



Scalar transport across the interface between a random sphere pack and a turbulent flow

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The transport of a passive scalar at unity Schmidt number in a turbulent flow over a random sphere pack is investigated by direct numerical simulation. A bed-normal scalar flux is introduced by prescribed scalar concentration values at the bottom and top domain boundaries, whereas sphere surfaces are impermeable to scalar fluxes. We analyse eight different cases characterised by friction Reynolds numbers $Re_{\tau} \in [150, 500]$ and permeability Reynolds numbers $Re_K \in [0.4, 2.8]$ at flow depth-to-sphere diameter ratios of $h/D \in \{3, 5, 10\}$. The dimensionless roughness heights lie within $k_s^+ \in [20, 200]$. The free-flow region is dominated by turbulent scalar transport and the effective diffusivity scales with flow depth and friction velocity. Near the interface, dispersive scalar transport and molecular diffusion gain importance, while the normalised near-interface effective diffusivity is approximately proportional to Re_K^2 . Even without a macroscopic bed topography, local hotspots of dispersive scalar transport are observed ('chimneys'), which are linked to strong spatial variations in the time-averaged scalar concentration field. The form-induced production of temporal scalar fluctuations, however, goes along with a homogenisation of those spatial variations of the scalar concentration field due to turbulent fluid motion. Accordingly, form-induced production determines the interaction of turbulent and dispersive scalar transport at the interface. With increasing Re_K , momentum from the free-flow region entrains deeper into the sediment bed, such that the form-induced production intensifies and peaks at lower positions. As a result, the transition from dispersive to turbulent scalar transport is observed deeper inside the sphere pack.

Key words: turbulent boundary layers, turbulence simulation

1. Introduction

The hyporheic zone comprises the saturated regions of the sediment bed, where the water in the pore space interacts with the stream flow via a bidirectional exchange of momentum,

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mass and energy (e.g. Boano et al. 2014; Woessner 2017). Steep biogeochemical gradients in the hyporheic zone create a unique habitat for a rich community of benthic and interstitial organisms (Brunke & Gonser 1997; Krause et al. 2017). Among the latter are many micro-organisms, which form biofilms on solid surfaces and rely on a steady supply with specific nutrients and dissolved substances, while they also depend on the removal of the end products of their metabolism (e.g. Battin et al. 2016). This microbial activity is decisive for the health of the aquatic ecosystem, it maintains different nutrient cycles and can even mitigate anthropogenic eutrophication of the water body (e.g. Harvey et al. 2013). Accordingly, mass transport processes across the sediment–water interface are of interdisciplinary interest (e.g. Krause et al. 2011; Ward 2016). Depending on the forcing mechanism, these transport processes can occur on different spatial scales, which can typically range up to tens of metres (Boano et al. 2014). In contrast to that, hyporheic transport processes can also occur on the critically smaller length scale of individual sediment grains, where primarily hydrodynamic forces tend to drive the flow (Boano et al. 2014). The transport processes on the grain-scale have high impact, as they appear over large areas and act within the region shortly below the sediment-water interface, where the ecologically most critical biota are found (Marion et al. 2014). Therefore, the present study focuses on grain-scale hyporheic scalar transport and aims to advance the mechanistic understanding of the processes involved.

The studies of Richardson & Parr (1988), Nagaoka & Ohgaki (1990) and Lai, Lo & Lin (1994) were among the first systematic investigations of mass transfer across the interface between a plane sediment bed and an overlying flow. Laboratory flume experiments were conducted to determine effective diffusivity coefficients, which were used to summarise the effects of turbulent transport, dispersive transport and molecular diffusion in the scope of a gradient-based transport model. Subsequent studies performed meta-analyses and combined different data sets to refine the prediction of an effective diffusivity, whereas different sets of input parameters were used.

O'Connor & Harvey (2008) concluded that the ratio between the effective diffusivity and the tortuosity-adapted molecular diffusivity can be approximated by the product of the roughness Reynolds number and a permeability Péclet number (with an exponent near unity). The value of this product allows the definition of four partially overlapping ranges, which are associated with transport conditions dominated by molecular diffusion, shear-induced flow, advective pumping or penetrating turbulence, respectively. After a correction of biases in the underlying data, Grant, Stewardson & Marusic (2012) applied a procedure based on multiple linear regression to isolate a small set of parameters with a high predictive power for the effective diffusivity. A resulting model uses the porosity, the permeability Reynolds number and a Reynolds number based on the bed depth as dimensionless input parameters, which appear with different exponents. In contrast to O'Connor & Harvey (2008), the roughness length remains unconsidered, which is explained by a strong correlation with other parameters. Voermans, Ghisalberti & Ivey (2018) combined insight from their own measurements (Voermans, Ghisalberti & Ivey 2017) with data points from various other experimental studies (e.g. Richardson & Parr 1988; Nagaoka & Ohgaki 1990; Packman, Salehin & Zaramella 2004; Chandler et al. 2016). On that basis, they proposed a model for the mass transport across the sediment-water interface, which predicts the ratio of effective diffusivity and molecular diffusivity only in dependency of the permeability Reynolds number and the Schmidt number. With a progressively higher permeability Reynolds number, the model describes a transition from the diffusion-dominated regime to the dispersion-dominated regime and from there to a regime dominated by turbulent scalar transport. From the observed

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scaling behaviour at the transition from the dispersion-dominated regime to the turbulent regime, Voermans *et al.* (2018) deduced that turbulent motion at the interface disrupts dispersive scalar transport. A hypothetical explanation is found in the reduction of the spatial variations in the passive scalar field due to turbulent mixing. Voermans *et al.* (2018) remarked that the permeability Reynolds number is correlated with the roughness Reynolds number, which also indicates the roughness regime. In agreement with this remark, Chen, Fytanidis & Garcia (2024) concluded that the roughness Reynolds number is the preferred input parameter to determine the interfacial effective diffusivity.

