

THE  
JOURNAL  
OF  
SYMBOLIC LOGIC

EDITED BY

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## ERRATA

### VOLUME 1

In *A bibliography of symbolic logic*, entry 4189, for « Realisierung », read « Realisierungen ».

### VOLUME 6

Page 183, second column, line 4 from the bottom. For « Notion », read « Notions ».

Page 184, first column, line 4 from the bottom. For « МАСКЭЙЕ », read « МАСКЭЙЕ, James ».

### VOLUME 10

Page 67. In the definition of  $G(P_1, \dots, P_{n+1})$ , for  $J_i(P)$ , read  $J_i(P_i)$ .

Page 79, line 26. For « alteration », read « alternation ».

Page 119, line 10. The expression in quotation marks is «“(Ee)[e realizes  $A(y_1, \dots, y_n)$ ]”».

Page 127, line 16. For « *Prädikatenkalkül* », read « *Prädikatenkalkül* ».

Page 136. In the upper left corner, for « Volume 4, Number 10 », read « Volume 10, Number 4 ».

Page 142, second column, line 6 from the bottom. For « Blanchard », read « Blanshard ».

### VOLUME 11

Page 1. After the line which introduces propositional variables insert the line: « Individual variables  $x, y, z, x_1, y_1, z_1, \dots, x_n, y_n, z_n, \dots$  ».

Page 2, line 6. For  $(A \equiv B)$  read  $(A \equiv B)$ .

Page 4, line 11. Insert  $\sim$  before the third occurrence of  $A$ .

Page 7, line 23. After « if », insert  $\vdash$ .

Page 9, line 33. Insert a parenthesis,  $)$ , immediately before the period at the end of the line.

Page 16. The footnote at the bottom of the page should be numbered 9.

Page 27, line 32. Insert an additional parenthesis,  $)$ , immediately before the comma at the end of the line.

Page 31, line 16. In the definition at the end of the line, the subscript 0 should be a subscript  $i$  (seven times).

Page 65. In the upper left corner, for « Volume 11, Number 4 », read « Volume 11, Number 3 ».

Page 92, line 9. The fifth word in the title of the paper is « *charakteru* ».

Page 97, line 18. At the beginning of the line insert « line ». Also the blank space after line 18 should be deleted.