

RESEARCH ARTICLE

Generation mechanism of 100 MG magnetic fields in the interaction of ultra-intense laser pulse with nanostructured target

J. M. Tian¹, H. B. Cai^{2,3}, W. S. Zhang², E. H. Zhang¹, B. Du², and S. P. Zhu²

¹Graduate School, China Academy of Engineering Physics, Beijing 100088, China

²Institute of Applied Physics and Computational Mathematics, Beijing 100094, China

³Center for Applied Physics and Technology, HEDPS, and College of Engineering, Peking University, Beijing 100871, China

(Received 17 December 2019; revised 14 March 2020; accepted 26 March 2020)

Abstract

Experimental and simulation data [Moreau *et al.*, Plasma Phys. Control. Fusion **62**, 014013 (2019); Kaymak *et al.*, Phys. Rev. Lett. **117**, 035004 (2016)] indicate that self-generated magnetic fields play an important role in enhancing the flux and energy of relativistic electrons accelerated by ultra-intense laser pulse irradiation with nanostructured arrays. A fully relativistic analytical model for the generation of the magnetic field based on electron magneto-hydrodynamic description is presented here. The analytical model shows that this self-generated magnetic field originates in the nonparallel density gradient and fast electron current at the interfaces of a nanolayered target. A general formula for the self-generated magnetic field is found, which closely agrees with the simulation scaling over the relevant intensity range. The result is beneficial to the experimental designs for the interaction of the laser pulse with the nanostructured arrays to improve laser-to-electron energy coupling and the quality of forward hot electrons.

Keywords: nanolayered target; self-generated magnetic field; ultra-intense laser pulse

1. Introduction

The interaction of relativistically intense laser pulses with solid targets has stimulated considerable interest because of its practical applications in laser-driven particle acceleration^[1–7], high-brightness ultrafast hard X-ray and K_α source^[8–11], cancer treatment^[12, 13], fast ignition in inertial confinement fusion^[14], etc. A crucial issue, in all these applications, is to produce high-quality forward hot electrons efficiently. Some experimental and simulation results^[15–25] indicate that the interaction of the intense laser pulse with the subwavelength nanowire targets can significantly increase laser energy absorption and enhance the flux and energy of relativistic electrons compared to flat targets. In addition, nanowire arrays can greatly affect the transport of the fast electrons and the generation of mega-ampere relativistic electron beams^[17, 26, 27]. There are also strong magnetic fields (about 100 MG) produced within the nanowire arrays^[20, 27]. It is worth noting that the self-

generated magnetic field plays an important role in both the production and the transport of the fast electrons. However, the mechanism of the generation of the magnetic field in nanostructured arrays has not yet been studied in detail.

In this paper, we consider an ultra-intense laser pulse normally irradiating on a fully ionized nanolayered target. The schematic diagram of the electron density for the nanolayered target (partial) is shown in Figure 1. Since the averaged electron density of the nanolayered target is much larger than the critical density n_c , the interaction of the laser pulse with the nanolayered target mainly occurs near the front surface of the target. Here, $n_c = m_e \epsilon_0 \omega_0^2 / e^2$ is the critical density; m_e , $-e$, ϵ_0 and ω_0 represent the electron mass, electron charge, dielectric constant in vacuum and laser angular frequency, respectively. During the interaction of the laser pulse with the nanolayered target, a large number of energetic electrons are accelerated by the laser pulse, resulting in the formation of a relativistic electron beam. At relativistic intensities, 10^{18} – 10^{22} W/cm², most of the laser energy is transported by relativistic electrons, which are collisionless. Charge neutrality requires that a flux of relativistic electron beam into the target must be balanced

Correspondence to: H. B. Cai and S. P. Zhu, No. 2 Fenghao East Road, Haidian District, Beijing 100094, China. Email: Cai_hongbo@iapcm.ac.cn (H. B. Cai), Zhu_shaoping@iapcm.ac.cn (S. P. Zhu)

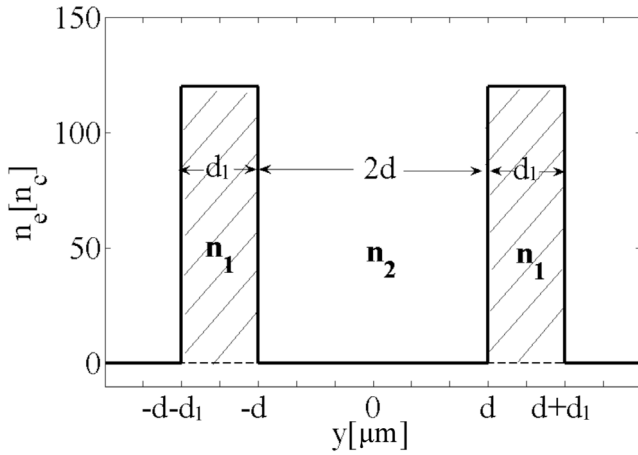


Figure 1. Schematic diagram of the initial electron density for the partial nanolayered target.

by a return current of thermal electrons. Note that the returned thermal electrons are reflected by the sheath field at the interface of the nanolayered target while the relativistic electrons can spread inside the target with a divergence angle, resulting in a net current along the surface of the nanolayered structure. Thus, quasi-static magnetic fields of the order of 100 MG can be produced inside the gaps between the nanolayers.