Besides the effort invested in effective diffusivity models, several studies also documented qualitative phenomena associated with hyporheic scalar transport. Packman et al. (2004) conducted experiments in a laboratory flume for both flat beds and beds with a dune-shaped surface topography. Injected dye allowed a visualisation of the scalar transport. Also in flat-bed sediments, advective flow paths in the bed-normal direction were observed. Though the concept of advective pumping had been described by Elliott & Brooks (1997) for beds with a macroscopic topography, Packman et al. (2004) hypothesised that grain-scale irregularities induce pressure head variations, which are sufficient to cause upwelling or downwelling fluid motion. In deeper regions of the sediment bed, dye was sometimes found to follow preferred flow paths, while a pulsating motion suggested an influence from the turbulent flow above the bed. Shen, Yuan & Phanikumar (2020) emphasised the impact of bed roughness on the exchange processes across the interface, while keeping Re_{K} constant. In the scope of a grain-resolved direct numerical simulation (DNS), they compared synthesised macroscopically flat beds with randomly and regularly arranged spheres at the interface against each other. The random arrangement of spheres at the interface was shown to introduce larger roughness length scales, which cause larger-scale pressure fluctuations at the interface. The resulting flow paths reach deeper into the sediment layer and increase the contribution of dispersive fluxes to the transport of mass and momentum. Thus, the irregular texture of the sediment bed surface also influences the time that an average fluid parcel resides within the sediment bed, as documented by Shen, Yuan & Phanikumar (2022).

The above overview emphasises the strong scientific interest in hyporheic scalar transport. Many studies focus on the effective scalar diffusivity and the dominant processes at the interface, whereas different models for the prediction of the interfacial effective diffusivity utilise different input parameters. In recent years, pore-resolved numerical studies have granted valuable insight into the complex and strongly three-dimensional flow field inside the sediment bed, which allowed further conclusions concerning hyporheic scalar transport processes. To our knowledge, however, no pore-resolved single-domain simulations with a wider parameter space have been conducted, which actually solve the advection–diffusion equation for a passive scalar in the context of turbulent flow over a random sphere pack. Building on v.Wenczowski & Manhart (2024), the present study closes this gap, whereas particular focus is put on the following research questions. (i) Which parameters affect the near-interface scalar transport? (ii) Which scalar transport mechanisms are dominant in different regions? (iii) How do these transport mechanisms interact with each other?

Section 2 contains the underlying equations as well as their formulation within the double-averaging analysis framework. The applied methods and the parameter space with a systematic variation of Re_{τ} and Re_{K} are introduced in § 3. In § 4, we present the main results, which are then discussed in § 5. Section 6 concludes the study.

2. Theory

The following § 2.1 contains the underlying equations. The double-averaging analysis framework is introduced in § 2.2, which allows us to discuss the double-averaged scalar transport equation in § 2.3. In § 2.4, budget equations for temporal scalar fluctuations and spatial scalar variations are formulated, which will help us later to investigate the interaction between processes.

2.1. Governing equations

Using DNS, we solve the incompressible Navier–Stokes equations for a Newtonian fluid with a kinematic viscosity ν and a density ρ . The Einstein summation notation allows us to formulate the conservation of momentum and mass as given by (2.1) and (2.2):

$$\frac{\partial u_i}{\partial x_i} = 0, \tag{2.1}$$

$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_i} = -\frac{1}{\rho} \frac{\partial p}{\partial x_i} + v \frac{\partial^2 u_i}{\partial x_i \partial x_j} + g_i.$$
(2.2)

The coordinate $x_1 \equiv x$ represents the streamwise direction, $x_2 \equiv y$ represents the spanwise direction and the coordinate $x_3 \equiv z$ specifies a vertical position above the sediment bed. The corresponding flow velocities are $u_1 \equiv u$, $u_2 \equiv v$ and $u_3 \equiv w$, respectively. Furthermore, *p* represents the pressure and g_i is a volume force acting on the fluid. The computed flow field is used in the solution of the advection–diffusion equation for a passive scalar, which reads

$$\frac{\partial c}{\partial t} + u_j \frac{\partial c}{\partial x_i} = \Gamma_c \frac{\partial^2 c}{\partial x_i \partial x_i}.$$
(2.3)

In (2.3) the variable c represents the scalar concentration and Γ_c is the corresponding scalar diffusion coefficient. As we consider a Schmidt number of $Sc = \nu/\Gamma_c = 1$, the Batchelor length scale is similar to the Kolmogorov length scale. Under steady conditions, the dimensionless form of (2.3) reduces to

$$\hat{u}_j \frac{\partial \hat{c}}{\partial \hat{x}_j} = \frac{1}{Pe} \frac{\partial^2 \hat{c}}{\partial \hat{x}_j \partial \hat{x}_j}.$$
(2.4)

In (2.4), Pe = Re Sc represents the dimensionless Péclet number, which describes the ratio between the diffusive and the advective term. If one wished to interpret the passive scalar *c* as a temperature (without buoyancy effects), Γ_c would correspond to the thermal diffusivity and the Schmidt number *Sc* would be replaced by the Prandtl number *Pr*.

