

Research Article

A measurement of Galactic synchrotron emission using MWA drift scan observations

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Abstract

Studying the diffuse Galactic synchrotron emission (hereafter, DGSE) at arc-minute angular scale is important to remove the foregrounds for the cosmological 21-cm observations. Statistical measurements of the large-scale DGSE can also be used to constrain the magnetic field and the cosmic ray electron density of our Galaxy's interstellar medium. Here, we have used the Murchison Widefield Array drift scan observations at 154.2 MHz to measure the angular power spectrum (C_ℓ) of the DGSE of a region of the sky from right ascension 349° to 70.3° at the fixed declination -26.7° . In this RA range, we have chosen 24 pointing centers (PCs), for which we have removed all the bright point sources above ~ 430 mJy (3σ), and applied the Tapered Gridded Estimator on residual data to estimate the C_ℓ . We use the angular multipole range $65 \leq \ell \leq 650$ to fit the data with a model, $C_\ell^M = A \times (\frac{1000}{\ell})^\beta + C$, where we interpret the model as the combination of a power law ($\propto \ell^{-\beta}$) nature of the DGSE and a constant part due to the Poisson fluctuations of the residual point sources. We are able to fit the model C_ℓ^M for six PCs centered at $\alpha = 352.5^\circ, 353^\circ, 357^\circ, 4.5^\circ, 4^\circ$, and 1° . We run the Markov Chain Monte Carlo (MCMC) ensemble sampler to get the best-fit values of the parameters A , β , and C for these PCs. We see that the values of A vary in the range 155–400 mK², whereas the β varies in the range 0.9–1.7. We find that the value of β is consistent at $2 - \sigma$ level with the earlier measurement of the DGSE at similar frequency and angular scales.

Keywords: Large-scale structure of universe; first stars; cosmology: reionisation; diffuse radiation; methods: statistical; technique; interferometric

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1. Introduction

The epoch of reionisation (EoR), when the neutral hydrogen (H I) in the inter-galactic medium (IGM) was nearly completely ionised by the first luminous sources, is one of the least known epochs in cosmology. Direct observations of the EoR using the redshifted H I 21-cm line hold the potential to reveal a substantial volume of astrophysical and cosmological information. Several current and future radio interferometers aim to measure the power spectrum of intensity fluctuations of the EoR 21-cm signal, namely the Giant Metrewave Radio Telescope (GMRT; Swarup et al. 1991; Gupta et al. 2017), the Murchison Widefield Array (MWA; Tingay et al. 2013), the LOw Frequency ARray (LOFAR; van Haarlem et al. 2013), the Hydrogen Epoch of Reionization Array (HERA; DeBoer et al. 2017), and the upcoming SKA-low (Mellema et al. 2013; Koopmans et al. 2015).

Measuring the EoR 21-cm signal is particularly challenging due to the presence of strong foregrounds, which are 4–5 orders of magnitude brighter than the expected 21-cm signal

(Ali, Bharadwaj, & Chengalur 2008; Bernardi et al. 2009; Ghosh et al. 2012; Paciga et al. 2013; Patil et al. 2017). Extra-galactic point sources are the most dominant foreground component at small angular scales, whereas the DGSE dominates at large angular scales (> 10 -arcmin). To mitigate galactic and extra-galactic foreground contamination, interferometric experiments use either foreground avoidance or foreground removal techniques. The foreground avoidance technique relies upon the fact that the foregrounds are intrinsically smooth in frequency and expected to remain restricted in the ‘foreground wedge’ (Datta, Bowman, & Carilli 2010; Thyagarajan et al. 2013). Whereas removal of the foregrounds involves modeling contributions from each component and subtracting them from the observed data. Possibly the most optimal way to extract the EoR 21-cm signal is to use foreground removal in conjunction with the avoidance (Barry et al. 2019; Trott et al. 2020). Essentially, these subtraction techniques rely upon modeling the bright compact sources using longer baselines. The EoR 21-cm signal is pronounced in short baselines that remain dominated by the DGSE. Also, incomplete sky models used in the calibration can also lead to the suppression of DGSE in-turn suppressing the EoR 21-cm signal (Byrne et al. 2019). These make it crucial to measure and model the DGSE particularly at small baselines (large angular scales). Further exclusion of these small baselines in the calibration steps can possibly

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lead to the problem of ‘excess variance’ that is seen in the 21-cm power spectrum estimates (Barry et al. 2016). DGSE models can be used for better calibration thus mitigating these issues. The foreground removal at large scales employs techniques such as Fast Independent Component Analysis (FastICA; Maino et al. 2002), Generalised Morphological Component Analysis (GMCA; Bobin et al. 2007), Smooth Component Filtering (SCF; Elahi et al. 2025), Gaussian Process Regression (GPR; Mertens et al. 2020; Elahi et al. 2023); primarily relies upon the fact that the DGSE is smooth in frequency. An accurate measurement of angular power spectrum (C_ℓ) at different frequencies can quantify the degree of smoothness. Furthermore, current analysis of LOFAR-EoR observations suggests the idea of differentiating the contaminate subtraction process over different distinct spatial scales (Hothi et al. 2020). A measurement of DGSE amplitude at different scales can provide the expected level of contamination to accurate subtraction of foregrounds with relatively lower signal loss. Several 21-cm experiments such as MWA (Byrne et al. 2021), OVRO-LWA (Eastwood et al. 2018), and the LWA New Mexico station (Dowell et al. 2017) are already being used to develop diffuse sky maps to facilitate the precise calibration of 21-cm experiments.

It is, therefore, of considerable interest to measure and quantify the statistical properties of the DGSE, which is an important foreground while measuring the EoR 21-cm power spectrum. The study of the DGSE is also important in its own right. The Galactic synchrotron radiation is mainly emitted by the relativistic electrons rotating in the magnetic fields. The observed fluctuations of the DGSE at different scales will depend on the fluctuation of both density and magnetic field strength. Also, the magnetohydrodynamic turbulence in the interstellar medium plays a significant role in the observed structures of synchrotron emission. Thus, the C_ℓ of the DGSE can probe statistics of the density and magnetic field fluctuation as well as about the nature of the turbulence in the plasma (Cho & Lazarian 2010; Lazarian & Pogosyan 2012; Iacobelli et al. 2013b). The largest linear scale of turbulent component of the galactic magnetic field L_{out} that quantifies the scale of energy injection can be used to investigate the interplay between the magnetic field with the turbulence in the interstellar medium. A measurement of the DGSE angular power spectrum can be used to constrain the outer scales of the turbulence L_{out} and in-turn the relative strength of the magnetic field (Iacobelli et al. 2013b). Also, the observed DGSE can be used to differentiate the contribution in the diffuse emission from the thermal and non-thermal components.