2. Generation mechanism of the magnetic field

If the laser spot size is large enough, we can simply assume that an equally infinite and uniform fast electron beam with electron density n_h and averaged velocity v_h propagates along the x -axis. The neutralizing electron current also flows in the x -direction with averaged velocity v_{e0} . Since magnetic fields can develop in a very short time, the combined system of the fast electron beam and the response of the background plasma can be suitably treated by a single-fluid electron magneto-hydrodynamic (EMHD) description, which contains electron-fluid equations and Maxwell equations. The electron-fluid equations consist of the continuity equation and the force balance equation. From it, we can obtain the relationship between the self-generated magnetic field and the electron flow velocity as^[28, 29]

$$\mathbf{B} = \frac{c}{e} \nabla \times \mathbf{p}_e, \quad (1)$$

where $\mathbf{p}_e = m_e \gamma_e \mathbf{v}_{e0}$ is the momentum of the background electrons, γ_e is the relativistic factor, $-e$ is the electron charge and c is the speed of light. Besides, the self-generated electromagnetic fields in the nanolayered target satisfy the Maxwell equations

$$\nabla \times \mathbf{B} = \frac{4\pi}{c} (-en_e \mathbf{p}_e / m_e \gamma_e + \mathbf{j}_h) + \frac{1}{c} \frac{\partial \mathbf{E}}{\partial t}, \quad (2)$$

where \mathbf{j}_h is the current density of the fast electron beam and n_e is the background electron density. Here, for a long beam with pulse length $l_b \gg v_h / \omega_p$, where v_h and ω_p are the fast electron beam velocity and background plasma frequency, the displacement current $(1/c)(\partial \mathbf{E} / \partial t)$ is of order $(v_h / \omega_p l_b) \ll 1$ compared to the electron current. So, the displacement current can be neglected. Equation (2) can be rewritten as

$$\mathbf{p}_e = -\frac{m_e c \gamma_e}{4\pi e n_e} \nabla \times \mathbf{B} + \frac{m_e \gamma_e}{e} \frac{\mathbf{j}_h}{n_e}. \quad (3)$$

Substituting Equation (3) into Equation (1), we can obtain

$$\mathbf{B} = \frac{m_e c}{e^2} \left(\frac{1}{n_e} \nabla \times \mathbf{j}_h - \frac{1}{n_e^2} \nabla n_e \times \mathbf{j}_h \right) - \nabla \times (\delta_{pe}^2 \nabla \times \mathbf{B}), \quad (4)$$

where $\delta_{pe} = c / \omega_{pe}$ is the electron skin depth and $\omega_{pe} = (4\pi n_e e^2 / m_e)^{1/2}$ is the electron plasma frequency. The three terms of the right-hand side of Equation (4) are the source of the self-generated magnetic field. The first term generates a magnetic field that pushes the fast electrons toward regions of higher fast electron current density, and the second term pushes the fast electrons toward regions of lower density. The third term represents the interaction of the self-generated magnetic field with the plasmas of the nanolayered target. From Equation (4), it is obvious that a sharp electron density gradient and a strong fast electron current are necessary to generate a strong magnetic field. For the nanolayered target, in order to keep the charge neutrality, the return electrons must exist inside the nanolayers. Due to the strong self-generated magnetic field, most of the fast electrons and return electrons are bounded near the edges of the nanolayers.

To further understand the characteristics of the self-generated magnetic fields, we take a part of the nanolayered target as an example to analyze the generation of the magnetic field when the laser pulse interacts with the nanolayered target. As shown in Figure 1, three regions are divided as follows: region 1 with $-d_1 - d < y < -d$ and the region 3 with $d < y < d + d_1$ are the high-density plasma for the nanolayers and region 2 with $-d < y < d$ is the gap between the nanolayers. In order to solve Equation (4), a one-dimensional model is adopted to quantitatively estimate the self-generated magnetic field. In other words, only the spatial variations in the y -direction are considered. Then, Equation (4) can be rewritten as