2.2. Analysis framework

Double averaging in time and space provides a useful analysis framework for hyporheic scalar transport (e.g. Giménez-Curto & Lera 1996; Nikora *et al.* 2001; Mignot, Barthelemy & Hurther 2009). In a first step, the arbitrary quantity φ undergoes a Reynolds decomposition. The ensemble average in time is denoted as $\overline{\varphi}$, while φ' represents a temporal fluctuation of the quantity, such that

$$\varphi(\mathbf{x}, t) = \overline{\varphi}(\mathbf{x}) + \varphi'(\mathbf{x}, t), \quad \text{where} \quad \overline{\varphi}(\mathbf{x}) = \frac{1}{T} \int_0^T \varphi(\mathbf{x}, t) \, \mathrm{d}t.$$
 (2.5)

In the following, $\overline{\varphi}$ is further decomposed with respect to its spatial distribution. The intrinsic average within a horizontal plane is written as $\langle \overline{\varphi} \rangle$. Deviations from the in-plane



Figure 1. Diffusion problem with decomposition of the solution into intrinsic horizontal averages and spatial variations. In contrast to the actual solution, both the intrinsic averages and the spatial variations violate the zero-flux (adiabatic) Neumann boundary conditions.

average represent spatial variations and are marked by a tilde, such that

$$\overline{\varphi}(\mathbf{x}) = \langle \overline{\varphi} \rangle(z) + \widetilde{\overline{\varphi}}(\mathbf{x}), \quad \text{where} \quad \langle \overline{\varphi} \rangle(z) = \frac{1}{A_f} \iint_{A_f} \overline{\varphi}(\mathbf{x}) \, \mathrm{d}x \, \mathrm{d}y.$$
 (2.6)

The intrinsic average $\langle \overline{\varphi} \rangle$ is defined by (2.6) and results from averaging over the fluidfilled area A_f of the averaging plane at height z. In contrast, the superficial average $\langle \overline{\varphi} \rangle^s$ represents a spatial mean value with respect to the complete area A_0 of the averaging plane, such that both quantities are connected via the in-plane porosity $\theta(z)$, i.e.

$$\langle \overline{\varphi} \rangle^s(z) = \theta(z) \langle \overline{\varphi} \rangle(z), \text{ with } \theta(z) = A_f(z)/A_0.$$
 (2.7)

Below the crests of the topmost spheres of the sphere pack, the fluid-filled area A_f in the averaging plane is interrupted by solid-occupied areas. In general, however, the physical boundary conditions on the fluid-solid interface are neither fulfilled by $\langle \overline{\varphi} \rangle$ nor by $\tilde{\overline{\varphi}}$, individually. As a consequence, horizontal averaging and spatial derivatives do not simply commute and special rules apply (e.g. Giménez-Curto & Lera 1996), which gives

$$\langle \nabla \overline{\varphi} \rangle = \begin{pmatrix} \left\langle \frac{\partial \overline{\varphi}}{\partial x} \right\rangle \\ \left\langle \frac{\partial \overline{\varphi}}{\partial y} \right\rangle \\ \left\langle \frac{\partial \overline{\varphi}}{\partial z} \right\rangle \end{pmatrix} = \begin{pmatrix} \frac{1}{A_f} \oint_s \overline{\varphi} \frac{n_x}{\sqrt{n_x^2 + n_y^2}} \, ds \\ \frac{1}{A_f} \oint_s \overline{\varphi} \frac{n_y}{\sqrt{n_x^2 + n_y^2}} \, ds \\ \frac{1}{\theta} \frac{\partial \theta}{\partial z} + \frac{1}{A_f} \oint_s \overline{\varphi} \frac{n_z}{\sqrt{n_x^2 + n_y^2}} \, ds \end{pmatrix} \triangleq \begin{pmatrix} BT_1(\overline{\varphi}) \\ BT_2(\overline{\varphi}) \\ \frac{1}{\theta} \frac{\partial \theta}{\partial z} + BT_3(\overline{\varphi}) \end{pmatrix}.$$
(2.8)

In (2.8) the curve *s* represents the intersection of the averaging plane with the fluid-solid interface. The unit normal vector $\mathbf{n} = (n_x, n_y, n_z)^T$ at the solid-fluid interface points out of the fluid-filled volume. We will refer to the curve integrals as boundary terms, abbreviated by BT_i($\overline{\varphi}$). By that, we emphasise that the terms are necessary to take into account for the physical boundary conditions, which are met by $\overline{\varphi}$ and φ' , but not by $\langle \overline{\varphi} \rangle$ and $\overline{\widetilde{\varphi}}$. This issue is illustrated by figure 1 for the solution of a two-dimensional diffusion problem with adiabatic boundary conditions on curved boundaries, which enforce that $\partial \overline{\varphi} / \partial \mathbf{n} = 0$. While the field $\overline{\varphi}$ fulfills this condition, both $\langle \overline{\varphi} \rangle$ and $\overline{\widetilde{\varphi}}$ have non-zero wall-normal gradients, which would cause unphysical wall-normal diffusive fluxes of these quantities. These unphysical fluxes have opposite signs and compensate each other.

