on a pre-PD controller and indirect adaptive update strategy will be proposed to maximize the force tracking accuracy.

3.2. Smooth adaptive admittance control

Equation (3) reveals that the admittance model acts as a second-order low-pass filter. The force feedback signal is converted to a position correction signal in the admittance control framework. This greatly tests the trajectory tracking ability of the internal position controller, and a high-gain PD controller

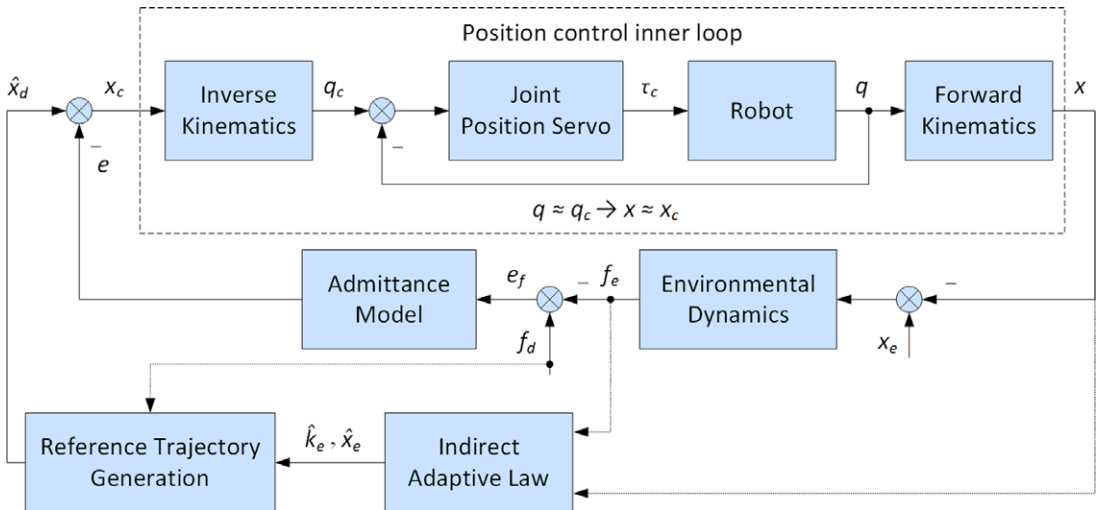


Figure 4. The schematic diagram of AAC. Compared with the AC, the modules of indirect adaptive law and reference trajectory generation have been added.

is generally used to improve the fast response-ability. For purpose of comprehensively improving the fast convergence ability of parameters, mitigating the influence of high gain of the internal position controller, and improving the accuracy of force tracking, a pre-PD controller is put forth to improve the admittance model and it is designed as

$$k_p e_f(t) + k_d \dot{e}_f(t) = m\ddot{e}(t) + b\dot{e}(t) + ke(t) \tag{20}$$

where k_p and k_d are the proportional and differential gains of the pre-PD controller.

Referring to Eq. (7), the steady-state error expression of the system after the introduction of the pre-PD controller can be obtained as

$$e_{ss} = \lim_{s \rightarrow 0} s e_f(s) = \frac{s(ms^2 + bs + k) [k_e(x_d(s) - x_e(s)) + f_d(s)]}{ms^2 + (b + k_e k_d) s + k_e k_p + k_e + k} \tag{21}$$

The reference trajectory expression represented by the numerator of the Eq. (21) remains unchanged, and the increase in the denominator reduces the steady-state error. This feature reveals that integrating pre-PD controllers to improve the admittance model is reasonable because it not only coexists with the indirect adaptive update strategy but also improves the steady-state tracking accuracy. Figure 5 shows the schematic diagram of smooth adaptive admittance control (SAAC).

3.3. System robustness analysis

Stability is the ability of a system to return to the desired state when subjected to transient perturbations, while robustness is the ability of a system to maintain the desired state when subjected to continuous perturbations. Therefore, stability and robustness analysis are essential for control systems. As mentioned in Subsection 3.1, the stability of the system is derived by designing a suitable Lyapunov function. In this subsection, the robustness of the control system is analyzed.

Since the environmental position parameter x_e cannot be estimated precisely, the impact of these uncertainties on the control system performance must be considered. Therefore, two issues need to be addressed.

- a. Ensure that the robot is in contact with the physical environment.
- b. Achieving accurate force tracking for robots.

1. When the robot is in the contact space

Combining $x_d = x_e - \Delta x_d$ with Eq. (24) yields

$$\ddot{\delta} - \Delta \ddot{x}_d + \frac{1}{m} [b(\dot{\delta} - \Delta \dot{x}_d) + k(\delta - \Delta x_d) - k_p e_f - k_d \dot{e}_f] = 0 \tag{28}$$

where $\delta = x_e - x$. Meanwhile, $\Delta \ddot{x}_d = \Delta \dot{x}_d = 0$. Eq. (28) is simplified as

$$\ddot{\delta} + \frac{1}{m} \left[b\dot{\delta} + k\delta \left(1 - \frac{f_d}{f_e} \right) - k_p e_f - k_d \dot{e}_f \right] = 0 \quad \text{Contact Space} \tag{29}$$

2. When the robot is in free space

When the robot is in free space, Eq. (29) can be expressed according to Eq. (25) as

$$\ddot{\delta} + \frac{1}{m} (b\dot{\delta} + k\delta - k_p f_d - k_d \dot{f}_d) = 0 \quad \text{Free Space} \tag{30}$$

Obviously, the function of f_d is to drive the robot to approach from the free space to the contact space.

Suppose that the environmental position input of the control system is $\tilde{x}_e = x_e + \Delta x_e$, and Δx_e is the uncertain error of the environment. It can be assumed that $\tilde{\delta} = \delta + \Delta x_e$, by combining Eqs. (29) and (30), yields

$$\ddot{\tilde{\delta}} + \frac{1}{m} (b\dot{\tilde{\delta}} + k\tilde{\delta} - k_p f_d - k_d \dot{f}_d) = 0 \quad \text{Free Space} \tag{31}$$

$$\ddot{\tilde{\delta}} + \frac{1}{m} \left[b\dot{\tilde{\delta}} + k\tilde{\delta} \left(1 - \frac{f_d}{f_e} \right) - k_p e_f - k_d \dot{e}_f \right] = 0 \quad \text{Contact Space} \tag{32}$$

When the robot moves from free space to contact space, there must be an uncertain error Δx_e in the interaction environment. Therefore, the influence of this error parameter on the force control performance of the robot must be analyzed.