$$\begin{cases} -\delta_{pe1}^2 \frac{\partial^2}{\partial y^2} \mathbf{B} + \mathbf{B} = 0, & -d - d_1 < y < -d, \\ -\delta_{pe2}^2 \frac{\partial^2}{\partial y^2} \mathbf{B} + \mathbf{B} = 0, & -d < y < d, \\ -\delta_{pe1}^2 \frac{\partial^2}{\partial y^2} \mathbf{B} + \mathbf{B} = 0, & d < y < d + d_1, \end{cases} \quad (5)$$

where d_1 is the width of the nanolayer, $\delta_{pei} = c/\omega_{pei}$ is the electron skin depth and $\omega_{pei} = (4\pi n_i e^2/m_e)^{1/2}$ is the electron plasma frequency for the i th region ($i = 1, 2$). Here, the electron density n_2 and the fast electron current density j_h are assumed as constants. From Equation (5), the self-generated magnetic field can be solved analytically as follows:

$$\mathbf{B} = \begin{cases} c_1 \exp\left(\frac{y}{\delta_{pe1}}\right) + c_2 \exp\left(\frac{-y}{\delta_{pe1}}\right), & -d - d_1 < y < -d, \\ c_3 \exp\left(\frac{y}{\delta_{pe2}}\right) + c_4 \exp\left(\frac{-y}{\delta_{pe2}}\right), & -d < y < d, \\ c_5 \exp\left(\frac{y}{\delta_{pe1}}\right) + c_6 \exp\left(\frac{-y}{\delta_{pe1}}\right), & d < y < d + d_1. \end{cases} \quad (6)$$

The constants c_1, c_2, c_3, c_4, c_5 and c_6 can be solved by the boundary conditions

$$\left\{ \begin{aligned} c_1 &= \frac{\mathbf{B}_0 \exp\left(\frac{d_1}{\delta_{pe1}}\right) - \mathbf{B}_1}{\exp\left(\frac{-d + d_1}{\delta_{pe1}}\right) - \exp\left(\frac{-d - d_1}{\delta_{pe1}}\right)}, \\ c_2 &= \frac{\mathbf{B}_1 - \mathbf{B}_0 \exp\left(\frac{-d_1}{\delta_{pe1}}\right)}{\exp\left(\frac{d + d_1}{\delta_{pe1}}\right) - \exp\left(\frac{d - d_1}{\delta_{pe1}}\right)}, \\ c_3 &= \frac{-\mathbf{B}_0 \exp\left(-\frac{d}{\delta_{pe2}}\right) + \mathbf{B}_1 \exp\left(\frac{d}{\delta_{pe2}}\right)}{\exp\left(\frac{2d}{\delta_{pe2}}\right) - \exp\left(-\frac{2d}{\delta_{pe2}}\right)}, \\ c_4 &= \frac{\mathbf{B}_0 \exp\left(\frac{d}{\delta_{pe2}}\right) - \mathbf{B}_1 \exp\left(-\frac{d}{\delta_{pe2}}\right)}{\exp\left(\frac{2d}{\delta_{pe2}}\right) - \exp\left(-\frac{2d}{\delta_{pe2}}\right)}, \\ c_5 &= \frac{\mathbf{B}_0 - \mathbf{B}_1 \exp\left(\frac{-d_1}{\delta_{pe1}}\right)}{\exp\left(\frac{d + d_1}{\delta_{pe1}}\right) - \exp\left(\frac{d - d_1}{\delta_{pe1}}\right)}, \\ c_6 &= \frac{\mathbf{B}_1 \exp\left(\frac{d_1}{\delta_{pe1}}\right) - \mathbf{B}_0}{\exp\left(\frac{-d + d_1}{\delta_{pe1}}\right) - \exp\left(\frac{-d - d_1}{\delta_{pe1}}\right)}, \end{aligned} \right. \quad (7)$$

where \mathbf{B}_0 and \mathbf{B}_1 are the maximum magnetic fields at the nanolayer interfaces ($y = -d$ and $y = d$). Note that $n_1 \gg n_2, d_1 \gg \delta_{pe1}$ and $d \gg \delta_{pe2}$ in the nanolayered target. In order to get the values of \mathbf{B}_0 and \mathbf{B}_1 , we integrate Equation (4) across the interfaces of $y = -d$ and $y = d$. Then, we can obtain the integrated magnetic flux^[30, 31]

$$\begin{cases} \Phi_0 = (\delta_{pe1} + \delta_{pe2})\mathbf{B}_0 = \frac{m_e c}{e^2} \left(\frac{\mathbf{j}_{h2}}{n_2} - \frac{\mathbf{j}_{h1}}{n_1} \right), \\ \Phi_1 = (\delta_{pe1} + \delta_{pe2})\mathbf{B}_1 = \frac{m_e c}{e^2} \left(\frac{\mathbf{j}_{h3}}{n_1} - \frac{\mathbf{j}_{h2}}{n_2} \right), \end{cases} \quad (8)$$