There are several observations spanning a wide range of frequencies which characterise the Galactic synchrotron emission at different angular scales. Haslam et al. (1981) have first measured the brightness temperature of the Galactic synchrotron radiation at 408 MHz radio frequency. Later, Remazeilles et al. (2015) reprocessed the raw data to produce an improved 408-MHz all-sky map. Reich (1982), Reich & Reich (1986) generated the synchrotron map for the northern sky but at a relatively higher frequency (1.4 GHz). Reich et al. (2001) repeated the analysis for the southern sky using a 30 m radio telescope at Villa Elisa, Argentina. The all-sky spectral index of the synchrotron emission can be measured using these observations at different frequencies (Reich & Reich 1988; Guzmán et al. 2011). de Oliveira-Costa et al. (2008) have produced a Global Sky Model (hereafter, GSM) for the synchrotron map using 11 most accurate data in the frequency range 10 MHz to 94 GHz. Zheng et al. (2016) have improved the GSM map by using 29 sky maps from 10 MHz to 5 THz. Upcoming

310 MHz observation using the Green Bank telescope (GBT) along with custom instrumentation expected to produce absolute DGSE map calibrated zero level (Singal et al. 2023).

It is useful to consider the C_ℓ to quantify the two-point statistics of the DGSE. Several authors have used the all-sky maps to estimate C_ℓ of the DGSE. At 2.4 GHz, Giardino et al. (2001) have found that C_ℓ follows a power-law $C_\ell \propto \ell^{-\beta}$ with $\beta = 2.43 \pm 0.01$ in the ℓ range 2–100, when estimated across the entire sky. They also found that the slope appears to steepen ($\beta = 2.92 \pm 0.07$) at higher Galactic latitudes. Bennett et al. (2003) have used the *Wilkinson Microwave Anisotropy Probe* (WMAP) data and found that $\beta = 2$ for the ℓ range 2–100. La Porta et al. (2008) have used data from two different frequencies, 408 MHz and 1.4 GHz, to estimate the C_ℓ separately at different parts of the sky, for which the values of β are found to be in the range 2.6–3.0 for $\ell < 300$ (angular scale greater than 1 deg). However, the angular ranges and the frequencies in most of these observations are larger than those corresponding to most EoR 21-cm observations.

Directly addressing radio-interferometric observations at the angular scales and frequencies relevant for EoR 21-cm observations, Bernardi et al. (2009) have first analysed Westerbork Synthesis Radio Telescope (WSRT) data to measure C_ℓ of the DGSE at 150 MHz for a particular pointing direction. They found that the power law behaviour $C_\ell \propto \ell^{-\beta}$, and obtained $\beta = 2.2$ at the angular multipoles $\ell < 900$. Ghosh et al. (2012) have analysed a single pointing of the GMRT 150 MHz observations and found the value $\beta = 2.34$ for the ℓ range $253 \leq \ell \leq 800$. Iacobelli et al. (2013a) showed that the C_ℓ follows a power-law at even smaller angular scales ($\ell \leq 1300$), and they found a slightly smaller value $\beta = 1.8$. Choudhuri et al. (2016b), (2020) used the TIFR GMRT Sky Survey (TGSS) (Sirothia et al. 2014; Intema et al. 2017) data to estimate C_ℓ of the DGSE for different pointing directions distributed all over the sky. This is the first all-sky measurement of C_ℓ at this low frequency of 150 MHz. They also found the slopes β in the range 2–3 for two slightly off-galactic pointing directions.

In this paper, we consider the MWA drift scan observations (Patwa, Sethi, & Dwarakanath 2021), which were originally carried out to measure the EoR 21-cm signal. This observation is carried out at the fixed declination (DEC; δ) of -26.7° , and it covers a region of the sky from right ascension (RA; α) 349° to 70.3° at an interval of 0.5° along α . Visibilities are dumped every 2 min with a total of 163 different pointings centers (PCs). This drift scan observation covers both EoR 0 ($0^\circ, -26.7^\circ$) and EoR 1 ($60^\circ, -26.7^\circ$), which are two of the main targets of MWA EoR 21-cm experiments (Beardsley et al. 2016). It is particularly important to quantify the foregrounds in this region of the sky where a substantial effort is underway to detect the EoR 21-cm signal. Although this observation has 163 PCs, we have analyzed a total of 24 PCs in this paper. Out of the 24 PCs, 21 PCs span the α range from 349° to 70.3° at regular 4° intervals, and 3 PCs are located at intermediate RAs. The interval of 4° along the RA is sufficient to capture the variation of intensity of the DGSE. We have used the Tapered Gridded Estimator (TGE; Choudhuri et al. 2016a) to characterise the DGSE for this observation. The full-width-at-half-maximum (FWHM) of the MWA primary beam is 27° at 154.2 MHz (Franzen et al. 2016), and we used a window with FWHM 15° to taper the response of the primary beam. We are able to fit the data with a model only for 6 PCs at $\alpha = 352.5^\circ, 353^\circ, 357^\circ, 4.5^\circ, 4^\circ$ and 1° . A brief outline of this paper follows: In Section 2, we discuss the data analysis and

