

THE
JOURNAL
OF
SYMBOLIC LOGIC

EDITED BY

MAX BLACK

ALONZO CHURCH

LEON HENKIN

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ERRATA

VOLUME 3

Page 134, line 32. For the second occurrence of « (IV) », read « (V) ».

VOLUME 6

Page 19, line 31. For « to to », read « to ».

Page 93. In each of the last five lines on this page, replace the last occurrence of = by \neq .

Page 188, second column, line 19 from the bottom and line 6 from the bottom. For 31, read 30.

VOLUME 7

Page 103, line 7 from the bottom. For « Kuratowski », read « Kuratowskiego ».

Pages 111, 112. See the author's footnote on page 9 of volume 14.

VOLUME 9

Page 104, line 25. For « Tarksi's », read « Tarski's ».

VOLUME 10

Page 12, line 7. For « moduc », read « modus ».

VOLUME 11

Page 115. In the second line of XXVI, for the last \neg , read \supset .

Page 116, line 23. For $(\alpha_1)(\alpha_2)B \dots (\alpha_m)$, read $(\alpha_1)(\alpha_2) \dots (\alpha_m)B$.

Page 118, footnote 7, line 3. For A_n , read A_i .

VOLUME 13

Page 133. In †741, change \cup to \cap , and insert a bar over \cup .

Page 168, lines 16–17. For « Adjukiewicz », read « Ajdukiewicz ».

Page 176, line 7. For « dan », read « dans ».

Page 225, line 23. For « mathematiche », read « matematiche ».

Page 225, line 34. For « does », read « goes ».

Page 233, line 6 from the bottom. Delete the first comma in the line.

VOLUME 14

Page 56. Supply the page number, « 56 », in the upper left corner.

Page 63, line 21. For « SMIELEW », read « SZMIELEW ».

Page 71, line 12 from the bottom. For « sciences », read « science ».

Page 70, line 36. For « esprimibilità », read « esprimibilità ».

Page 114. In [8], for « Congrès », read « Congrès ».

Page 116, line 5 from the bottom. For PTQ_1 read PRQ_1 .

Page 118, line 2. For $B_1U_2^*$, read $B_1^*U_2^*$.

Page 118, line 4. For $p + 1 \geq i$, read $i \geq p + 1$.

Page 118, line 3 from the bottom. For $T baab$, read $R baab$.

Page 139, line 13. For « basés », read « basées ».

Page 140, line 16. For « paraissantes », read « paraissant ».

Page 143, line 2 from the bottom; page 144, lines 2, 4, 7. For XIV (62), XIV (63), XIV (64),

Page 163, line 5. For Γ_i , read Γ_1 . [read respectively XIV 62, XIV 63, XIV 64.

Page 163, line 7. For Γ_i , read Γ_i .

Page 165, line 24. For (Λ, E_1, E_2) , read (Λ, E'_1, E'_2) ; and in the latter part of the line, for

Page 165, line 27. For « Λ, E_1, E_2 », read « Λ, E'_1, E'_2 ». [E_1 , read E'_1].

Page 177. In 2.41, for i^n , read i^m .

Page 189, line 18. For « relation numbers », read « relation-numbers ».

Page 193, line 21. For « Structure », read « Structures ».

Page 197, line 23 from the bottom. After « of », insert « the ».

Page 205, line 6 from the bottom. For « AND'S », read « AND's ».

Page 208, line 20. For « methodes », read « méthodes »; and for « de », read « du ».

Page 208, line 23. For « deductive », read « déductive ».