where $\Phi_0 = \int_{-d-d_1/2}^0 \mathbf{B} dy, \Phi_1 = \int_0^{d+d_1/2} \mathbf{B} dy$ are the integrated magnetic fluxes and $\mathbf{j}_{hi} = en_{hi} v_{hi}$ ($i = 1, 2, 3$) are the electron current densities within different regions. Since the background electron density satisfies $n_1 \gg n_2$ and the fast electron current densities are assumed as $\mathbf{j}_h \simeq \mathbf{j}_{h1} \simeq \mathbf{j}_{h2} \simeq \mathbf{j}_{h3}$, the terms \mathbf{j}_{h1}/n_1 and \mathbf{j}_{h3}/n_3 can be neglected in Equation (8). Then, we can obtain

$$\begin{cases} \mathbf{B}_0 = \frac{m_e c}{e^2(\delta_{pe1} + \delta_{pe2})} \frac{\mathbf{j}_h}{n_2}, \\ \mathbf{B}_1 = -\frac{m_e c}{e^2(\delta_{pe1} + \delta_{pe2})} \frac{\mathbf{j}_h}{n_2}. \end{cases} \quad (9)$$

If we simply assume that the absorbed laser energy flux is approximately equal to the electron energy flux $\zeta I_{18} = 0.02 f n_h T_{keV}^{3/2}$ [32], where the electron temperature is expressed by the ‘Beg law’^[33] with $T_{keV} = 200 I_{18}^{1/3}, n_h = \zeta I_{18}/(0.02 f T_{keV}^{3/2})$ is the density of energy carrying electrons in units of 10^{23} cm^{-3} , ζ is the fraction of laser energy absorbed by the fast electrons and f is the flux limiting factor. Here, the ratio of ζ to f is approximated as $\zeta/f = 0.39$. Thus, the maximum value for the magnetic field can be written as

$$B_{max} = 188 \frac{\zeta}{f} \frac{I_{18}^{1/2}}{\left(1/\sqrt{\frac{n_1}{n_c}} + 1/\sqrt{\frac{n_2}{n_c}}\right) \frac{v_h}{n_c}} \text{ MG}, \quad (10)$$

where $v_h \simeq c$ is the fast electron velocity, n_1 is the electron density of the nanolayers, n_2 is the electron density in the gaps between the nanolayers, $n_c = m_e \epsilon_0 \omega_0^2/e^2$ is the critical density and $I_{18}^{1/2}$ is the normalized laser intensity.

Substituting Equation (7) into Equation (6) and combining Equation (9), we can obtain the complete expression of the self-generated magnetic field in the transverse direction. It can be found that the self-generated magnetic field is strongly dependent on the sharp gradient of the plasma density near the nanolayer interfaces ($y = \pm 0.3 \mu\text{m}$) and the current density of the fast electrons. Figure 2(a) shows the magnetic field generated in the nanolayered target with different electron densities $n_2 = 2n_c, 4n_c, 10n_c$ (in the nanolayered gap). The initial plasma density of the nanolayers is $n_1 = 120n_c$ and the current density of the fast electron is assumed as $j_h = 3n_c e c$. The width of the nanolayers is $d_1 = 0.2 \mu\text{m}$ and the width of the gap between the nanolayers is $2d = 0.6 \mu\text{m}$. It can be clearly seen that the maximum value of the self-generated magnetic

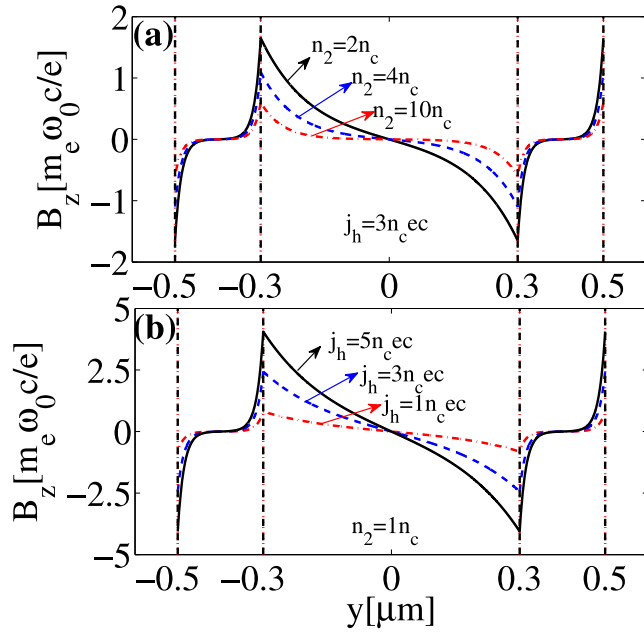


Figure 2. The magnetic field generated in the nanolayered target (a) with different electron density of $n_2 = 2n_c, 4n_c, 10n_c$ and (b) with different fast electron current density of $j_h = 1n_c ec, 3n_c ec, 5n_c ec$. The initial plasma density of the nanolayers is $120n_c$. The other parameters are $d_1 = 0.2 \mu\text{m}$ and $d = 0.3 \mu\text{m}$. The unit of the magnetic field here is $m_e \omega_0 c/e \approx 100 \text{ MG}$.

