

THE  
JOURNAL  
OF  
SYMBOLIC LOGIC

EDITED BY

ALONZO CHURCH    S. C. KLEENE    ALICE A. LAZEROWITZ

*Managing Editor:* JOSHUA BARLAZ

*Consulting Editors:*

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## ERRATA

### VOLUME 13

Page 164, line 25. Delete the last  $C$  in the single axiom for the  $CN$ -calculus, and insert  $C$  immediately after the first  $w$  in the axiom.

### VOLUME 14

Page 30, line 6. For the first occurrence of  $\vee^*$ , read  $^*\vee$ .

### VOLUME 15

Page 69, line 18. For  $2\ 2\ a = a$ , read  $2\ 2\ a = 2$ .

### VOLUME 16

Page 5. Interchange lines 30 and 33.

Page 5, line 35. Before « 2.17 », insert « dual of ».

Page 147, line 15 from the bottom. The parentheses should be bold.

Page 224, lines 1 and 4. For *stoiciens*, read *stoiciens*.

Page 270, line 6 from the bottom. For  $x_2$ , read  $x_2^i$ .

Page 271, line 12 from the bottom. Before « articulate », insert « be ».

Page 283, line 18 from the bottom. For « Espasa-Calpe », read « Espasa-Calpe ».

### VOLUME 17

Page 1. In the last two lines, for « proposition », read « proposition ».

Page 4. At the end of line 5 from the bottom, replace the period by a comma.

Page 5, line 24. Delete the word « inductive ».

Page 9, line 29. For the superior  $i$ , read superior  $i_p$ .

Page 14, line 4 from the bottom. Add an asterisk at the end of the formula.

Page 15, lines 4 and 6. For  $I$ , read  $I$ .

Page 17. In line 6, insert a bold dot after  $[F_1(x_k)]$ ; in line 7, for inferior  $p_\mu$ , read inferior  $p_\nu$ ; in line 11, for inferior  $S$ , read inferior  $S$ .

Page 18, line 5. For « is void », read « is void ».

Page 19, line 3 from the bottom. Above the first  $\mathbf{II}$ , for  $P$ , read  $p$ .

Page 20, lines 3–4. Enclose in parentheses the portion of the formula beginning after  $(\exists x_p)_1^{m+1}$  and ending before the final bracket; and insert a bold dot after  $I_1(x_p)$ .

Page 21, lines 1, 3, 10, 11, 15. For  $P$ , read  $P$ .

Page 22, line 15 from the bottom. For  $F$ , read  $F$ .

Page 24. In (5), for  $P$ , read  $P$ ; above the second  $\mathbf{II}$  in line 6 from the bottom, for  $k$ , read  $l$ .

Page 57, line 12. For  $\sum_{m=1}^n$ , read  $\sum_{m=1}^{\infty}$ .

Page 57, line 15. For « have », read « has ».

Page 61, line 35. In the signature of the review, read « CHISHOLM ».

Page 66, line 20. Delete the comma before the dash.

Page 76, line 21. For « Principle », read « Principal ».

Page 77, line 8. For « D. B. McCALLUM », read « D. M. McCALLUM ».

Page 77, line 9. For « Electronics », read « Electronic ».

Page 120, line 20. At the beginning of the line, for « einen », read « ein ».

Page 121, line 14. For « gesonderen », read « besonderen ».

Page 131, line 9. The first word in the line should be: « Conceiving ».

Page 150, line 37. For « idoms », read « idioms ».

Page 160, problem 2, line 3. For « functions », read « functionals ».

Page 204. In lines 9 and 18, delete the bold dots which appear after the sign  $\supset$ .