First, define $x_e > 0$, $x > 0$, so when $\Delta x_e < 0$, $\tilde{x}_e < x_e$. This means that \tilde{x}_e is lower than the actual environment equilibrium position x_e , and it is embedded in the actual environment. Similarly, $\Delta x_e > 0$ indicates $\tilde{x}_e > x_e$, which means that \tilde{x}_e is higher than the actual environment equilibrium position x_e , and it is far from the actual environment surface.

Case 1: $\Delta x_e > 0$.

Assuming that the initial state of the robot is in free space, which means $x > x_e$. Then, Eqs. (31) and (32) in steady state can be expressed as

$$k\tilde{\delta} - k_p f_d = 0 \quad \text{Free Space} \tag{33}$$

$$k_p f_e^2 + (k\tilde{\delta} - k_p f_d) f_e - k\tilde{\delta} f_d = 0 \quad \text{Contact Space} \tag{34}$$

Equation (33) can be converted into

$$k(x_e + \Delta x_e - x) - k_p f_d = 0 \text{ or } x = x_e + \Delta x_e - \frac{k_p f_d}{k} \tag{35}$$

After the above derivation, there are two possible steady-state results, the first result is $\Delta x_e - k_p f_d/k > 0$ (or $\Delta x_e > k_p f_d/k$), then $x > x_e$. This means that the robot is still not in contact with the environment at steady state. Therefore, the system will not work properly with this parameter in free space.

The second result is

$$\Delta x_e - k_p f_d/k < 0 \text{ (or } \Delta x_e < k_p f_d/k) \tag{36}$$

Then, $x < x_e$, which means that if $\Delta x_e < k_p f_d/k$, the robot must be in contact with the physical environment. This condition is easily satisfied. Once the robot is in contact with the environment, Eq. (34) can

be solved to obtain the following results

$$f_e = f_d \text{ and } f_e = -k\tilde{\delta}/k_p \tag{37}$$

Because $\Delta x_e > 0$, if the latter is to be established, k and k_e must be required to have opposite signs, so the latter cannot be established. Therefore, the former is realized when the system is stable, that is, the stable force tracking of the robot can be realized.

Case 2: $\Delta x_e < 0$.

When the robot is in free space, $x > x_e$, and because $\Delta x_e < k_p f_d / k$, so $x_e > x$ in steady state. Therefore, if $\tilde{x}_e < x_e$, the robot will also always be in contact with the physical environment. Referring to Eq. (37), it can also be solved as

$$f_e = f_d \text{ and } f_e = -k\tilde{\delta}/k_p \tag{38}$$

But since $\Delta x_e < 0$, only need Δx_e is very small to make both solutions hold. This means that precise force tracking of robots cannot be guaranteed.

To sum up, to make the robot come into contact with the physical environment, it must satisfy

$$\Delta x_e < k_p f_d / k \tag{39}$$

However, the upper boundary can only ensure that the robot is in contact with the physical environment, but cannot guarantee precise force tracking (as can be seen from the analysis of Case 2).

So, the lower boundary of Δx_e is analyzed to ensure precise force tracking.

From the above derivation, it can be obtained

$$\tilde{\delta} = \frac{f_e}{k_e} + \Delta x_e, \dot{\tilde{\delta}} = \frac{\dot{f}_e}{k_e} + \Delta \dot{x}_e, \ddot{\tilde{\delta}} = \frac{\ddot{f}_e}{k_e} + \Delta \ddot{x}_e \tag{40}$$

Substituting Eq. (40) into Eq. (29), a new differential equation of the admittance control system is calculated as

$$\begin{aligned} \ddot{f}_e + \frac{b + k_d k_e}{m} \dot{f}_e + \frac{k + k_p k_e}{m} f_e - \frac{k k_e f_d \Delta x_e}{m f_e} \\ = -k_e \Delta \ddot{x}_e + \frac{(k_p k_e - k) f_d + k_d k_e \dot{f}_d - k k_e \Delta x_e - b k_e \Delta \dot{x}_e}{m} \end{aligned} \tag{41}$$

Since $\Delta \ddot{x}_e = \Delta \dot{x}_e = 0$, simplify Eq. (41)

$$\ddot{f}_e + \frac{b + k_d k_e}{m} \dot{f}_e + \frac{k + k_p k_e}{m} f_e - \frac{k k_e f_d \Delta x_e}{m f_e} = \frac{1}{m} [(k_p k_e - k) f_d + k_d k_e \dot{f}_d - k k_e \Delta x_e] \tag{42}$$

This is a nonlinear equation concerning the variable f_e , and two solutions about Eq. (29) are obtained as follows:

$$f_e = f_d \text{ and } f_e = -k\tilde{\delta}/k_p \tag{43}$$

This allows us to calculate the stable conditions for the equilibrium state.