field is present near the nanolayer interfaces $y = \pm 0.3 \mu\text{m}$ with the values of B_0 and B_1 . The intensity of the self-generated magnetic field decreases as the nanolayered gap plasma density (n_2) increases due to the decrease of the plasma density gradient near the nanolayer interface. It is clear that the magnetic field exists within the skin depth δ_{pe} , so the magnetic field decays rapidly to zero in the nanolayer region. And due to the lower electron density in the nanolayered gap, the magnetic field decays much slower than that in the nanolayer region. Figure 2(b) shows the magnetic fields generated in the nanolayered target with different fast electron current densities of $j_h = 1n_c ec, 3n_c ec, 5n_c ec$. The electron density in the nanolayered gap is $1n_c$. The other parameters are similar to those in Figure 2(a). We found that with the same plasma density gradient near the nanolayer interfaces ($y = \pm 0.3 \mu\text{m}$), the maximum intensity of the self-generated magnetic field increases as the fast electron current density (j_h) increases. The physical reason is clear that the higher fast electron current density could induce higher return current density, which in turn makes the self-generated magnetic field much stronger. In addition, the theoretical analysis does not consider the detailed interaction process between the laser pulse with the nanolayered target. So, in the theoretical analysis, the width of the nanolayered gap does not affect the maximum intensity of the self-generated magnetic field but only affects the distribution of the self-generated magnetic field.

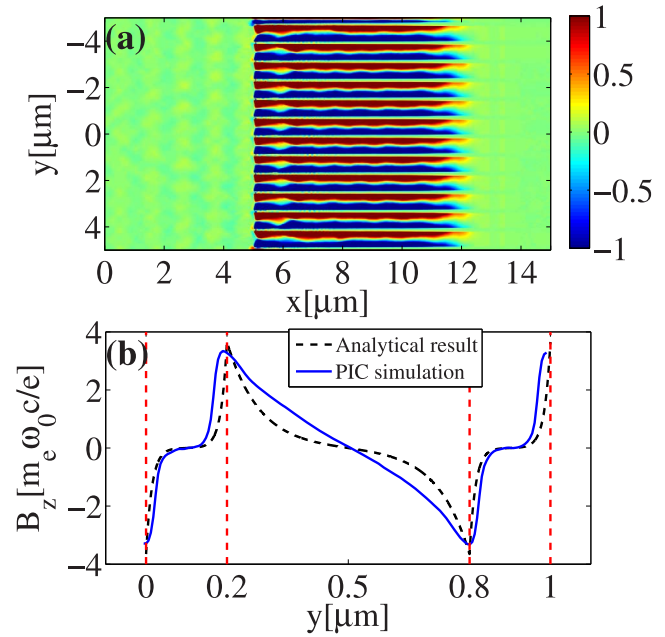


Figure 3. (a) The distribution of the magnetostatic field B_z at time 46.7 fs. (b) The transverse distributions of self-generated magnetic fields at $x = 8 \mu\text{m}$ and $y = (0, 1) \mu\text{m}$ are plotted. The blue solid curve is for the simulation result and the black dot curve is for the analytical result.

3. Numerical simulation

In the following, the generation of magnetic fields is studied in further detail by the two-dimensional (2D) particle-in-cell (PIC) simulations, which are performed using the simulation code EPOCH^[34]. In simulations, we take p-polarized laser pulses with normalized intensity of $a_0 = 6.0$, which are incident along the x -direction. The wavelength and duration of the laser pulse are $\lambda_0 = 1 \mu\text{m}$ and $\tau = 330 \text{ fs}$, respectively. The laser spot is large enough so that the transverse intensity of the laser pulse is uniform. The simulation box is $15 \mu\text{m} \times 10 \mu\text{m}$ with a resolution of 170 cells per λ in the longitudinal and transverse directions. The nanolayered target is located from $5 \mu\text{m}$ to $15 \mu\text{m}$, and the electron density of the nanowires is $120n_c$. The gaps between the nanolayers are empty at the initial time. Similar to the structure in Figure 1, the width of the nanolayers is $d_1 = 0.2 \mu\text{m}$ and the width of the nanolayered gap is $2d = 0.6 \mu\text{m}$.