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2.3. Scalar transport processes

In view of the application, we derive the equations under the assumption that no-slip conditions apply on the surface of the sediment grains. Furthermore, we assume that no net flux in the bed-normal direction exists, i.e. $\langle \overline{w} \rangle = 0$. The surface of the sediment grains is defined to be impermeable to (diffusive) scalar fluxes, which resembles adiabatic conditions. Therefore, the superficially averaged scalar flux $\langle \overline{J} \rangle_{tot}^s$ across all horizontal planes must be constant, while contributions from different scalar transport processes can be distinguished:

$$\langle \overline{J} \rangle_{tot}^{s} = \underbrace{\theta \langle \overline{w'c'} \rangle}_{\text{turb.}} + \underbrace{\theta \langle \widetilde{\overline{w}} \, \widetilde{\overline{c}} \rangle}_{\text{disp.}} - \underbrace{\theta \left(\Gamma_{c} \frac{\partial \overline{c}}{\partial z} \right)}_{\text{diff.}} = \text{ const. for } \forall z.$$
(2.9)

The terms on the right-hand side of (2.9) represent fluxes from turbulent scalar transport, dispersive scalar transport and scalar transport due to molecular diffusion. These transport processes rely on fundamentally different mechanisms: Turbulent transport results from temporally correlated fluctuations of the bed-normal velocity and the scalar concentration. In contrast, the dispersive transport depends on spatially correlated in-plane variations of the mean velocity and the mean scalar concentration. Finally, the diffusive flux term is induced by gradients of the concentration field in the bed-normal direction.

2.4. Budget equations

As both temporal fluctuations and spatial variations of the scalar concentration field play an important role for scalar transport (see (2.9)), we consider the budget equations for both quantities:

$$\frac{\partial}{\partial t} \left\langle \frac{1}{2} \overline{c'c'} \right\rangle = \underbrace{\left[-\left\langle \overline{w'c'} \right\rangle \frac{\partial \langle \overline{c} \rangle}{\partial z} \right]}_{\text{prod.}} - \left\langle \overline{u'_jc'} \frac{\partial \overline{c}}{\partial x_j} \right\rangle}_{\text{prod.}} - \Gamma_c \left\langle \frac{\partial c'}{\partial x_j} \frac{\partial c'}{\partial x_j} \right\rangle}_{\text{diss.}} + \frac{1}{\theta} \frac{\partial}{\partial z} \left(\underbrace{-\frac{\theta}{\overline{w}} \frac{\langle \overline{w}}{c'c'} \rangle}_{\text{adv. transp.}} - \underbrace{-\frac{\theta}{\overline{w}} \frac{\langle \overline{w'c'c'} \rangle}{2}}_{\text{turb. transp.}} + \underbrace{-\frac{\theta}{\overline{w}} \frac{\langle \overline{c} \frac{\partial \overline{c'c'}}{\partial z} \rangle}{2}}_{\text{diff. transp.}} \right)_{\text{diff. transp.}}$$
(2.10)
$$\frac{\partial}{\partial t} \left\langle \frac{1}{2} \overline{c} \overline{c} \right\rangle = \underbrace{\left[-\left\langle \overline{w} \overline{c} \right\rangle \frac{\partial \langle \overline{c} \rangle}{\partial z} \right]}_{\text{prod.}} + \underbrace{\left\{ \frac{u_j c'}{\partial x_j} \frac{\partial \overline{c}}{\partial x_j} \right\}}_{\text{diss.}} - \Gamma_c \left\langle \frac{\partial \overline{c}}{\partial x_j} \frac{\partial \overline{c}}{\partial x_j} \right\rangle}_{\text{diss.}} + \frac{1}{\theta} \frac{\partial}{\partial z} \left(\underbrace{-\frac{\theta}{\overline{w}} \overline{c} \overline{c} \\ -\frac{2}{2}}_{\text{adv. transp.}} - \frac{\theta}{\overline{w}} \left\langle \overline{w'c'} \overline{c} \\ + \frac{\theta}{\overline{w}} \left\langle \overline{c} \\ \frac{\partial \overline{c}}{\partial x_j} \right\rangle}_{\text{diss.}} \right) + \underbrace{\operatorname{BT}_j \left(\frac{1}{2} \Gamma_c \frac{\partial \overline{c} \overline{c} \\ \partial \overline{x}_j } \right)}_{\text{boundary}} + (2.11)$$

A comparison of (2.10) and (2.11) shows similar patterns in the formulation of both budgets, which contain a production term, a dissipation term, as well as terms for

advective, turbulent and diffusive transport. The production part of the budgets is further subdivided: the term in the dashed box leads to a positive production of $\langle \overline{c'c'} \rangle$ or $\langle \overline{c} \ \overline{c} \rangle$, if turbulent or dispersive scalar transport, respectively, acts against the gradient of the double-averaged scalar concentration field. Accordingly, we will refer to these terms as turbulent or dispersive gradient production, respectively. The terms in the solid boxes appear with opposite signs in the budget equations and, therefore, represents a transfer mechanism between temporal fluctuations and spatial variations. Temporal scalar fluctuations $\langle \overline{c'c'} \rangle$ are generated at the expense of spatial scalar variations $\langle \overline{c} \, \overline{c} \rangle$, if turbulent scalar transport takes place against the gradient of the scalar variation, thus homogenizing the in-plane scalar field. In smooth-wall channel flow, \overline{c} has zero value, such that only the presence of a characteristic geometry renders the production mechanism relevant. Therefore, the mechanism is referred to as form-induced production of temporal scalar fluctuations. Besides the already discussed terms, (2.11) contains a boundary term. This term arises as both $\langle \overline{c} \rangle$ and \overline{c} violate the boundary condition by inducing non-zero diffusive fluxes of opposite signs across the zero-flux boundary. Formally, the boundary term represents a redistribution of $\overline{c} \,\overline{c}$ between $\langle \overline{c} \rangle \langle \overline{c} \rangle$ and $\langle \overline{c} \,\overline{c} \rangle$ by means of these fluxes across the boundary. The role of the boundary term is highlighted by the diffusion problem in figure 1, in which the Neumann boundary condition on the inclined walls acts as the only source of spatial variations under zero-velocity conditions.