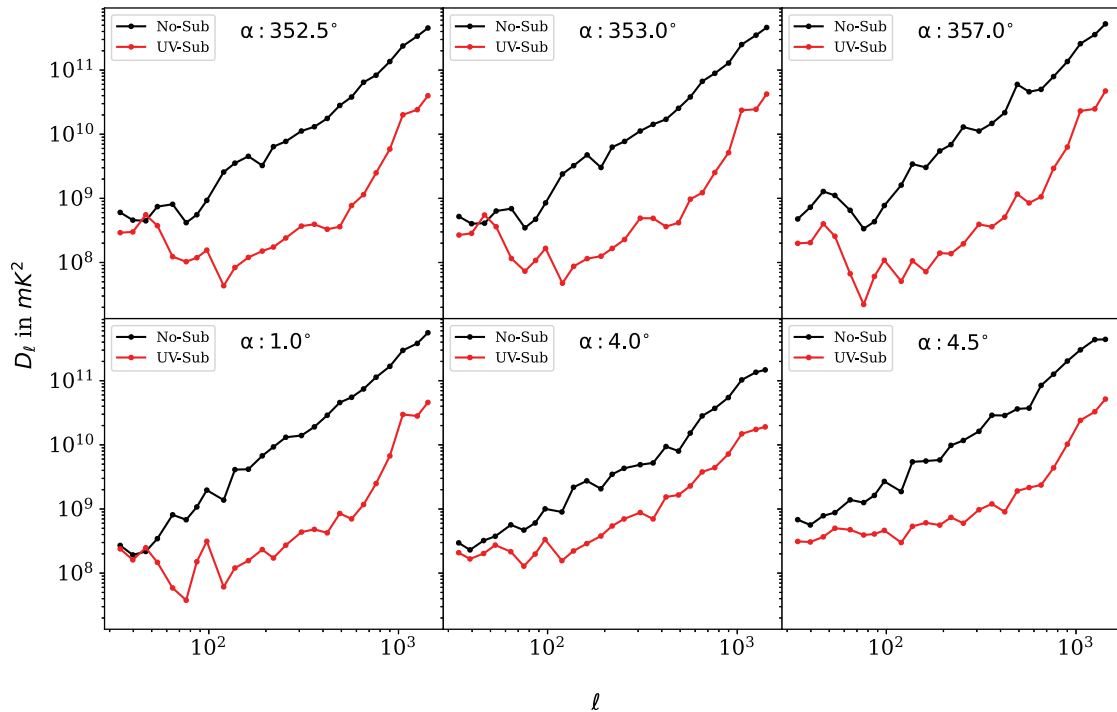


Figure 1. This shows the estimated $\mathcal{D}_\ell = \ell(\ell + 1)C_\ell/2\pi$ as a function of ℓ for six pointing centered at $\alpha = 352.5^\circ, 353^\circ, 357^\circ, 4.5^\circ, 4^\circ$ and 1° , and δ remain the same for all pointing at $\delta = -26.7^\circ$. The black lines show the total data before point source subtraction, and the red lines show the C_ℓ after removing the sources above 3σ .

methodology. The results of this study are discussed in [Section 3](#), and we summarise and conclude in [Section 4](#).

2. Methodology

In this section, we describe the methodology used to estimate the angular power spectrum C_ℓ of the DGSE using MWA drift scan observations. Here, we have used the Phase II compact configuration of the MWA radio telescope (Lonsdale et al. 2009; Wayth et al. 2018). The maximum extent of this configuration is 488 m, which is suitable for studying large-scale diffuse emission from the sky. We consider a particular drift-scan observation (project ID G0031; Patwa et al. 2021) with an observing time of 5 h 24 min per night, and the same sky is observed for 10 consecutive nights. Since the observations cover the same region of the sky everyday, we perform Local Sidereal Time (LST) stacking of the measured data (e.g. Bandura et al. 2014; Collaboration et al. 2022) and obtain the equivalent one-night drift scan data. The δ for this drift scan observation is fixed at -26.7° , and α changes from 349° to 70.3° . [Figure 1](#) of Chatterjee et al. (2024) shows the total sky coverage for this observation. The bandwidth of this observation is 30.72 MHz, centered at $\nu_c = 154.2$ MHz and the total bandwidth is divided into 24 coarse-bands with 32 channels each. Frequency resolution of each channel is $\Delta\nu_c = 40$ kHz.

The flagging and calibration details for these data sets are presented in Patwa et al. (2021). Here, we have used the calibrated visibilities to make a continuum image of angular extent $30^\circ \times 30^\circ$ centred on our PC. We have used the multi-scale CLEAN feature of WSCLEAN (Offringa et al. 2014; Offringa & Smirnov 2017) with a cleaning threshold of 3σ and ‘Briggs -0.1’ weighting-scheme. We have used only the longer baselines ($|u| > 50\lambda$) during imaging

in order to avoid large-scale diffuse emission during the deconvolution process. This step will help to model the bright sources only, and we plan to remove them from the total visibility data to study the residual large-scale diffuse emission. The resolution of the final images are relatively poor, as an example for $\alpha = 4.5^\circ$ the FWHM of synthesise beam is $\approx 18.5' \times 11.0'$ with a position angle of 42.3° . We have identified and modelled sources with flux density $S > S_c \approx 3\sigma$ ($= 430$ mJy) from the entire image, where σ is the r.m.s. noise estimated from a source free region (see [Table 1](#)). We have subtracted out the model visibilities corresponding to the CLEAN component of our sources from the visibility data and used this for the subsequent analysis. To validate our source identification, we have used PyBDSF (Mohan & Rafferty 2015) to extract a source catalogue from our primary beam-corrected image. For source identification, we use a central region of radius 7.5° where the primary beam is quite well quantified. We have compared the angular position and flux of our sources with those in the GLEAM survey (Wayth et al. 2015). We found the maximum deviation are less than 50 arcsec for all source, whereas the median flux deviation remain less than 25% for the sources above 800 mJy. We show the comparison results in [Appendix A](#) for one pointing only centered at $(\alpha, \delta = 4.3^\circ, -26.7^\circ)$ for validation and found that the source properties match quite reasonably with the GLEAM catalogue.

In this paper, we have used a visibility-based power spectrum estimator, namely the TGE, to estimate C_ℓ for the data both before and after source removal. The detailed mathematical formalism of the TGE has been discussed in several earlier works (Choudhuri et al. 2016a, 2017, 2020), and we briefly summarise the main features here. First, TGE uses gridded visibilities to reduce the computation. Second, the TGE tapers the sky response with a tapering function $\mathcal{W}(\theta)$ that suppresses the contribution from the

Table 1. This table provides the details of the model fitting for 6 PCs. The column descriptions are as follows: (1) RA of the pointings, (2) rms of the image, (3) (4) (5) the best-fit value of parameter A , β and C after MCMC run (equation 4), (6) χ_R^2 , and (7) p -value.

α	σ (in mJy)	A (in mK ²)	β	C (in mK ²)	χ_R^2	p -value
352.5°	146.4	154.3 ^{+397.5} _{-114.6}	1.4 ^{+0.6} _{-0.6}	1 199.1 ^{+292.5} _{-540.2}	1.147	0.313
353.0°	150.0	201.9 ^{+525.3} _{-167.4}	1.1 ^{+0.8} _{-0.5}	1 214.6 ^{+337.7} _{-633.5}	2.185	0.008
357.0°	143.5	241.2 ^{+603.2} _{-200.3}	0.9 ^{+0.8} _{-0.5}	1 255.9 ^{+348.9} _{-674.5}	1.585	0.081
1.0°	177.9	568.4 ^{+398.9} _{-314.9}	0.9 ^{+0.3} _{-0.2}	777.7 ^{+471.8} _{-494.7}	1.234	0.247
4.0°	146.0	388.3 ^{+1133.5} _{-297.9}	1.3 ^{+0.6} _{-0.6}	4 057.5 ^{+916.9} _{-1675.1}	1.018	0.430
4.5°	143.3	407.7 ^{+353.7} _{-211.0}	1.7 ^{+0.3} _{-0.3}	2 574.8 ^{+679.0} _{-777.0}	0.656	0.839

