

THE  
JOURNAL  
OF  
SYMBOLIC LOGIC

EDITED BY

ALONZO CHURCH

ERNEST NAGEL

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## ERRATA

### VOLUME 1

In *A bibliography of symbolic logic*, entries 999, 29510, and 3941, for « *Brittanica* », read « *Britannica* ».

### VOLUME 3

Page 118, line 18. For « Bd. 14 (1938) », read « Bd. 15 (1938) ».

### VOLUME 8

Page 158, first column, line 19 from the bottom. Delete the parentheses enclosing the reference VIII 81.

### VOLUME 9

Page 94, line 2. For « logic », read « logical ».

### VOLUME 10

Page 8, line 8 from the bottom. For « truth-value if », read « truth-value is ».

Page 10, lines 2 and 4. For « eleven », read « twelve ».

Page 23, next to last line. Read « Review of Cooley's *A primer of formal logic* ».

Page 28, line 14. For  $P(x, z)$ , read  $P(x \cdot z)$ .

Page 28, line 18. At the beginning of the line, for  $Pr(x, y)$ , read  $Pr(x, z)$ . And in the last denominator, for  $P(x \cdot z)$ , read  $P(z)$ .

Page 31, line 13. For  $V$ , read  $V_i$ .

Page 33, footnote 12. For  $i \rightarrow \infty$ , read  $i \rightarrow n$ .

Page 34, line 5. For  $S$ , read  $S_v$ .

Page 42, Example 6. For

$$n_1^{q_1} n_2^{q_2} n_3^{q_3} n_4^{q_4},$$

read

$$q_1^{n_1} q_2^{n_2} q_3^{n_3} q_4^{n_4}.$$