3. Methods

The case configuration is described in § 3.1 and the representation of the porous medium in § 3.2. The parameter space is introduced in § 3.3, before we discuss the interface definition in § 3.4. Section 3.5 focuses on the numerical methods, and a convergence study follows in § 3.6. Some aspects of this section are described in greater detail in v.Wenczowski & Manhart (2024), where we validated the flow field.

3.1. Case configuration

In the scope of a single-domain DNS, we investigate turbulent open-channel flow over a mono-disperse random sphere pack. This configuration resembles the flow in a gravel-bed river, as the sphere pack imitates the sediment bed and individual spheres act as sediment grains. As sketched in figure 2, the top boundary of the domain is a rigid lid with a freeslip boundary condition, which approximates the free water surface. A constant volume force in the streamwise direction, i.e. $g_x > 0$, acts on the fluid and drives the flow. The domain has periodic domain boundary conditions in the streamwise x-direction and lateral y-direction. The simulation statistics are gathered in a statistically stationary state, where the boundary layer is fully developed and the boundary layer thickness δ equals the flow depth h. During the flow simulation, the spheres with diameter D remain in fixed positions and no-slip boundary conditions apply on the sphere surfaces. The bottom boundary of the domain cuts through the sphere pack. A free-slip condition reduces the influence of the bottom domain boundary, as it ensures that streamwise momentum is only absorbed by the spheres and not by the domain boundary. Dirichlet boundary conditions prescribe fixed scalar concentration values c_{bot} and c_{top} at the bottom and top domain boundary, respectively. The concentration difference $\Delta c = c_{top} - c_{bot}$ induces a scalar flux in the bed-normal direction. The surfaces of the spheres are impermeable to scalar fluxes, which is equivalent to adiabatic conditions in heat transport. In the absence of any scalar sinks or sources, the superficially double-averaged scalar flux is constant at all vertical positions z within the domain (see (2.9)).



Figure 2. Sketch of case configuration. The bed-normal scalar flux is induced by fixed scalar values at the bottom and top of the domain. Dispersive transport due to mean flow paths through the sediment (a), diffusive transport due to scalar concentration gradients (b) and turbulent transport due to turbulent fluid motion (c) contribute to the scalar flux.



Figure 3. Properties of a sediment bed with $A_0 = 64D \times 32D$. (a) In-plane porosity profile with the geometric interface z = 0 defined by $\frac{\partial^2 \theta}{\partial z^2} = 0$. (b) Spatial autocorrelation of the bed elevation fluctuation \tilde{z}_b over the horizontal shift r.

3.2. Representation of the porous medium

In preparation for the flow simulations, mono-disperse random sphere packs of different extents were generated, as described in v.Wenczowski & Manhart (2024). The generated sphere packs have a level mean bed surface, as we do not consider bed forms like, e.g. riffles or dunes. The in-plane porosity profile $\theta(z)$ of a sphere pack with a base area of $A_0 = 64D \times 32D$ is shown in figure 3(*a*). Like Voermans *et al.* (2017), we use the inflection point $\partial^2 \theta / \partial z^2 = 0$ of the porosity profile as a geometrically defined interface position. The distance between the geometrically determined interface and the top boundary of the domain defines the nominal flow depth *h* of the case. For all simulated cases, the sediment bed has a depth of 5 *D*. At each location, the bed elevation $z_b(x, y)$ is defined as the topmost point, where a vertical line at this location would intersect a sphere surface. The derived variable \tilde{z}_b represents the spatial autocorrelation of the bed elevation field around its mean value. Figure 3(*b*) shows the spatial autocorrelation over the distance *r* confirms that no repeating large-scale patterns prevail in the bed surface.

3.3. Parameter space

The parameter space of the present study is described in terms of the friction Reynolds number Re_{τ} and permeability Reynolds number Re_K . The friction Reynolds number $Re_{\tau} = u_{\tau}h/v$ characterises the unconfined flow above the sediment layer, where



Figure 4. Simulated cases as sampling points within a dimensionless parameter space, including reference points from literature. The grey dashed lines represent fixed ratios between the flow depth h and the sphere diameter D. The reference points refer to Breugem *et al.* (2006), Voermans *et al.* (2017), Shen *et al.* (2020) and Karra *et al.* (2023). Figure adapted from v.Wenczowski & Manhart (2024).

similarities to smooth-wall open-channel flow prevail. The available computing power limited the Reynolds number to $Re_{\tau} < 500$. The permeability Reynolds number $Re_K = u_{\tau}\sqrt{K}/v$ uses the square root of the permeability as an effective length scale of the pore space (Breugem, Boersma & Uittenbogaard 2006). By putting \sqrt{K} in relation to the viscous length scale $\delta_{\tau} = v/u_{\tau}$, Re_K gives an indication whether the smallest-scale turbulent motion can penetrate the pore space or not. Therefore, $Re_K \ll 1$ and $Re_K \gg 1$ represent effectively impermeable and highly permeable regimes, respectively. Values of $Re_K \approx 1 - 2$ mark the transition between both extremes (Voermans *et al.* 2017). The cases are characterised by different ratios of the flow depth to the sphere diameter, i.e. h/D, which allows different combinations of Re_{τ} and Re_K , as shown in figure 4. Besides the Reynolds numbers, table 1 summarises further nominal parameters of the simulated flow cases. We use the term nominal parameters to indicate that those parameters refer to the *a priori* geometrically defined flow depth *h* and the friction velocity $u_{\tau} = \sqrt{g_x h}$.

