



# CORRIGENDUM

## On wave-driven propulsion – CORRIGENDUM

Graham P. Benham<sup>1,†</sup>, Olivier Devauchelle<sup>2</sup> and Stuart J. Thomson<sup>3</sup>

<sup>1</sup>School of Mathematics and Statistics, University College Dublin, Dublin 4, Ireland

<sup>2</sup>Université de Paris, Institut de Physique du Globe de Paris, CNRS, F-75005 Paris, France

<sup>3</sup>School of Engineering Mathematics and Technology, University of Bristol, Ada Lovelace Building, University Walk, Bristol, BS8 1TW, UK

doi:10.1017/jfm.2024.352, Published by Cambridge University Press, 24 May 2024

### 1. Corrigendum

Upon more detailed inspection, figure 4 in our paper (Benham, Devauchelle & Thomson 2024) did not provide a consistent direct comparison between the present simulation work and the predictions of Longuet-Higgins & Stewart from 1964 (associated Ref. is displayed in our paper). The analysis of Longuet-Higgins & Stewart is summarized and applied in follow-up work from 1977, and provides a quantitative prediction for the force (per unit width) associated with deep-water gravity waves on a floating body as

$$F = \frac{1}{4} \rho g [A^2]_{x=\ell}^{x=-\ell}. \quad (1.1)$$

As such, a difference in the amplitude of the fore and aft wave emission will lead to a net wave thrust (see Ref's by Rhee *et al.* (2022) and Ho *et al.* (2023) in our paper). When one substitutes the dispersion relation for deep-water gravity waves ( $\omega^2 = gk$ ), this can be seen to be consistent with the 'Longuet-Higgins scaling' in the original publication (Benham *et al.* 2024, Eq. (C16)), apart from the prefactor. This classical prediction is derived from first principles and goes beyond scaling, and thus provides an exact prefactor associated with the result allowing for a more direct quantitative comparison. Furthermore, the simulations underlying the original figure 4 were not in fact all conducted in the deep-water limit (i.e.  $kH \gg 1$ ) as stated. When the simulations are repeated while respecting this limit (specifically  $kH = 4$  is sufficient), the exact prediction of Longuet-Higgins is nearly indistinguishable from the present numerical predictions as shown in figure 1 below. Henceforth, we replace figure 4 from the original paper with figure 1 herein.

This new successful comparison in figure 1 suggests that the simple expressions derived in prior work by Longuet-Higgins & Stewart (see Ref. from 1964) are appropriate for application to wave-driven propulsion, provided one operates within the assumptions of the theory. Note that Longuet-Higgins & Stewart derive and provide analogous predictions to (1.1) for the more general case of capillary-gravity waves in finite depth. To the best of our knowledge, while these results have been applied to *estimate* wave-driven propulsive forces in several experiments (e.g. see Ref's by Pucci (2015), Roh & Gharib (2019),

† Email address for correspondence: [graham.benham@ucd.ie](mailto:graham.benham@ucd.ie)

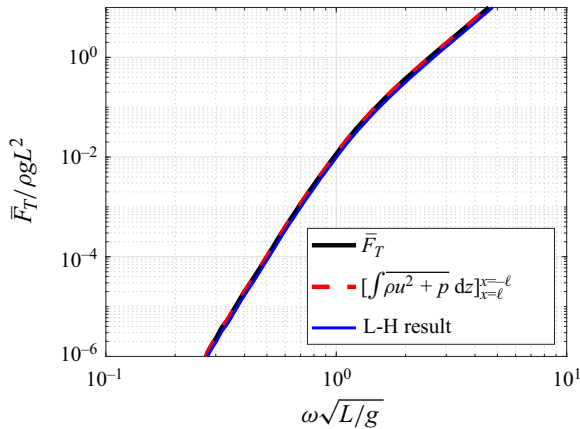


Figure 1. Comparison between the numerically calculated thrust  $\bar{F}_T$  and momentum flux across the domain showing close agreement between the two as well as close agreement with the prediction of Longuet-Higgins (1964) for the case of deep-water gravity waves. Surface tension and viscosity are neglected for the purpose of these calculations, with  $kH = 4$  and  $500 \times 500$  gridpoints in the simulations.

Rhee *et al.* (2022), Ho *et al.* (2023), Barotta *et al.* (2023) in our paper), direct force measurements have not been completed in this context that would likely provide additional clarity to the numerous remaining subtleties in this rich problem.

**Acknowledgements.** We are grateful to Mr Jack-William Barotta and Prof Dan Harris of Brown University for pointing this error out and helping us with the present corrigendum.

**Author ORCIDs.**

-  Graham P. Benham <https://orcid.org/0000-0003-1664-6976>;
-  Olivier Devauchelle <https://orcid.org/0000-0002-7295-4896>.

REFERENCE

BENHAM, G.P., DEVAUCHELLE, O & THOMSON, S.J. 2024 On wave-driven propulsion. *J. Fluid Mech.* **987**, A44.