outer region of the primary beam. Here, we have used a Gaussian $\mathcal{W}(\theta) = e^{-\theta^2/\theta_w^2}$ that peaks around $\theta = 0$ and falls off rapidly away from the centre. The tapering function $\mathcal{W}(\theta)$ has a FWHM $\theta_{\text{FWHM}} = \theta_w/0.6$ and for this work we have used $\theta_{\text{FWHM}} = 15^\circ$. Our earlier study (Chatterjee et al. 2022) shows that the choice of the FWHM of 15° results in reasonable SNR values while keeping the foreground contamination from far field sources to a minimum. The tapering is implemented by convolving the measured visibilities with $\tilde{w}(\mathbf{u})$, the Fourier transform of $\mathcal{W}(\theta)$. Considering a square grid in the uv plane, $\mathcal{V}_g$ the convolved visibility at a grid point g can be written as

$$\mathcal{V}_g = \sum_i \tilde{w}(\mathbf{u}_g - \mathbf{u}_i) \mathcal{V}_i \quad (1)$$

where $\mathbf{u}_g$ refers to the baseline corresponding to the grid point g , and $\mathcal{V}_i$ is the visibility measured at baseline $\mathbf{u}_i$. Third, the TGE provides an unbiased estimate of the true sky signal by subtracting the noise bias that arises due to the self-correlation of the measured visibilities. The TGE is given by

$$\hat{E}_g = M_g^{-1} \left(|\mathcal{V}_g|^2 - \sum_i |\tilde{w}(\mathbf{u}_g - \mathbf{u}_i)|^2 |\mathcal{V}_i|^2 \right), \quad (2)$$

where $\langle \hat{E}_g \rangle = C_{\ell_g}$ with $\ell_g = 2\pi |\mathbf{u}_g|$. Here, M_g is a normalising factor, which we calculated using simulated visibilities corresponding to a unit angular power spectrum (UAPS), $C_\ell = 1$. To reduce the statistical fluctuations, we have used 50 realisations of UAPS to estimate M_g . Chatterjee et al. (2022) presents an extensive description of the simulations used to estimate M_g for MWA observations. It has further validated the TGE, considering simulated MWA observations.

We have divided the uv plane into annular rings and binned the estimated C_{ℓ_g} , assuming the sky signal to be statistically isotropic in the plane of the sky. We finally have estimates of the binned C_ℓ at the mean ℓ value corresponding to each bin. To avoid the effect of bandwidth smearing, we have used 17 channels of total bandwidth 0.68 MHz centred at 154 MHz for further analysis. We further averaged those 17 channels to make an equivalent single-channel data for C_ℓ estimation, presented in the next section.

3. Results

Figure 1 shows the measured mean-squared brightness temperature fluctuation

$$\mathcal{D}_\ell = \ell(\ell + 1) C_\ell / 2\pi \quad (3)$$

for both before (No-Sub) and after (UV-Sub) point source subtraction from the 6 PCs where we are able to measure the

contribution of the DGSE from the residual visibility data. In each panel, the red and black lines show the ‘No-Sub’ and ‘UV-Sub’ cases, respectively. We find that, in the No-Sub scenarios, $\mathcal{D}_\ell$ ranges from approximately $\sim 2 \times 10^8$ mK² to $\sim 5 \times 10^{11}$ mK² for ℓ values in the range 40 and 1 000. The amplitude of the $\mathcal{D}_\ell$ is consistent with earlier observations with the GMRT at the same frequency range (Choudhuri et al. 2017, 2020). We also note that $\mathcal{D}_\ell \propto (\ell/1\,000)^2$ for $\ell > 200$ for all pointings, which indicates that the measured $\mathcal{D}_\ell$ is dominated by the Poisson fluctuations due to bright point sources (Ali et al. 2008). Next, to study the statistical properties of the DGSE, we have removed the point sources with flux $S > S_c \approx 3\sigma$ (Table 1) from the data and used the residual data to estimate $\mathcal{D}_\ell$. After removing the bright sources, we see that the amplitude falls significantly across the whole ℓ range. However, we clearly see two distinct ℓ ranges in the residual $\mathcal{D}_\ell$. After point source subtraction, the amplitude decreases by a larger amount at the high ℓ values ($\ell > 200$) compared to the smaller ℓ . At high ℓ , we find again that $\mathcal{D}_\ell \propto (\ell/1\,000)^2$. The sky signal in this ℓ range is mainly dominated by the Poisson fluctuations from the point sources that are below our flux limit $S \leq S_c$, which we are not able to subtract out. We expect the sky signal ($\mathcal{D}_\ell$) at this ℓ range to go down even further if we have more sensitive observations where we can achieve a lower value of S_c . At lower ℓ (≤ 200), the sky signal does not go down as much after point source subtraction. The slope here is shallower than $\mathcal{D}_\ell \propto \ell^2$. We believe that the DGSE starts to dominate the sky signal at $\ell \leq 200$ after point source subtraction. Further, we do not expect the sky signal at the DGSE-dominated small ℓ (≤ 200) range to go down much, even if it is possible to lower S_c and improve point source subtraction.

Figure 2 shows the estimated C_ℓ (red solid line) of the residual sky signal for the UV-Sub case. Here, we show the results for aforementioned 6 PCs. We interpret the measured C_ℓ as a combination of a power law ($\propto \ell^{-\beta}$) due to DGSE and a constant Poisson fluctuation part due to the residual point sources. Here, we have used

$$C_\ell^M = A \times \left(\frac{1\,000}{\ell} \right)^\beta + C \quad (4)$$

to model the residual C_ℓ . Later, we used the Markov Chain Monte Carlo (MCMC) ensemble sampler to estimate the best-fit values and errors for the model parameters A , β and C . To estimate the measurement errors, we assume that the residual sky signal is a realisation of a Gaussian random field with a given angular power spectrum. In reality, it is quite likely that this assumption is not strictly valid for the actual data. However, little is known about the statistics of the residual signal, and this assumption considerably simplifies the analysis. To estimate the 1σ error bars of the