While the transport of gases in air is described by Sc = O(1), the transport of dissolved substances in water is usually characterised by critically higher Schmidt numbers of $Sc = O(10^3)$. Still, we consider a unitary Schmidt number ideal for the present study, as it will allow us to observe both diffusion- and advection-dominated hyporheic regimes within the range of $Re_K \in [0.4, 2.8]$. From a practical perspective, the choice of Sc = 1 allows us to keep control of the required grid resolution, while the comparatively short diffusive time scale reduces the amount of simulated time until a steady state is reached.

3.4. Interface position

The geometrically defined interface is determined from the porosity profile of the sphere pack, such that this interface is available during the configuration phase of the simulations, while it lacks flow-dynamical motivation. To discuss the scalar transport across the interface between a porous medium and a free turbulent flow and to find similarities, a flow-dynamically meaningful interface definition is required, which can be obtained *a posteriori* from the simulation results. As described in v.Wenczowski & Manhart (2024) in greater detail, we computed the superficially double-averaged drag distribution $f_{(p+v)}^s$

Symbol	Case	h/D	$L_x/h \times L_y/h$	$\Delta x^+_{i,min}$	$\Delta x_{i,max}^+$	Re_{τ}	Re_K	Re_p
	L-180	3	13.3×6.7	1.21	1.21	174	1.63	0.95
-8	L-300	3	13.3×6.7	1.04	2.08	300	2.82	2.77
	M-150	5	12.8×6.4	0.63	2.52	154	0.87	0.15
<u> </u>	M-300	5	12.8×6.4	0.63	2.52	300	1.69	0.59
▼	M-500	5	12.8×6.4	1.04	4.16	500	2.82	1.60
—	S-150	10	12.8×6.4	0.31	1.24	150	0.42	0.02
—	S-300	10	12.8×6.4	0.63	2.52	300	0.84	0.07
	S-500	10	12.8×6.4	1.04	4.16	500	1.40	0.20
	I-180	$\rightarrow \infty$	13.3×6.7	0.63	1.26	180	0	0
	I-300	$\rightarrow \infty$	12.8×6.4	0.75	3.00	300	0	0
	I-500	$\rightarrow \infty$	12.8×6.4	0.90	3.60	500	0	0

Table 1. Overview of nominal case parameters. The variable *h* represents the flow depth above the geometrically defined interface, *D* is the sphere diameter, *L* is the extent of the domain, $\Delta x_{i,min}^+$ describes the side length of the smallest cubic cells near the interface and $\Delta x_{i,max}^+$ the side length of the largest cells in the free-flow region. The friction, permeability and particle Reynolds numbers are defined as $Re_{\tau} = u_{\tau}h/v$, $Re_K = u_{\tau}\sqrt{K}/v$, $Re_p = \langle \overline{u} \rangle^s D/v$, respectively, where $u_{\tau} = \sqrt{g_x h}$ is the friction velocity, *K* the permeability and *v* the kinematic viscosity.

on the porous medium via the relation

$$f^{s}_{(p+\nu)} = \frac{\partial}{\partial z} \left(-\theta \left(\nu \frac{\partial \overline{u}}{\partial z} \right) + \theta \left\langle \widetilde{\overline{u}} \, \widetilde{\overline{w}} \right\rangle + \theta \left\langle \overline{u'w'} \right\rangle \right) - \theta \, g_x. \tag{3.1}$$

The expression in (3.1) results from the double-averaged Navier–Stokes equation (e.g. Nikora *et al.* 2001), while we summarise both viscous and pressure drag in $f_{(p+\nu)}^s$. The obtained drag distribution exhibits a characteristic peak near the sediment–water interface, which can be associated with the absorption of incoming momentum from the free-flow region. Inspired by the idea of Thom (1971) and Jackson (1981), we apply a curve fitting approach to characterise the free-flow momentum absorption peak by few parameters and to distinguish it from the Darcy drag, which is exerted by the porous media flow independently of the free flow above. In our fitting function, a Gaussian normal distribution is used to parametrise the free-flow momentum absorption peak, while a complementary error function ensures that the Darcy drag is only accounted for below the interface. Both terms of our fitting function $f(z, \mu_z, \sigma_z)$ share the mean position μ_z and spread σ_z as fitting parameters, such that

$$f(z, \mu_z, \sigma_z) = \underbrace{(u_\tau^{\mu})^2 \cdot \left(\frac{1}{\sigma_z \sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{z-\mu_z}{\sigma_z}\right)^2}\right)}_{\text{Free-flow momentum absorption}} + \underbrace{\theta_{por} g_x \cdot \left(\frac{1}{2} \operatorname{erfc}\left(\frac{z-\mu_z}{\sqrt{2\sigma_z}}\right)\right)}_{\text{Darcy drag absorption}}.$$
 (3.2)

With $(u_{\tau}^{\mu})^2 = g_x(h - \mu_z)$, the formulation of the first term in (3.2) ensures that all momentum introduced by the source term g_x between the free surface and the mean position μ_z is absorbed. Accordingly, u_{τ}^{μ} is the consistent friction velocity for the interface-adapted flow depth $h^{\mu} = (h - \mu_z)$. The second term in (3.2) represents the absorbed Darcy drag, which is computed from an equilibrium with the volume forces acting on the fluid in the pore space of the porous medium, which has a bulk porosity of value $\theta_{por} = 0.385$.