Defining symbols $x_1 = f_e, x_2 = \dot{f}_e$, the state equation can be rewritten as:

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = -\frac{b + k_d k_e}{m} x_2 - \frac{k + k_p k_e}{m} x_1 + \frac{k k_e f_d \Delta x_e}{m x_1} + \frac{(k_p k_e - k) f_d + k_d k_e \dot{f}_d - k k_e \Delta x_e}{m} \end{cases} \tag{44}$$

In equilibrium, $f_e = f_d, \dot{f}_d = 0$. Equation (44) becomes the linear equation of f_e . So, when $x_1 = f_d, x_2 = 0$, the state equation can rewrite as

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -\frac{kk_e \Delta x_e}{mf_d} - \frac{k + k_p k_e}{m} & -\frac{b + k_d k_e}{m} \end{bmatrix} x + \begin{bmatrix} 0 \\ \frac{(k_p k_e - k) f_d + k_d k_e \dot{f}_d - kk_e \Delta x_e}{m} \end{bmatrix} \quad (45)$$

The characteristic equation of this state matrix is

$$\det(sI - A) = s^2 + \frac{b + k_d k_e}{m} s + \frac{k + k_p k_e}{m} + \frac{kk_e \Delta x_e}{mf_d} = 0 \quad (46)$$

Then, the stability conditions of the system are

$$\frac{b + k_d k_e}{m} > 0 \text{ or } \frac{k + k_p k_e}{m} + \frac{kk_e \Delta x_e}{mf_d} > 0 \quad (47)$$

Since m, b , and k_d are already selected parameters, we only need to ensure that

$$\Delta x_e > -\frac{(k + k_p k_e) f_d}{kk_e} \quad (48)$$

Therefore, at the equilibrium state of $f_e = f_d$, the conditions that need to be satisfied are

$$\Delta x_e > -\frac{(k + k_p k_e) f_d}{kk_e} \text{ at } f_e = f_d \quad (49)$$

Similarly, when $f_e = -k\tilde{\delta}/k_p$ yields

$$f_e = -k\tilde{\delta}/k_p = -k\left(\frac{f_e}{k_e} + \Delta x_e\right)/k_p \Rightarrow f_e = -\frac{kk_e}{k_p k_e + k} \Delta x_e \quad (50)$$

In the equilibrium state $x_1 = -k\tilde{\delta}/k_p, x_2 = 0$, the state equation is

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ -\frac{f_d(k_p + k_e)^2}{mkk_e \Delta x_e} - \frac{k + k_p k_e}{m} & -\frac{b + k_d k_e}{m} \end{bmatrix} x + \begin{bmatrix} 0 \\ \frac{(k_p k_e - k) f_d + k_d k_e \dot{f}_d - kk_e \Delta x_e}{m} \end{bmatrix} \quad (51)$$

The characteristic equation of the state matrix is

$$\det(sI - A) = s^2 + \frac{b + k_d k_e}{m} s + \frac{k + k_p k_e}{m} + \frac{f_d(k_p + k_e)^2}{mkk_e \Delta x_e} = 0 \quad (52)$$

Then, the stability conditions of the system are

$$\frac{b + k_d k_e}{m} > 0 \text{ or } \frac{k + k_p k_e}{m} + \frac{f_d(k_p + k_e)^2}{mkk_e \Delta x_e} > 0 \quad (53)$$

So, it should be satisfied as

$$\Delta x_e < -\frac{f_d(k_p + k_e)^2}{k_e k(k + k_p k_e)} \text{ at } f_e = f_d \quad (54)$$

This situation should be avoided. Combining Eq. (39) with (49), the upper and lower boundaries of Δx_e can be obtained as

$$-\frac{(k + k_p k_e) f_d}{kk_e} < \Delta x_e < \frac{k_p f_d}{k} \quad (55)$$

Meanwhile, the upper boundary of Eq. (55) is known a priori because k_p, f_d , and k are the values initially specified by the user. The lower boundary of Eq. (55) is not known because k_e is unknown. So,

when the interactive environment is hard, that means $k_e \gg k_d$, considering

$$-\frac{(k + k_p k_e) f_d}{k k_e} \approx -\frac{k_p f_d}{k} \quad (56)$$

So, the upper and lower boundaries of Δx_e can be rewritten as

$$-\frac{k_p f_d}{k} < \Delta x_e < \frac{k_p f_d}{k} \quad (57)$$

Because the robot is equipped with a relatively precise force sensor, the actual environmental position x_e can be estimated accurately, so the environmental uncertainty Δx_e is usually relatively small, as long as f_d , k_p , k are chosen appropriately, the system will remain stable. At the same time, the introduction of the pre-PD controller can expand the upper and lower boundary of the environmental uncertainty Δx_e , which means that the robustness of the system is enhanced.

3.4. Discretization of control algorithms

Nowadays, most robot controllers are developed based on the upper computer or embedded microprocessor, so they all work in the discrete-time domain. Therefore, the continuous control algorithm should be converted from the S domain to the discrete-time domain, and the discrete implementation of the proposed algorithm is shown in Fig. 6. First, the parameters of the target admittance model, the pre-PD controller, and the indirect adaptive update strategy are initialized. Second, the contact force $f_e(n)$ and the motion state $x(n)$ of the robot at the current moment are feedback to the upper computer, and the values of $e_f(n)$ and $\dot{e}_f(n)$ are calculated by combining the desired tracking force $f_d(n)$. Third, the values of $\hat{f}_e(n)$, $\hat{k}_e(n)$, and $\hat{x}_e(n)$ are obtained by the indirect adaptive update strategy. Fourth, the reference trajectory $x_d(n)$ of the admittance model can be derived. Fifth, the reference trajectory $x_d(n)$ is substituted into the pre-PD admittance controller and the value of $e(n+1)$ obtained by double integration. Finally, the command trajectory $x_c(n+1)$ of the next moment is generated and sent to the robot motion servo system. When the next period is performed, the system status returns to the second step.

4. Simulation

This section verifies the performance of the designed algorithm based on the MATLAB/SIMULINK platform, where the interactive scenarios include a structured environment (The stiffness parameter k_e of the environment is constant) and a dynamic environment (The stiffness parameter k_e of the environment is dynamically varying). The simulation program mainly includes the admittance model, pre-PD controller, robot motion servo system, and environmental dynamics model, as shown in Fig. 7.

4.1. Simulation parameters setting

For purpose of verifying the system response speed and steady-state tracking accuracy of the designed control algorithm, it is assumed that the robot moves along the z -axis on the horizontal plane, the control period is $T = 0.005$ (s), the sensor noise amplitude is $1 \times e^{-4}$ to simulate the white noise, and other simulation-related parameters have been shown in Table I.

