

**Geometrical Problem.**

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FIGURE 24.

Let OQ, OR be two straight lines meeting at O, and P any point. Required to draw through P a straight line cutting off a given area OAB from the two straight lines.

Draw PD parallel to OR cutting OQ in D.

Construct a  $\triangle OPC$  equal to the given area, and such that OP is one of its sides, and that another of its sides, OC, lies along OQ.

Take OE a mean proportional to OC, OD.

Draw OF perpendicular to OC and equal to half of it.

Join EF, and cut off  $FG = OF$ .

Take  $OA = EG$ . Then PAB is the required straight line.

**PROOF :**

Sqs. on OE, OF = sq. on EF

$$= \text{sqs. on EG, GF,} + 2 \text{ rect. EG} \cdot \text{GF}$$

$\therefore$  sq. on OE = sq. on EG + 2 rect. EG · GF

$$= \text{sq. on OA} + \text{rect. OA} \cdot \text{OC (since OC} = 2\text{GF)}$$

$\therefore$  rect. OC · OD = sq. on OA + rect. OA · OC

$$\text{rect. OC} \cdot (\text{OA} + \text{AD}) = \text{sq. on OA} + \text{rect. OA} \cdot \text{OC}$$

$\therefore$  rect. OC · OA + OC · DA = sq. on OA + rect. OA · OC

$\therefore$  sq. on OA = rect. OC · DA

$\therefore$  OC : DA :: OA<sup>2</sup> : DA<sup>2</sup>

$\therefore$   $\triangle OPC : \triangle DPA :: \triangle OAB : \triangle DAP$

$\therefore$   $\triangle OAB = \triangle OPC = \text{given area.}$

**Colour-sensation and Colour-blindness, with Experiments.**

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