For each simulated case, a nonlinear least-square fit of $f(z, \mu_z, \sigma_z)$ to the actual drag distribution $f_{(p+\nu)}^s$ yields case-specific values for the fitting parameters μ_z and σ_z , which are listed in table 2. Figure 5 shows that the fitted function achieves a good approximation

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Case	μ_z/D	σ_z/D	h^{μ}/h	$Re^{\mu}_{ au}$	Re_K^{μ}	λ	k_s^+
L-180	0.141	0.272	0.953	162	1.59	0.159	131
L-300	0.093	0.283	0.969	286	2.78	0.161	204
M-150	0.215	0.276	0.957	144	0.85	0.111	59
M-300	0.143	0.290	0.971	286	1.67	0.119	126
M-500	0.096	0.303	0.981	482	2.79	0.118	202
S-150	0.257	0.271	0.974	143	0.41	0.060	16
S-300	0.202	0.273	0.980	289	0.83	0.074	50
S-500	0.151	0.287	0.985	489	1.39	0.079	95
I-180	_	_	1.000	174	0.00	0.033	0
I-300	_	_	1.000	300	0.00	0.028	0
I-500	_	_	1.000	500	0.00	0.024	0

Table 2. Parameters of the drag-based interface as well as interface-adapted flow depth and Reynolds numbers. The parameters μ_z and σ_z specify a mean interface position and an interfacial length scale, respectively. The interface-adapted flow depth is defined as $h^{\mu} = h - \mu_z$, where *h* is the nominal flow depth. The interface-adapted Reynolds numbers are defined as $Re_{\tau}^{\tau} = u_{\tau}^{\mu}h^{\mu}/\nu$ and $Re_K = u_{\tau}^{\tau}\sqrt{K}/\nu$, respectively, where $u_{\tau}^{\mu} = \sqrt{g_x h^{\mu}}$ is the interface-adapted friction velocity. The Darcy–Weisbach friction factor λ and the equivalent sand roughness k_s were determined as described in v.Wenczowski & Manhart (2024). The variable *D* represents the sphere diameter.



Figure 5. Distribution of the superficially double-averaged drag on the sediment bed. The coloured curves with symbols represent the drag-distribution obtained from the simulation (see (3.1)), while the dashed black lines represent the approximation by the fitting function using the case-specific fitting parameters μ_z and σ_z (see (3.2)). Each of the three plots summarises simulation cases with an equal h/D ratio. The sphere diameter D and the shear velocity u_τ are used for normalisation. Figure adapted from v.Wenczowski & Manhart (2024).

of the drag distribution. The obtained parameter μ_z represents the centroid of the freeflow momentum absorption peak, and is thus interpreted as the mean interface position. The spread σ_z of the drag peak was used as a proxy for an interfacial length scale.

While the nominal parameters of the simulation cases in table 1 refer to the geometrically defined interface, table 2 provides the interface-adapted flow depths and Reynolds numbers. For the computation of the interface-adapted Reynolds numbers, a consistent friction velocity is used, which is obtained as $u_{\tau}^{\mu} = \sqrt{g_x h^{\mu}}$. Whereas the

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Reynolds numbers of cases with smooth impermeable walls do not change, it is worthwhile to note that $Re_{\tau}^{\mu} < Re_{\tau}$ and $Re_{K}^{\mu} < Re_{K}$ for cases with rough and permeable surfaces.

In the following, the vertical position is either specified in terms of z/D or z/h, where z refers to the geometrically defined interface. Alternatively to z/h, we use the interfaceadapted coordinate $\zeta = (z - \mu_z)/(h - \mu_z)$ for orientation in the free-flow region, where $\zeta = 0$ coincides with the drag-based interface and $\zeta = 1$ with the free-slip water surface.

In v.Wenczowski & Manhart (2024), we demonstrated that the flow-dynamically motivated drag-based interface and the adapted parameters allow us to unravel several similarities in the flow field, which we could not see clearly within the framework of the geometric interface. Particularly in advection-dominated regions, it appears unlikely to find potential similarities in the scalar field if there are no similarities in the flow field, such that we resort to the drag-based interface whenever we aim to investigate similarities. While we will employ the drag-based interface framework in parts where similarities are addressed, other paragraphs can be presented more conveniently with respect to the geometric interface.

3.5. Numerical methods

To resolve all temporal and spatial scales both in the free-flow region and in the pores of the sphere pack, we follow a single-domain DNS approach, which avoids model assumptions. The simulations were conducted by means of our MPI-parallel in-house code MGLET (Manhart, Tremblay & Friedrich 2001; Manhart 2004; Sakai et al. 2019), which solves the incompressible Navier-Stokes equations using an energy-conserving central second-order finite-volume method. MGLET resorts to an explicit third-order low-storage Runge-Kutta method (Williamson 1980) for the time integration. Local grid refinement was applied to ensure that the Kolmogorov and Batchelor scales are resolved within the complete domain. The highest spatial resolution is required near the surface of the sediment bed, where we use cubic cells with a side length of $\Delta x_i^+ \lesssim 1$ (see table 1). Within the porous medium, a resolution of 48 cells per sphere diameter was found to yield a good resolution of the pore space (v.Wenczowski & Manhart 2024). The geometry of the sphere pack is represented by an immersed boundary method. The no-slip Dirichlet condition on the sphere surfaces is enforced by a ghost-cell approach, which reaches second-order spatial accuracy for the velocity field, while mass conservation is ensured (Peller et al. 2006; Peller 2010). The zero-flux Neumann boundary condition for the scalar reaches first-order spatial accuracy at the immersed boundary. By its construction, the implementation ensures strict conservation of the scalar within the complex geometry, such that we tolerate the reduced order in comparison to the velocity field. Commonly used spatial discretisation methods fail to resolve the infinitesimally narrow fluid gap at the contact points between spheres (Finn & Apte 2013; Unglehrt & Manhart 2022). To achieve a convergence against a defined geometry, we insert small fillet bridges, which seal regions where the sphere surfaces are extremely close to each other (v.Wenczowski & Manhart 2024). We acknowledge that the contact points influence the mixing processes on the microscale (e.g. Heyman et al. 2020), but, as errors cannot be completely avoided, it appears preferable to commit a quantifiable error, which is independent of the grid resolution.