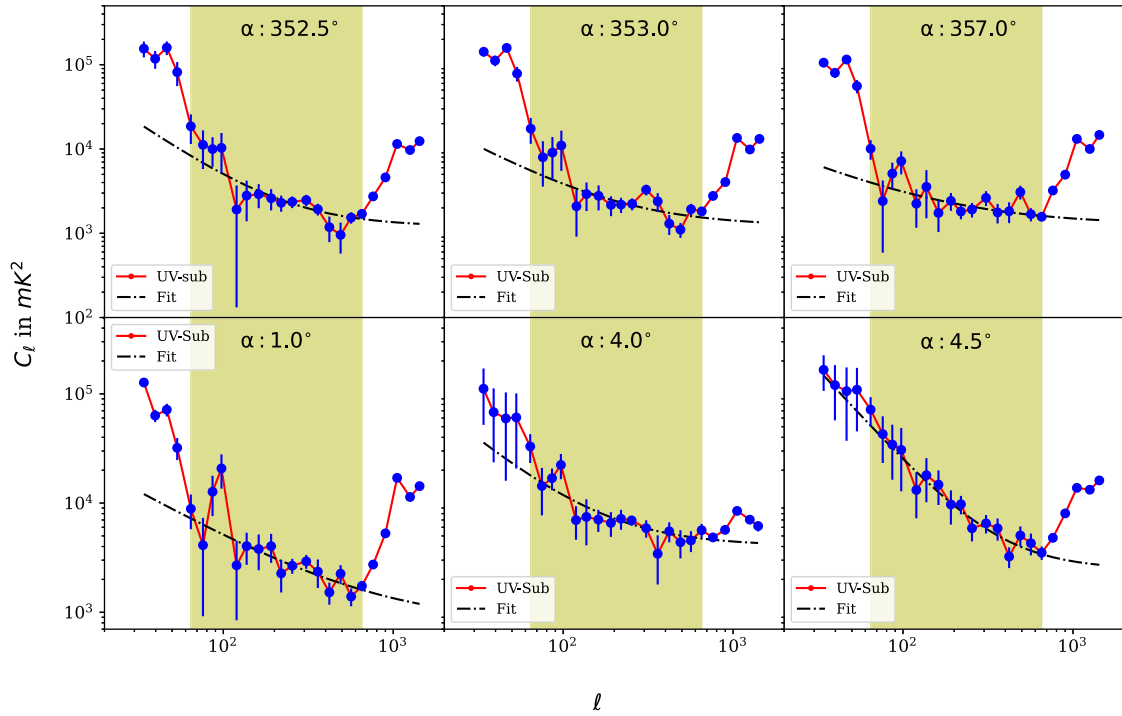


Figure 2. The blue points show the estimated angular power spectrum C_ℓ as a function of ℓ with 1σ error bars from the residual data. The black dot-dashed line shows the model C_ℓ^M (equation 4) with best-fitted parameters from the MCMC run. The shaded region ($65 \leq \ell \leq 650$) shows the data range used for the fitting.

estimated C_ℓ , we have simulated 40 independent Gaussian random realisations of the residual sky signal and estimated the resulting visibilities. The sky signal was simulated so that we roughly recover the estimated C_ℓ if we analyse the simulated visibilities in exactly the same way as the actual data. The simulated visibilities also include a Gaussian random system noise contribution with the same r.m.s. in the actual data. In this observation, we expect the r.m.s. noise is likely dominated by thermal receiver noise, and the confusion noise from unresolved point sources is insignificant for the pointing considered here. We have used the r.m.s. of the 40 independent realisations of the simulated C_ℓ to estimate the 1σ errors for the estimated C_ℓ .

We expect C_ℓ measured at low ℓ to be affected by the convolution with the primary beam and the tapering function. Using realistic simulations, Chatterjee et al. (2022) showed that the range $\ell \geq 65$ is largely unaffected by convolution for the tapering window function, and we have excluded the range $\ell < 65$ for fitting equation (4). We further notice that the residual C_ℓ increases sharply at $\ell > 650$. Our data has poor sampling at the longer baselines, and it is possible that the source subtraction is not very effective at these small angular scales. Here, we have also discarded the range $\ell > 650$ for fitting equation (4).

We use the ℓ range $65 < \ell < 650$ to fit the model C_ℓ^M (equation 4) with the measured values from the data. As mentioned, we have used the MCMC ensemble sampler to get the best-fit values of the model parameters A , β , and C . Here, we have used the python module EMCEE (Foreman-Mackey et al. 2013), which implements the affine-invariant ensemble sampling (Goodman & Weare 2010) algorithm, to get the posterior probability distribution of the parameters. We assumed a Gaussian likelihood function for this analysis. Also, we set a uniform prior of the parameters in the ranges: $\mathcal{U}(0, \infty)$ on A , $\mathcal{U}(0, 5.0)$ on β and $\mathcal{U}(0, \infty)$ on C . We put

the condition that A would always be positive based on the earlier analysis of the DGSE (Choudhuri et al. 2017). In the MCMC run, we used 32 random walkers initialised randomly, and we ran the full chain for 100 000 steps, out of which 10 000 steps are discarded for the burn-in process. We show the best-fit model C_ℓ^M after the MCMC run, along with the measured C_ℓ from the MWA observations. The black dot-dashed lines in Figure 2 show the best-fit model C_ℓ^M (equation 4) after MCMC run for these 6 PCs. This figure also highlights the range $65 \leq \ell \leq 650$ that has been used for model fitting. We see that the model fits quite well the measured C_ℓ in this range, and the reduced chi-square (χ_R^2) values for the fit, and the p -value^a are given in Table 1. In the figure, we also plot the C_ℓ^M beyond the range $65 \leq \ell \leq 650$, used for the fitting. This is to show the expected sky contribution beyond this fitted region without any noise and convolution error.

Figure 3 shows the posterior distributions of the parameters A , β and C for one PC centered at $\alpha = 4.5^\circ$. The diagonal panels show the one-dimensional marginalised posterior distributions for the parameters. The off-diagonal panels show the 2D contours of correlations between parameter pairs. The vertical lines from the left are the 16th (black), 50th (green), and the 84th (black) percentile, respectively. The best-fit values of the parameters and their corresponding errors are as follows: $A = 407.7^{+353.7}_{-211.0}$, $\beta = 1.7^{+0.3}_{-0.3}$, and $C = 2574.8^{+679.0}_{-777.0}$. We see that all the parameters are strongly correlated. The parameters β and C are positively correlated, while

^aThe probability-to-exceed (PTE or p -value) is the probability of obtaining a value of χ^2 higher than what is obtained, and defined as $p = 1 - \text{CDF}(\chi^2; f)$ where CDF is the cumulative distribution function of the χ^2 distribution and f is the number of degrees of freedom. A low p -value would imply that there is an unlikely chance of obtaining a higher χ^2 than what is already obtained. It suggests that the model and the data are more distinct from each other than what a random chance would allow (see e.g. Rice 2006).

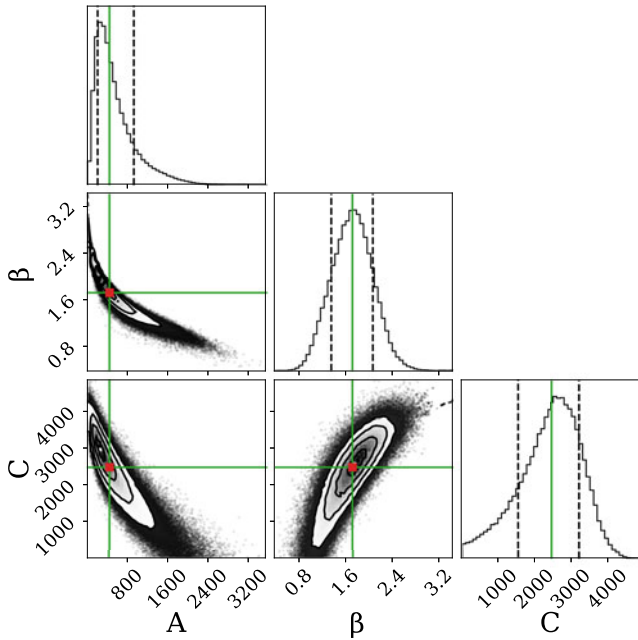


Figure 3. The posterior distributions of the parameters A , β , and C for PC centered at $\alpha = 4.5^\circ$. The best-fit values of the parameters and their corresponding errors are as follows: $A = 407.7^{+353.7}_{-211.0}$, $\beta = 1.7^{+0.3}_{-0.3}$ and $C = 2574.8^{+679.0}_{-777.0}$. We see that the parameters β and C are positively correlated, while A shows a negative correlation with both.