During the interaction of the laser pulse with the nanolayered target, most of the laser energy is absorbed by the nanolayered target. And a large number of energetic electrons can be accelerated by the laser pulse. The simulation results indicate that the peak of the laser energy absorption can reach as high as 80%. The temperature of the fast electrons calculated from the electron spectrum is about 0.81 MeV, which is well consistent with the calculated value $T_e = 0.79 \text{ MeV}$ by the Beg law.

Figure 3(a) shows the magnetic fields produced by the interaction of a laser pulse with the nanolayered target at

time 46.7 fs. In Fig. 3(a), it can be clearly seen that the strong periodic positive and negative quasi-static magnetic fields are generated near the nanolayer interfaces. In this case, the maximum value of the magnetic field can reach 300 MG. Figure 3(b) shows the transverse distribution of self-generated magnetic fields at $x = 8 \mu\text{m}$. The blue solid curve is for the simulation result and the black dot curve is for the analytical result. To obtain the analytical result, we have to count the current density j_h and electron density n_2 from the PIC simulation results. The current density $j_h = -3.3n_c e c$ is counted as the averaged current density of the forward fast electrons at the position $x = 8 \mu\text{m}$ and the transverse range of $y = (0, 1) \mu\text{m}$. The electron density of the nanolayered gap $n_2 = 0.7n_c$ is counted as the averaged background electron density at the position $x = 8 \mu\text{m}$ and the transverse range of $y = (0.2, 0.8) \mu\text{m}$. The velocity of the fast electrons is approximately assumed as $v_h \simeq c$. Then the transverse distribution of self-generated magnetic fields can be obtained by using Equation (6). We can see that the simulation result is well consistent with the analysis result. The slight difference of the self-generated magnetic field between the analytical result and the PIC simulation is only at the position of the nanolayered gap. Here, the distribution of the self-generated magnetic field is affected by the distribution of electron density in the nanolayered gap. In the analytical model, the distribution of electron density of the nanolayered gap is counted as a uniform value. But, in PIC simulation results, the distribution of the electron density near the nanolayers could be higher than that away from the nanolayers. So the slight difference of the self-generated magnetic field in the nanolayered gap is mainly caused by the nonuniform electron density.

In the theoretical analysis, the current density of the fast electron beam could affect the intensity of the self-generated magnetic field. So, we can change the intensity of the laser pulse to affect the current density of the fast electron beam and thus the intensity of the self-generated magnetic field. In Figure 4, we plot the maximum intensity of the self-generated magnetic field versus the normalized intensity of the laser pulse. The blue dashed line stands for the simulation results and the black solid line stands for the theoretical analysis results by using Equation (10). In the analytical model, the velocity of the fast electrons is approximately assumed as $v_h \simeq c$, and the electron density of the nanolayers is $n_1 = 120n_c$; the electron density of the nanolayered gap is approximately $n_2 = 1n_c$, and the ratio of ζ to f is approximated as $\zeta/f = 0.39$. In simulations, except for the laser intensity, the other laser and plasma parameters are the same as in Figure 3(a). In Figure 4, it can be seen that the simulation results and the analytical results are basically consistent.

4. Summary

In summary, we have established accurate results for the generation of magnetic fields in a laser irradiated nanolayered

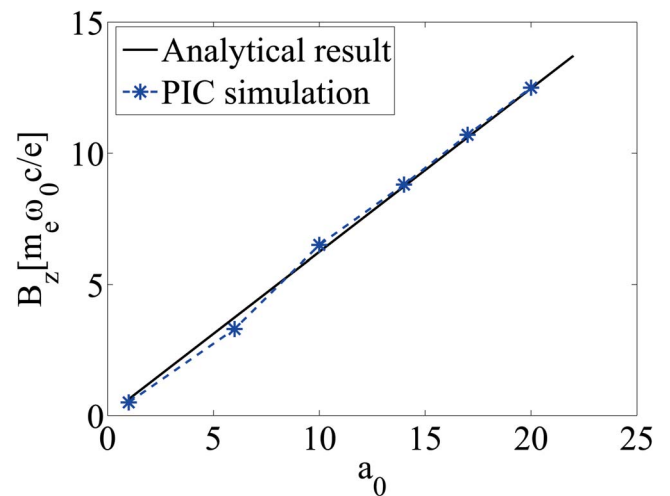


Figure 4. The maximum intensity of the self-generated magnetic field versus the normalized intensity of the laser pulse. The unit of the magnetic field here is $m_e \omega_0 c / e \approx 100 \text{ MG}$. The blue dashed line stands for the simulation results and the black solid line stands for the theoretical analysis result.

target based on the EMHD approximation. The resultant structure and amplitude of the magnetic field inside the nanolayered target are determined for a given laser intensity and plasma density. It reveals that the characteristics of the self-generated magnetic field are strongly dependent on the density gradient of the nanostructured arrays and the fast electron current. The 2D-PIC simulation results are in good agreement with the theoretical analysis. When designing the relevant experiments of the interaction of ultra-intense laser pulse with a nanowire target, our work can better predict the structure and the intensity of the self-generated magnetic field inside the nanowire target, which is beneficial to improving the quality of the energetic electrons and ions accelerated by the laser pulse in the nanowire target.