4.2. Simulation results

The motion of the robot in the simulation is divided into three stages as follows:

- Firstly, the robot starts moving from free space driven by the desired force of the admittance model.

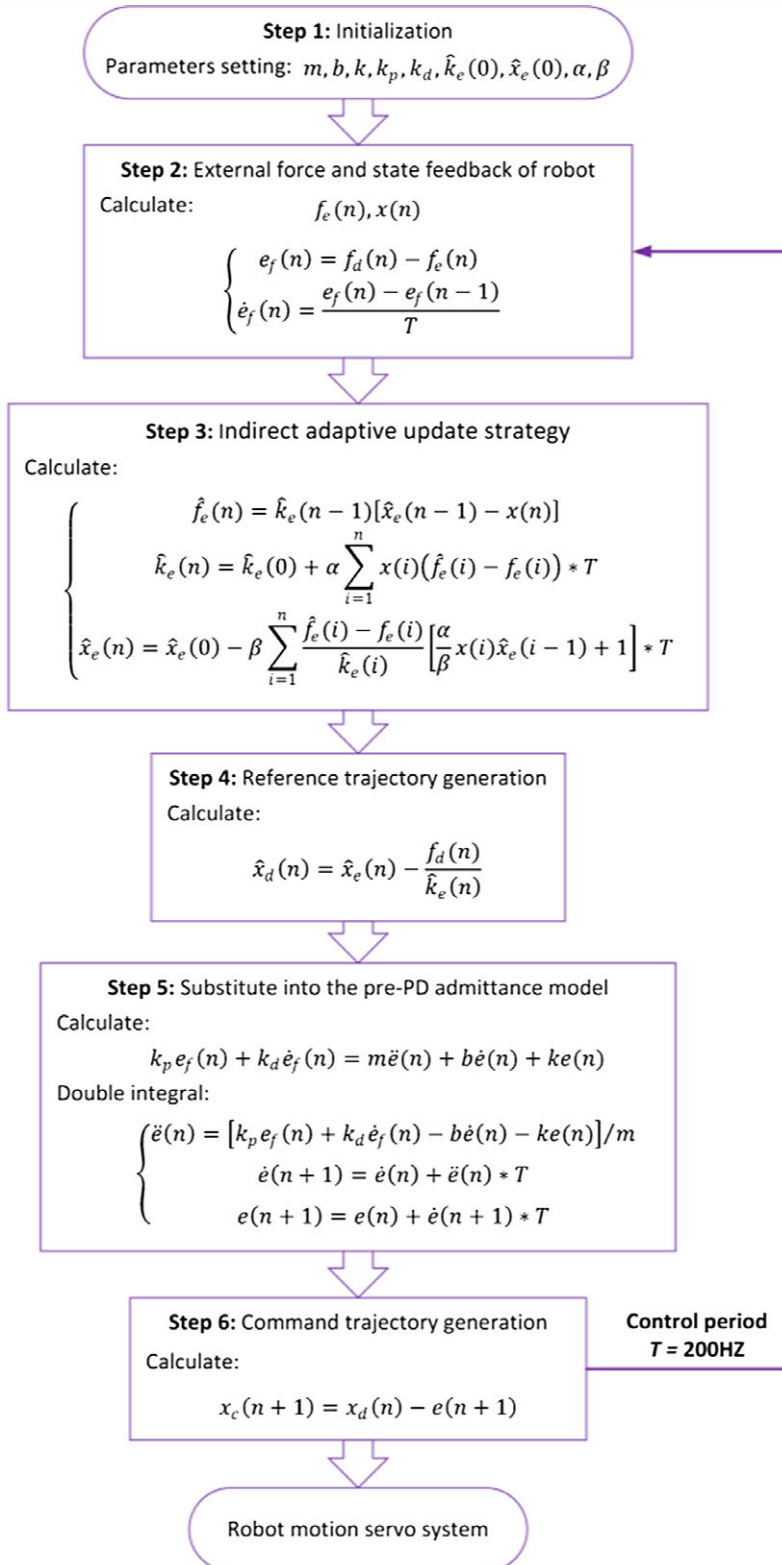


Figure 6. The discrete implementation of the SAAC algorithm.

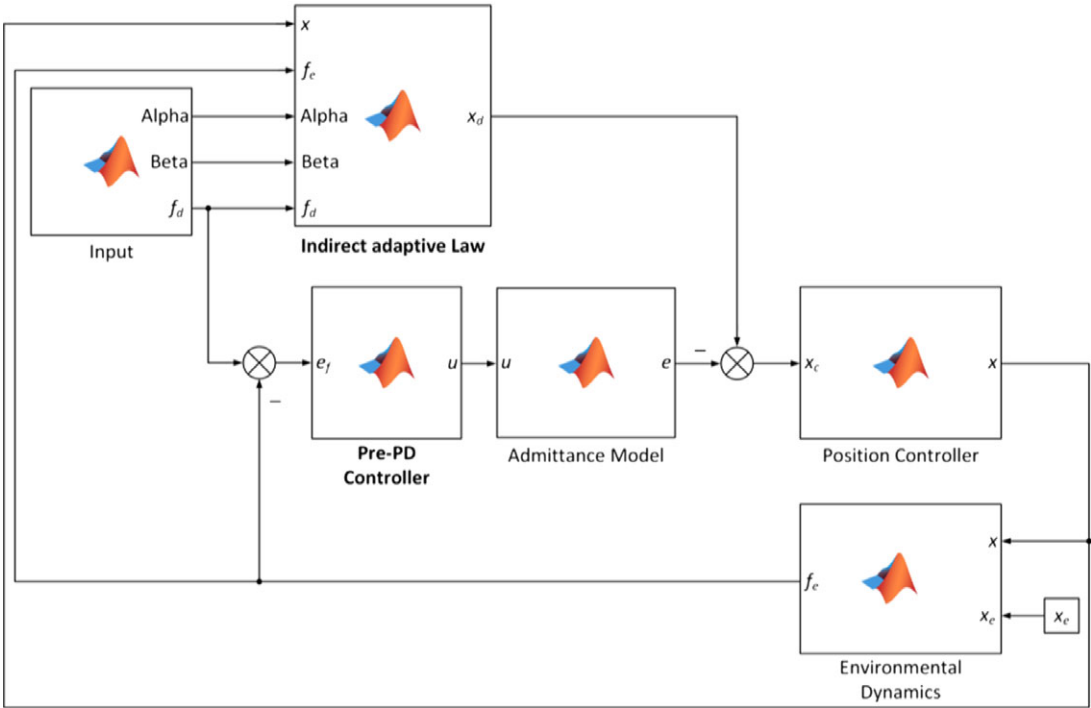


Figure 7. The simulation block diagram of the SAAC.