A shows an anti-correlation with both. The Pearson's product-moment correlation coefficients for A with β and C are -0.9 and -0.89 , respectively, whereas the same for β with C is 0.84 . We have shown the posterior distribution of rest of the PCs in Appendix B.

In Table 1, we report the median value, which represents the 50th percentile, alongside the upper and lower limits corresponding to the 84th and 16th percentiles, respectively. We find that the amplitude A varies significantly for different pointings. The pointing centered at $\alpha = 352.5^\circ$ has the lowest amplitude 154.3 mK^2 , whereas the $\alpha = 1^\circ$ has the highest amplitude of 568.4 mK^2 . We expect the residual C_ℓ to be dominated most likely by the DGSE, and the amplitude may vary depending on the location of the PC with respect to the Galactic plane. We have seen a similar variation of the amplitude at different pointing centers using the all-sky TGSS survey (Choudhuri et al. 2020). The values of β vary in the range 0.9 – 1.7 , which are consistent with other measurements in this frequency range (Bernardi et al. 2009; Ghosh et al. 2012; Iacobelli et al. 2013a; Choudhuri et al. 2016b). The constant part C is coming due to unsubtracted point sources in the field and varies in the range 777 – 4057 mK^2 for different pointing. To show the goodness of the fit, we quoted the value of χ^2_R and p -values for all pointings in Table 1. We see that 5 out of the 6 PCs have the p -values > 0.05 , which implies that the model provides a reasonable fit to the data for these PCs. Considering the PC centered at $\alpha = 353^\circ$, we find the p -value to be 0.008 . Although the fit is poorer for this PC, there is still a 0.8% chance for the model to fit the data, and we have considered this to be acceptable.

We have identified 6 PCs (out of the 24 PCs) for which the residual angular power spectra C_ℓ could be fitted with a model C_ℓ^M given in equation (4). For the remaining PCs, the measured C_ℓ does not exhibit a power-law behavior, and we show one such representative PC ($\alpha = 37^\circ$) in Figure 4. Here, we see that the best-fit model C_ℓ (black dot-dashed) is nearly flat across the entire ℓ range.

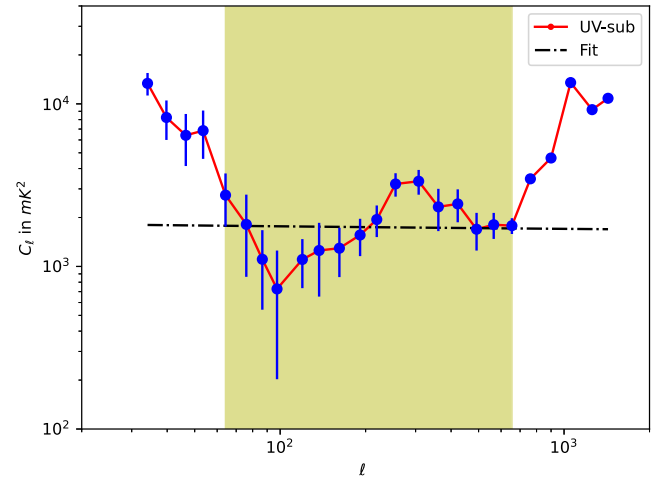


Figure 4. The blue points show the estimated C_ℓ as a function of ℓ with $1 - \sigma$ error bars from the residual data for a PC centered at $\alpha = 37^\circ$. The black dot-dashed line shows the fitted model, which is a straight line with amplitude $A = 272.8^{+719.2}_{-238.6}$. Here, we are not able to fit the data points with a power-law model (equation 4).

We attribute this flatness to the unclustered Poisson distribution of faint point sources within this PC (Ali et al. 2008). These sources have flux densities below the 3σ threshold and thus could not be subtracted using the standard technique. Further, imaging artifacts around bright sources, possibly arising from residual gain calibration errors, may affect the measured C_ℓ . We note that the observations that we consider here are shallow (~ 17 min per PC), and the limited baseline coverage results in poor angular resolution, and these make it difficult to subtract compact sources accurately, which in turn leads to the failure of fitting a model to the C_ℓ . We also note that the bright source Fornax A starts to dominate the visibilities during the latter part of the observation $\alpha \gtrsim 40^\circ$ (Chatterjee et al. 2024), which makes it difficult to model the residual visibilities in that region.

4. Summary and conclusions

In this paper, we studied the statistical properties of the DGSE in terms of the angular power spectrum. For this purpose, we used the drift scan observations of the Phase II compact configuration of the MWA. Here, we analyze total 24 PCs to characterise the DGSE, however, we are only able to fit the data with a model for 6 PCs centered at $\alpha = 352.5^\circ, 353^\circ, 357^\circ, 4.5^\circ, 4^\circ$, and 1° . The total observing time for each pointings is of around 17 min (a total 10 nights of LST stacking). We removed all the bright point sources above 3σ (Table 1) to detect the DGSE, which is the most dominant component at low-frequency observation after point source removal.

We apply the TGE to measure the $\mathcal{D}_\ell$ (equation 3) of the DGSE. In Figure 1, we show both the measured $\mathcal{D}_\ell$ before and after the point source removal. The value of the $\mathcal{D}_\ell$ before point source subtraction varies from $\sim 2 \times 10^8 \text{ mK}^2$ to $\sim 5 \times 10^{11} \text{ mK}^2$ for ℓ values in the range 40 and 1000. Also, it follows a power law $\mathcal{D}_\ell \propto \ell^2$ for $\ell > 200$. This behaviour of $\mathcal{D}_\ell$ is due to the Poisson fluctuations of the bright point sources, and it is consistent with the model prediction (Ali et al. 2008). We removed the bright sources with flux $S > S_c \approx 3\sigma$ from the data and measured the $\mathcal{D}_\ell$ from the residual data. Here, we clearly see two distinct ℓ ranges in the measured $\mathcal{D}_\ell$. At higher ℓ values ($\ell > 200$) values, it follows the same power law

$\mathcal{D}_\ell \propto \ell^2$; however, the amplitude falls substantially as compared with the case where the bright sources are not removed. We expect this higher ℓ range in the residual data to be dominated by the Poisson fluctuations of the point sources below 3σ level. At lower ℓ (≤ 200), the slope is shallower than $\mathcal{D}_\ell \propto \ell^2$, and we believe the DGSE dominates at large angular scales or lower ℓ range.