Acknowledgements

This work was supported by the Science Challenge Project (No. TZ2016005), NSAF (No. U1730449), the National Natural Science Foundation of China (Nos. 11575030 and 11975055) and the National Key Programme for S&T Research and Development in China (No. 2016YFA0401100). The authors are grateful for the fruitful discussions with X. X. Yan and P. L. Yao.

References

1. J. Faure, C. Rechatin, A. Norlin, A. Lifschitz, Y. Glinec, and V. Malka, *Nature* **444**, 737 (2006).
2. A. Macchi, M. Borghesi, and M. Passoni, *Rev. Mod. Phys.* **85**, 751 (2013).

3. F. Wagner, C. Brabetz, O. Deppert, M. Roth, T. Stohlker, An. Tauschwitz, A. Tebartz, B. Zielbauer, and V. Bagnoud, *High Power Laser Sci. Eng.* **4**, e45 (2016).
4. S. Kawata, T. Nagashima, M. Takano, T. Izumiyama, D. Kamiyama, D. Barada, Q. Kong, Y. J. Gu, P. X. Wang, Y. Y. Ma, W. M. Wang, W. Zhang, J. Xie, H. R. Zhang, and D. B. Dai, *High Power Laser Sci. Eng.* **2**, e4 (2014).
5. J. Schreiber, F. Bell, and Z. Najmudin, *High Power Laser Sci. Eng.* **2**, e41 (2014).
6. D. Khaghani, M. Lobet, B. Borm, L. Burr, F. Gartner, L. Gremillet, L. Movsesyan, O. Rosmej, M. E. Toimil-Molares, F. Wagner, and P. Neumayer, *Sci. Rep.* **7**, 11366 (2017).
7. M. Dozires, G. M. Petrov, P. Forestier-Colleoni, P. Campbell, K. Krushelnick, A. Maksimchuk, C. McGuffey, V. Kaymak, A. Pukhov, M. G. Capeluto, R. Hollinger, V. N. Shlyaptsev, J. J. Rocca, and F. N. Beg, *Plasma Phys. Control. Fusion* **61**, 065016 (2019).
8. A. Rousse, C. Rischel, and J.-C. Gauthier, *Rev. Mod. Phys.* **73**, 17 (2001).
9. A. Pukhov, *Nat. Phys.* **2**, 439 (2006).
10. L. M. Chen, F. Liu, W. M. Wang, M. Kando, J. Y. Mao, L. Zhang, J. L. Ma, Y. T. Li, S. V. Bulanov, T. Tajima, Y. Kato, Z. M. Sheng, Z. Y. Wei, and J. Zhang, *Phys. Rev. Lett.* **104**, 215004 (2010).
11. E. Brambrink, S. Baton, M. Koenig, R. Yurchak, N. Bidaut, B. Albertazzi, J. E. Cross, G. Gregori, A. Rigby, E. Falize, A. Pelka, F. Kroll, S. Pikuz, Y. Sakawa, N. Ozaki, C. Kuranz, M. Manuel, C. Li, P. Tzeferacos, and D. Lamb, *High Power Laser Sci. Eng.* **4**, e30 (2016).
12. V. Malka, S. Fritzler, E. Lefebvre, E. dHumieres, R. Ferrand, G. Grillon, C. Albaret, S. Meyroneinc, J.-P. Chambaret, A. Antonetti, and D. Hulin, *Med. Phys.* **31**, 1587 (2004).
13. D. Schardt, *Nucl. Phys. A* **787**, 633 (2007).
14. M. Tabak, J. Hammer, M. E. Glinsky, W. L. Kruer, S. C. Wilks, J. Woodworth, E. M. Campbell, M. D. Perry, and R. J. Mason, *Phys. Plasmas* **1**, 1626 (1994).
15. A. Moreau, R. Hollinger, C. Calvi, S. Wang, Y. Wang, M. G. Capeluto, A. Rockwood, A. Curtis, S. Kasdorf, V. N. Shlyaptsev, V. Kaymak, A. Pukhov, and J. J. Rocca, *Plasma Phys. Control. Fusion* **62**, 014013 (2020).
16. D. Sarkar, P. K. Singh, G. Cristoforetti, A. Adak, G. Chatterjee, M. Shaikh, A. D. Lad, and P. Londrillo, *Appl. Phys. Lett. Photonics* **2**, 066105 (2017).