- Then, the robot is in contact with the physical environment until stabilization.
- Finally, the desired force is accurately tracked to accomplish the related force control task.

Transient response speed and steady-state tracking accuracy are used to synthesize the system performance. The former consists of the following two metrics.

(a) The time from free space to contact transient of the robot. It is artificially defined and named contact time t_c , the shorter t_c , the faster the response speed.

(b) The time from contact transient to stable tracking phase of the robot. Called the setting time t_s in control theory. This is the minimum time required for the response to arrive and remain within $\pm 5\%$ of the desired value, and it is also a composite indicator to evaluate the speed of response and the degree of damping of the system.

The latter is represented by the steady-state error e_f , which is a metric of the system's control accuracy or immunity to disturbances.

The force control performance of AAC and SAAC were compared under different environmental stiffnesses and different desired tracking forces as shown in Fig. 8(a), (b), and (c).

As can be seen from Fig. 8(a), one compares the force control curves of AAC and SAAC at $f_d = 10$ (N), $k_e = 1000$ (N/m). In the transient contact stage, $t_{c-SAAC}^{s-1} = 0.3$ (s) and $t_{c-AAC}^{s-1} = 0.9$ (s), which means that the SAAC is in contact with the environment faster than AAC. At the same time, in the force response stage, $t_{s-SAAC}^{s-1} = 2.2$ (s) and $t_{s-AAC}^{s-1} = 3.3$ (s), which means that the SAAC reaches steady-state faster than AAC. Similarly, in a structured environment with constant stiffness, both of our designed force controllers ensure high tracking accuracy at steady state.

Comparing Fig. 8(a) with Fig. 8(b), it shows that when the environmental stiffness k_e is increased from 1000 (N/m) to 2000 (N/m), the contact time t_c^{s-2} of SAAC and AAC remains equal to the previous working condition, but the setting time t_s^{s-2} is accelerated for both, and $t_{s-SAAC}^{s-2} = 1.7$ (s), $t_{s-AAC}^{s-2} = 2.6$ (s), which is due to the actual environmental stiffness k_e does not affect the robot motion process in free

Table I. Main simulation parameters.

Parameters	Values	Parameters	Values
m	5 (kg)	α	1
b	600 (Ns/m)	β	1
k	1000 (N/m)	k_p	3
$\hat{k}_e(0)$	1500 (N/m)	k_d	0.1
$\hat{x}_e(0)$	-0.25 (m)	x_e	-0.27 (m)

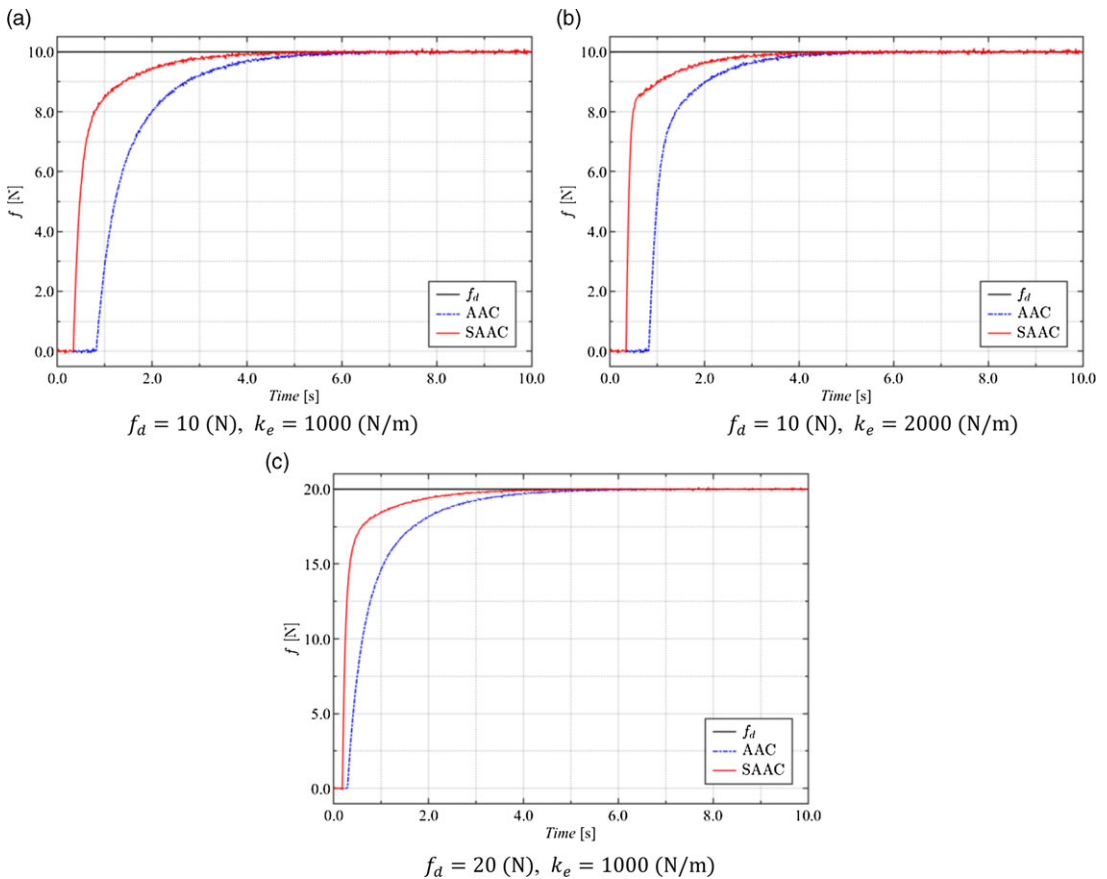


Figure 8. Comparison of force control performance of robots in structured interaction environments.

space but affects the process of generating reference trajectory in contact space, also the same tracking accuracy is maintained at steady state.