We fit the residual $\mathcal{C}_\ell$ with a model as given in equation (4). Here, the power-law part is due to the large-scale DGSE, and the constant part is due to the unsubtracted point sources at small angular scales. We found that the convolution of the primary beam affects the lower ℓ range ($\ell \leq 65$). Also, the large ℓ values ($\ell \geq 650$) are dominated by the system noise due to the limited number of samples in those bins. We use only the range ($65 \leq \ell \leq 650$), as shown with a shaded region in Figure 2, to fit the measured $\mathcal{C}_\ell$ with the model. We have used the MCMC ensemble sampler to estimate the best-fit values and errors for the model parameters A , β , and C . In Figure 3 (and Figures B1–B3), we show the posterior distribution of those parameters (diagonal panels) and also the correlation of these parameters (off-diagonal panels). We found a strong anti-correlation of parameter A with β and C , and a strong correlation between β and C . The best-fit values (50th percentiles) and their uncertainties (16th and 84th percentiles) of parameters A , β , and C are given Table 1. The values of A ranges from 154.3 to 568.4 mK². This is because of the different contributions of the Galactic emission in different pointings we considered here. The values of β changes from 0.9 to 1.7 for different pointings. These β values are consistent with 2σ measurement with the earlier measurement in a similar angular and frequency range (Bernardi et al. 2009; Ghosh et al. 2012; Iacobelli et al. 2013a; Choudhuri et al. 2017). The constant part C is coming due to unsubtracted point sources in the field and varies in the range 777–4 457 mK² for different pointing.

We studied a large patch of the sky in the southern hemisphere using the MWA drift scan observation to characterise the DGSE. Earlier, we did a similar study for the entire sky using the TIFR-GMRT sky survey at 150 MHz (Choudhuri et al. 2016a, 2020). Here, we expect the signal to be dominated by large-scale diffuse emission, and we assume it is a Gaussian random field generated by some statistical random process, e.g., MHD turbulence. We can use this to model the diffuse foreground model and subtract from the data for EoR observation in this region. The amplitude of $\mathcal{C}_\ell$ at $\ell = 1\,000$ varies for different pointings considered in this analysis. This variation is expected because the intensity of the Galactic synchrotron emission highly depends on the fluctuations of electron density and the magnetic field of the sky's position. This study will help us to constrain the electron density and the magnetic field strength in this region. Recently, Chakraborty et al. (2019) have studied the spectral nature of the $\mathcal{C}_\ell$, and found that the amplitude vs frequency follows a double power law nature with a break at 405 MHz. Next, we plan to analyse the a large bandwidth of MWA data to characterise the spectral nature of the $\mathcal{C}_\ell$ for different pointings. This will help us study the statistical properties of the DGSE for a large area of the sky and at different frequencies.

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Appendix A. Astrometry

In this appendix, we show the comparisons of the point sources extracted using this MWA observation with the GLEAM survey (Wayth et al. 2015). We select all the bright sources above 430 mJy/beam from a region of radius 7.5° centred at $(\alpha, \delta = 4.3^\circ, -26.7^\circ)$. The total number of sources we got from this observation is around 400. For rest of the discussion we consider an angular scale of $0.4 \times \theta_{\text{FWHM}}$, as the reliability of primary beam modeling plunges after that. This reduces the effective number of sources to 190. First, we compare the position of the sources from these two catalogues. The left panel of Figure A1 shows the position offset in terms of $(\Delta RA = \alpha_{\text{Drift}} - \alpha_{\text{GLEAM}})$ and $(\Delta DEC = \delta_{\text{Drift}} - \delta_{\text{GLEAM}})$ of the 190 number of sources from these two catalogues. Here, the deviations are less than 50 arcsec for all sources. Note that the angular resolution of this observation is around $18.54' \times 11.1'$. Also, the deviation is symmetric around zero along RA; however, there is a slight offset ($\sim 30''$) along DEC. The effect of the ionosphere can shift the position of the bright point source, and this can lead to inaccuracies during source subtraction and, potentially, signal loss. In presence of extreme ionospheric activity, performance of the calibration process becomes poor

which may introduce systematic offset (Chege et al. 2022; Pal, Datta, & Mazumder 2024). The offset of ($\sim 30''$) along DEC is significantly smaller than the synthesised beam and we expect this to have a very minimal impact on our analysis. We conclude that the recovered position of the sources matches the GLEAM catalogues reasonably. As we are removing these point sources from the data, this offset will not introduce any bias in our final power spectrum measurement of the residual visibility data.

We also compared the recovered flux values with the GLEAM sources for those 190 sources. The upper right panel of Figure A1 shows the GLEAM flux values, extrapolated from 151 to 154 MHz using the measured spectral index from the GLEAM survey, along the x -axis and the flux recovered from this observation along the y -axis. The black dashed line shows the 1:1 line. We see that all the points at higher flux values lie on top of the line; however, for small flux values, the points deviate significantly. The lower panel of the right panel shows the fractional deviation (Δ) of the recovered flux with respect to the GLEAM flux. We see that for most sources, Δ is less than 25%; however, there are few sources for which the Δ becomes large ($\geq 25\%$). We expect this flux deviation might be due to the error in the flux calibration for this observation. We are not planning to do any flux correction for this observation, as those sources are removed from the data.

Appendix B. MCMC results for PCs

In Figures B1–B3, we show the posterior probability distribution of the model parameters A , β , and C . The diagonal plots show the one-dimensional marginalised posterior distribution of those three parameters, whereas the off-diagonal panels show the posterior of each pair of parameters. The green vertical lines in the diagonal panels in all of the figures show the 50th percentiles of the samples in the marginalised distributions, and two vertical black lines show the 16th and 84th percentiles. The best-fit values (50th percentiles) and their uncertainties (16th and 84th percentiles) of those parameters are shown. We see a strong anti-correlation of parameter A with β and C . Since we have given only positive prior ranges for all the analysed PCs, we see that in some of the cases the posterior probability distribution is abruptly cut off. Apart from only a few, almost all the posterior distributions are very asymmetrical in nature.