17. A. Curtis, C. Calvi, J. Tinsley, R. Hollinger, V. Kaymak, A. Pukhov, S. J. Wang, A. Rockwood, Y. Wang, V. N. Shlyaptsev, and J. J. Rocca, *Nat. Commun.* **9**, 1077 (2018).
18. M. A. Purvis, V. N. Shlyaptsev, R. Hollinger, C. Bargsten, A. Pukhov, A. Prieto, Y. Wang, B. M. Luther, L. Yin, S. Wang, and J. J. Rocca, *Nat. Photonics* **7**, 796 (2013).
19. Z. Q. Zhao, L. H. Cao, L. F. Cao, J. Wang, W. Z. Huang, W. Jiang, Y. L. He, Y. C. Wu, B. Zhu, K. G. Dong, Y. K. Ding, B. H. Zhang, Y. Q. Gu, M. Y. Yu, and X. T. He, *Phys. Plasmas* **17**, 123108 (2010).
20. V. Kaymak, A. Pukhov, V. N. Shlyaptsev, and J. J. Rocca, *Phys. Rev. Lett.* **117**, 035004 (2016).
21. L. H. Cao, Y. Q. Gu, Z. Q. Zhao, L. F. Cao, W. Z. Huang, W. M. Zhou, H. B. Cai, X. T. He, W. Yu, and M. Y. Yu, *Phys. Plasmas* **17**, 103106 (2010).
22. L. H. Cao, Y. Q. Gu, Z. Q. Zhao, L. F. Cao, W. Z. Huang, W. M. Zhou, X. T. He, W. Yu, and M. Y. Yu, *Phys. Plasmas* **17**, 043103 (2010).
23. J. Q. Yu, W. M. Zhou, L. H. Cao, Z. Q. Zhao, L. F. Cao, L. Q. Shan, D. X. Liu, X. L. J, B. Li, and Y. Q. Gu, *Appl. Phys. Lett.* **100**, 204101 (2012).
24. L. L. Ji, S. Jiang, A. Pukhov, R. Freeman, and K. Akli, *High Power Laser Sci. Eng.* **5**, e14 (2017).
25. S. Jiang, L. L. Ji, H. Audesirk, K. M. George, J. Snyder, A. Krygier, P. Poole, C. Willis, R. Daskalova, E. Chowdhury, N. S. Lewis, D.W. Schumacher, A. Pukhov, R. R. Freeman, and K. U. Akli, *Phys. Rev. Lett.* **116**, 085002 (2016).
26. P. K. Singh, G. Chatterjee, A. D. Lad, A. Adak, S. Ahmed, M. Khorasaninejad, M. M. Adachi, K. S. Karim, S. S. Saini, A. K. Sood, and G. Ravindra Kumar, *Appl. Phys. Lett.* **100**, 244104 (2012).
27. G. Chatterjee, P. K. Singh, S. Ahmed, A. P. L. Robinson, A. D. Lad, S. Mondal, V. Narayanan, I. Srivastava, N. Koratkar, J. Pasley, A. K. Sood, and G. R. Kumar, *Phys. Rev. Lett.* **108**, 235005 (2012).
28. E. A. Startsev, R. C. Davidson, and M. Dorf, *Phys. Plasmas* **16**, 092101 (2009).
29. H. B. Cai, S. P. Zhu, M. Chen, S. Z. Wu, X. T. He, and K. Mima, *Phys. Rev. E* **83**, 036408 (2011).
30. A. R. Bell, J. R. Davies, and S. M. Guerin, *Phys. Rev. E* **58**, 2471 (1998).
31. W. S. Zhang, H. B. Cai, and S. P. Zhu, *Phys. Plasmas* **22**, 103109 (2015).
32. A. B. Bell, A. P. L. Robinson, M. Sherlock, R. J. Kingham, and W. Rozmus, *Plasma Phys. Control. Fusion* **48**, R37 (2006).
33. F. N. Beg, A. R. Bell, A. E. Dangor, C. N. Danson, A. P. Fews, M. E. Glinsky, B. A. Hamme, P. Lee, P. A. Norreys, and M. Tatarakis, *Phys. Plasmas* **4**, 447 (1997).
34. T. D. Arber, K. Bennett, C. S. Brady, A. Lawrence-Douglas, M. G. Ramsay, N. J. Sircombe, P. Gillies, R. G. Evans, H. Schmitz, A. R. Bell, and C. P. Ridgers, *Plasma Phys. Control. Fusion* **57**, 113001 (2015).