Similarly, comparing Fig. 8(a) and Fig. 8(c), it shows that when the environmental stiffness $k_e = 1000$ (N/m) is kept invariant, and the desired tracking force f_d is 10 and 20 (N), respectively. It can be seen that the contact time t_c^{s-3} and setting time t_s^{s-3} of SAAC and AAC are shortened. This is because the response speed of the robot to generate the reference trajectory in the free space and the contact space will be accelerated with the increase of the desired tracking force f_d , and the same tracking accuracy will be maintained in the steady state.

Figure 9 shows the force control performance of the robot while keeping the desired tracking force $f_d = 20$ (N), and the interaction environmental stiffness is varied with $k_e = 1000 + 50 \sin(\pi/4)$ (N/m).

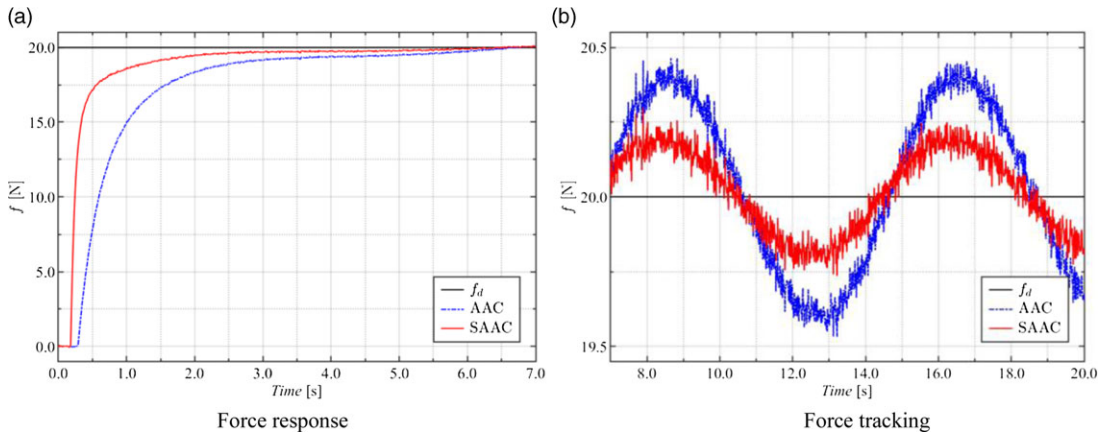


Figure 9. Comparison of force control performance of robots in a dynamic interactive environment.

It reveals that SAAC still maintains lower steady-state error e_f^{s-4} compared to AAC within the steady-state tracking phase of 10–20 (s), and $e_{f-SAAC}^{s-4} = 0.2$ (N), $e_{f-AAC}^{s-4} = 0.5$ (N). The reason why is that the introduction of the pre-PD controller enhances the robustness of the algorithm against environmental uncertainty, which can improve the steady-state tracking accuracy. Therefore, the previous research on theoretical derivation was also verified to be correct. The MSE (mean squared error) analysis of the steady-state tracking error between SAAC and AAC over 10-20 (s) is shown in Eq. (58).

$$\begin{cases} \text{MSE}_{SAAC}^s = 0.0174 \\ \text{MSE}_{AAC}^s = 0.0721 \end{cases} \quad (58)$$

Quantification from the MSE perspective indicates that the force tracking accuracy of SAAC enhanced by more than 75% than that of AAC. Therefore, it maintains better force tracking performance even in uncertain environments.

In summary, simulation results show that both the AAC and SAAC proposed in this article can guarantee high force tracking accuracy when the robot interacts with the unknown environment. However, the transient response rate of SAAC is higher than that of AAC for different environmental stiffnesses and different desired tracking forces. In the structured environment, both SAAC and AAC can maintain high accuracy in the steady-state tracking phase. However, in an unstructured environment or in the presence of nonlinear perturbations, SAAC is more robust, thus ensuring higher steady-state force tracking accuracy. Therefore, SAAC is more appropriate for applications involving contact force interaction.

5. Experimental verification

5.1. Experimental setup

To verify the actual performance of the proposed SAAC and AAC, an experimental environment based on the 6-Axis AUBO-i5 robot is built, as shown in Fig. 10. The interaction environment consists of a triangular stainless-steel plate with three sets of springs, and bearings are installed inside the slots so that the triangular stainless-steel plate can slide smoothly and freely on the rod when the robot presses downward during the force control task or lifts upward after completing the task.

The hardware architecture of the robot control system is shown in Fig. 11. The experimental hardware includes the AUBO-i5 robot, robot control cabinet, 6-Axis force sensor, unknown interactive environment, and upper computer. The robot control cabinet is based on the PREEMPT-Linux system to build the robot’s real-time controller. The main operating system of the upper computer is Windows, and the