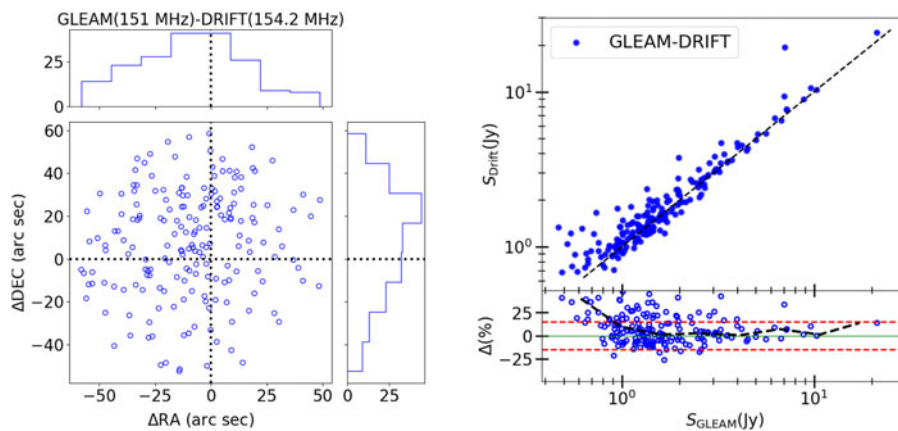


Figure A1. The left panel shows the position offset in terms of $(\Delta RA = \alpha_{\text{Drift}} - \alpha_{\text{GLEAM}})$ and $(\Delta DEC = \delta_{\text{Drift}} - \delta_{\text{GLEAM}})$ of the 190 number of sources from this observation and GLEAM catalogue. The upper right panel shows the GLEAM flux values extrapolated from 151 to 154 MHz along the x -axis and the flux recovered from this observation along the y -axis. The lower panel shows the fractional deviation (Δ) of the recovered flux values with respect to the GLEAM catalogue, and the black dashed show the binned median values of the Δ .

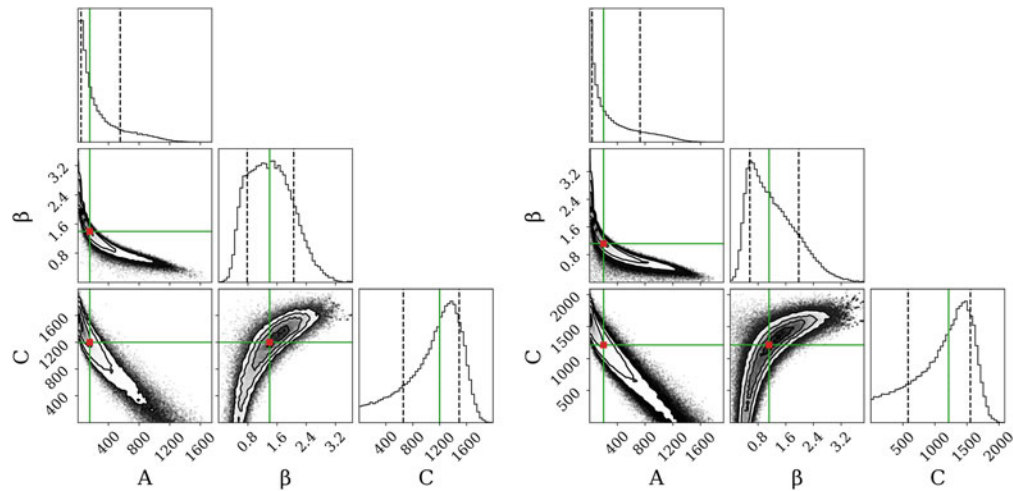


Figure B1. The panels show the posterior probability distribution of parameters A , β and C after the MCMC run for $\alpha = 352.5^\circ$ on the left and $\alpha = 353.0^\circ$ on the right. The green vertical lines in the diagonal panels show the 50th percentiles of the samples in the marginalised distributions, and two vertical black lines show the 16th and 84th percentiles.

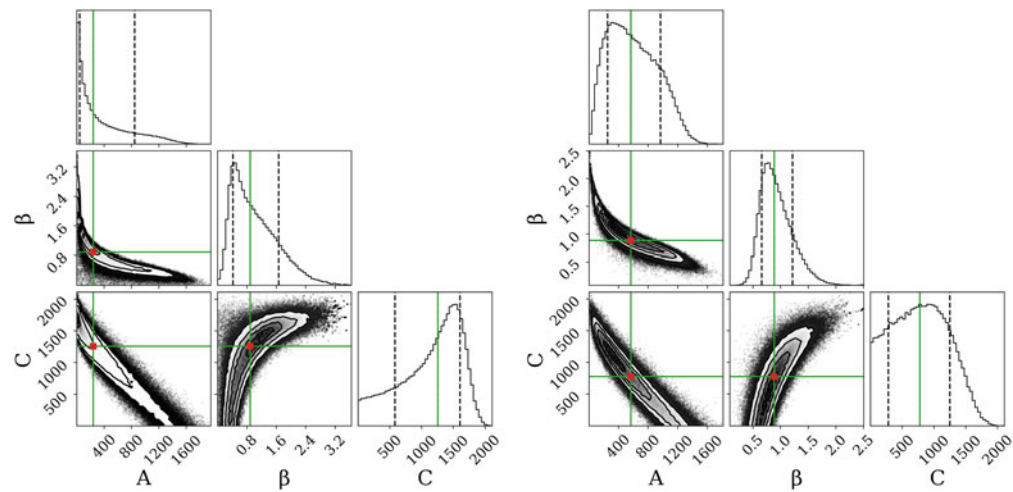


Figure B2. Same as Figure B1, with $\alpha = 357.0^\circ$ on the left and $\alpha = 1.0^\circ$ on the right.

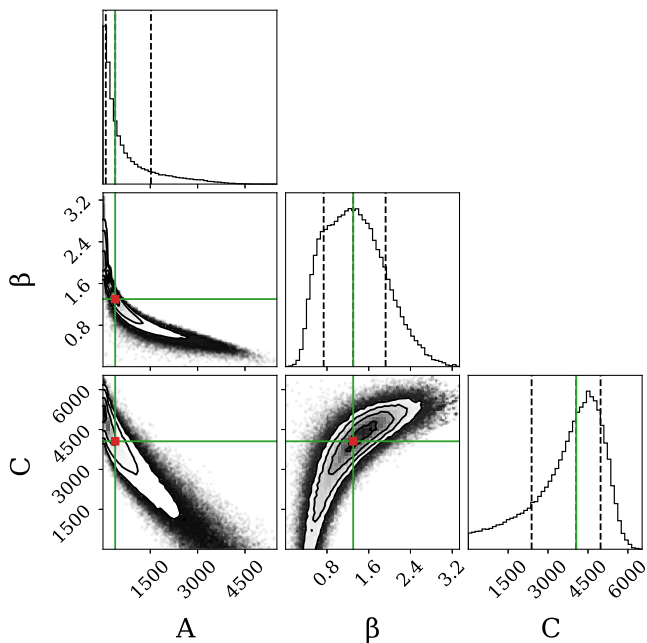


Figure B3. Same as Figure B1, with $\alpha = 4.0^\circ$.