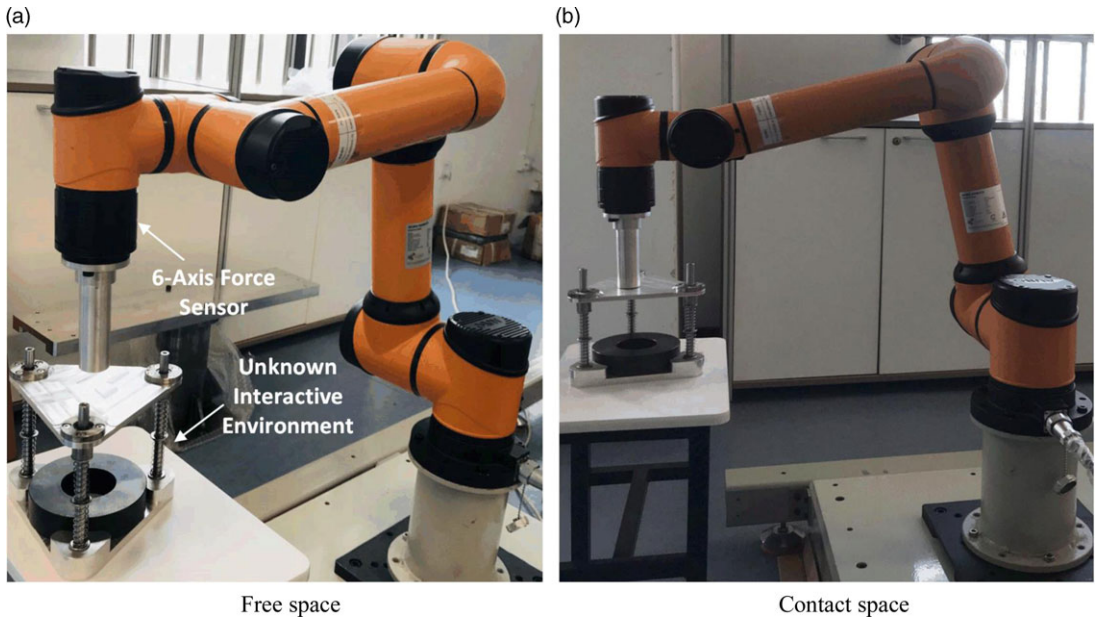


Figure 10. Experiment setup. The vertical direction is force control.

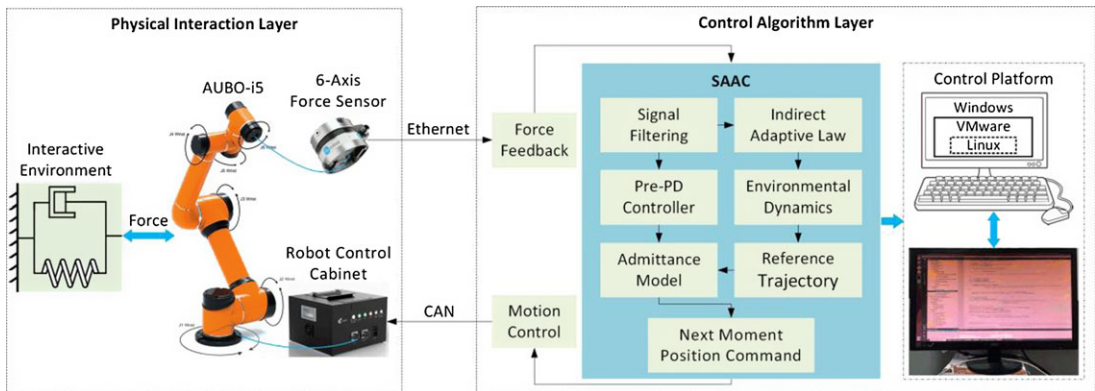


Figure 11. Hardware architecture of the 6-D of robot control system.

Linux system is built by VMware. The robot control program is written in the Linux-based Qt development environment of the upper computer, and the communication between the upper computer and the robot control cabinet is established through the Linux SSH service, which in turn allows the robot control cabinet to control the robot moves through the CAN bus. At the same time, the 6-Axis force sensor at the end of the robot provides real-time force feedback via Ethernet protocol, and the upper computer receives the feedback force signal for smooth adaptive admittance control algorithm updates. The control period is 200 (HZ).

5.2. Experimental parameters setting

The specific experimental parameters are set as shown in Table II. It should be emphasized that all parameter selection criteria are reference benchmarks, and the same experimental environment and parameters are used for all control algorithms.

Table II. Main experimental parameters.

Parameters	Values	Parameters	Values
m	5 (kg)	α	1
b	600 (Ns/m)	β	1
k	1500 (N/m)	k_p	5
$\hat{k}_e(0)$	2000 (N/m)	k_d	0.2
$\hat{x}_e(0)$	0 (m)	x_e	-0.27 (m)

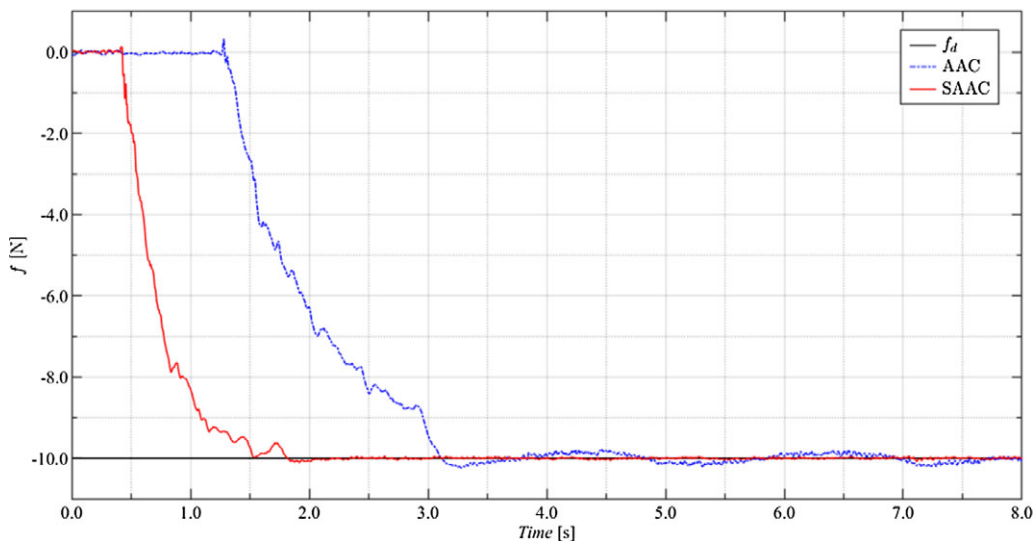


Figure 12. Comparison of transient response performance of AAC and SAAC. SAAC has a faster response rate than AAC.

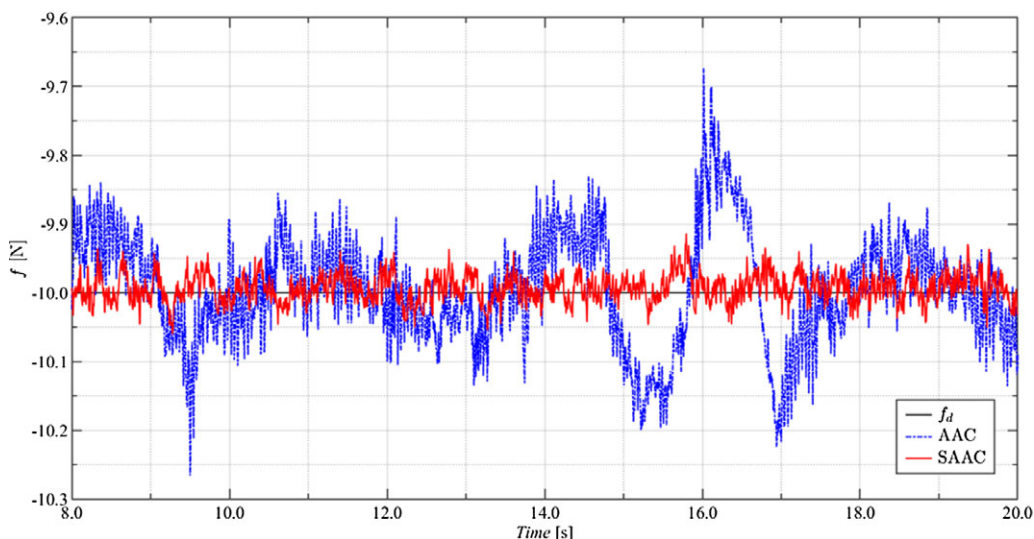


Figure 13. Comparison of steady-state tracking performance of SAAC and AAC. SAAC has higher robustness than AAC.

Table III. Comparison of simulation and experiment for MSE results.

	Simulation	Experimentation
AAC	0.0721	0.0054
SAAC	0.0174	$7.3799e^{-4}$

5.3. Experimental results

In this experiment, the motion process of the robot is divided into three phases: free motion, transient contact (collision), and steady-state tracking. Figure 12 shows the transient response performance of the adaptive admittance control (AAC) based on an indirect adaptive update strategy compared with the smooth adaptive admittance control (SAAC) based on the pre-PD and indirect adaptive update strategy. Under the condition that the robot starts moving from an initial equal height in free space, SAAC contacts the physical environment faster than AAC, and $t_{c-SAAC}^e = 0.5$ (s), $t_{c-AAC}^e = 1.3$ (s). Meanwhile, setting time of SAAC is also smaller than that of AAC, and $t_{s-SAAC}^e = 0.9$ (s), $t_{s-AAC}^e = 1.8$ (s). The reason for this is that the introduction of the outer-loop pre-PD controller speeds up the response of the overall system.

The performance comparison of the steady-state tracking phase is shown in Fig. 13. The ability of the robot to initially track the desired force and maintain force tracking performance under various external disturbances (Time lag of the position controller and unknown external nonlinear disturbances) is called the steady-state performance of the force-controlled robot. In AAC, the force error $e_{f-AAC}^e = 0.3$ (N) and the force curve fluctuates widely. In this case, the system is not very robust. In SAAC, the force error $e_{f-SAAC}^e = 0.05$ (N) and the force curve is smoother. Thus, a system with SAAC is more robust to external disturbances than that with AAC. It can be seen that SAAC can significantly improve the force control performance, and the contact force tracking error is greatly reduced.

For more intuitive and quantitative description of the effectiveness of the proposed algorithm, the steady-state tracking errors of different force controllers in the experiment from 8 to 20 (s) were characterized using MSE and compared with the MSE results of the simulation, as shown in Table III. In the experiment, SAAC improves the steady-state tracking accuracy by nearly an order of magnitude over AAC. On the other hand, both AAC and SAAC in the experiment are higher than the simulation in terms of tracking accuracy, which is due to the stronger noise and more uncertainty of the environmental dynamics model that we introduced in the simulation to highlight the effectiveness of the proposed algorithm. In general, SAAC has higher steady-state tracking accuracy and stronger robustness for unknown interaction environments compared to AAC due to the introduction of the pre-PD controller.

Both force control schemes, AAC and SAAC, are proposed for the disadvantages that the existing admittance control method cannot guarantee the steady-state tracking accuracy and robustness when the robot interacts with the unknown environment. From the experimental results, it can be seen that SAAC has faster system response and stronger robustness. Therefore, SAAC is a better control scheme for robots handling contact operation tasks in unknown environments to ensure high-accuracy force tracking at steady state while improving transient response performance. The experimental results show the superiority of this controller and also corroborate with the previous theoretical derivation.

6. Conclusion

As collaborative robots have been developed in recent years, robot contact interaction operations have become increasingly more important. Ensuring fast, stable, and smooth force interactions was a challenge for most robot controller designs. In this research, a SAAC has been proposed to deal with the problems of parameter convergence rate and steady-state tracking accuracy in unknown environments. An indirect adaptive update strategy has been designed to generate the reference trajectory of the admittance model. The necessity of the introduction of the pre-PD controller to enhance the robustness of the system against environmental uncertainties and unknown external disturbances is analyzed. Meanwhile,

the designed control strategy is task-oriented, and the adaptive rate dynamically updates the robot's reference trajectory in real time according to different interaction tasks to ensure optimal force control performance. Simulations and experiments verify that the SAAC can significantly improve the force control performance of the robot in unknown environments. Furthermore, the proposed method can be easily extended to other force control tasks, including deformation-prone machining environments in industrial applications or manufacturing tasks that require robot-based force control.

Author contributions. Chengguo Liu conceived and proposed this study, while performing the simulation analysis. Zeyu Li built the experimental platform and conducted the verification.

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Conflicts of interest. The authors declare none.

Ethical approval. Not applicable.

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