3.6. Convergence study

A case-specific grid study of the turbulent velocity field is documented in v.Wenczowski & Manhart (2024). This allows us to focus on the grid convergence of scalar profiles and the scalar transport processes, whereas turbulent and dispersive transport implicitly reflect the influence of the velocity field. The grid study is carried out on case L-180,

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Figure 6. Grid study for case L-180. The scalar concentration profile (*a*) and the relative contributions of different transport processes to the total scalar flux (b-d) are evaluated for different grids with cubic cells of side length Δx . The side length Δx is normalised by the sphere diameter *D*. A resolution of $D/\Delta x = 48$ corresponds to $\Delta x_i^+ = 1.21$.



Figure 7. Statistical convergence study for case L-180. Besides the scalar concentration profile (*a*), relative contributions of different transport processes to the total scalar flux (b-d) are evaluated after different statistical sampling time spans T_s . The sampling time span is normalised by the friction velocity u_τ and the flow depth *h*.

which is the computationally cheapest simulation. Spatial resolutions with 16, 24, 32 and 48 cells per sphere diameter D are compared. Figure 6 shows that the grid dependence is largest in deeper sediment layers, where insufficiently resolved configurations tend to underpredict diffusive scalar transport, while overpredicting the relative importance of dispersive transport.

In the flow case under consideration, the molecular scalar diffusion in the sediment bed is characterised by the largest time scale, which makes it the 'slowest' among all physical processes involved. Accordingly, the scalar field also requires more simulated time to reach a statistically stationary state than the velocity field. Due to that, the sampling of quantities related to scalar transport was only initiated a while after the sampling of velocity data had started. As a result, the scalar statistics were gathered over $T_s u_b/L_x > 10$, which corresponds to $T_s u_{\tau}/h > 13$. Thus, the scalar sampling time period T_s is about half as long as the sampling period T of the velocity field (v.Wenczowski & Manhart 2024). Using case L-180 as an example, the statistical convergence study in figure 7 shows a fast statistical convergence in the near-interface region, where turbulent motion on smaller length scales and shorter time scales is expected. In comparison, absolute statistical convergence in the free-flow region requires longer statistical sampling periods, whereas the time span T_s appears to be just sufficient for the convergence of second-order statistics.

4. Results

The following § 4.1 provides an overview of the scalar concentration profiles under different normalisation. Similarities in the free-flow region scalar concentration profile (§ 4.2) can be traced back to a similarity in the effective diffusivity, as shown in § 4.3. Section 4.4 presents the dominant processes within different regions. Local hotspots of different transport processes are identified in § 4.5. Finally, § 4.6 focuses on the near-interface interaction between dispersive and turbulent transport.

4.1. Double-averaged scalar concentration profiles

The three plots in figure 8 show the intrinsically double-averaged scalar concentration $\langle \overline{c} \rangle$ under different normalisations. In figure 8(a) the concentration profile is normalised by the concentration difference $\Delta c = c_{top} - c_{bot}$. Accordingly, the obtained curves show a zero value at the bottom boundary and increase monotonically, until they reach a value of unity at the top domain boundary. The vertical coordinate z is normalised by the sphere diameter D. Whilst all domains have the same depth of 5 D, the top domain boundary is found at different heights in terms of z/D. The gradient of the double-averaged concentration profile differs drastically between the free-flow region and the sediment bed. In the freeflow region a small gradient $\partial \langle \overline{c} \rangle / \partial z$ suffices to maintain the bed-normal scalar flux, which hints at a high effective conductivity in this region. Within the sediment bed, a critically steeper concentration gradient indicates that the vertical scalar flux encounters a high resistance. For cases with low Re_K , the profiles are approximately linear in the region of z/D < 0, whereas increasing values of Re_K lead to a progressively stronger curvature in the profiles below the interface, which points at a variation of the effective conductivity over the depth of the sediment bed. In figure 8(b) the vertical coordinate z is normalised by the flow depth h, which allows us to include the cases with smooth and impermeably bottom boundaries. Under normalisation with Δc , the concentration profiles deviate considerably from each other, as the scalar concentration at the geometrically defined interface at z/D = 0 differs between the cases. This observation motivates the normalisation applied in figure 8(c), where the concentration at z = 0 acts as a reference. Under this normalisation, the profiles in the free-flow region have a similar shape, though they still do not collapse.

4.2. Similarities in the free-flow region

To explore similarities in the free-flow scalar concentration profiles among all simulated cases, we resort to the dimensionless quantity $\langle \overline{c} \rangle^+$, which is defined as

$$\langle \overline{c} \rangle^+ = \frac{\langle \overline{c} \rangle}{c_\tau}, \quad \text{with} \quad c_\tau = \frac{\langle J \rangle_{tot}^s}{u_\tau^\mu} \quad \text{and} \quad u_\tau^\mu = \sqrt{g_x h^\mu}.$$
 (4.1)

The variable c_{τ} in (4.1) represents the friction scalar concentration (in analogy to the friction temperature), which is computed from the superficially double-averaged total scalar flux $\langle \overline{J} \rangle_{tot}^s$ in the bed-normal direction and the friction velocity u_{τ}^{μ} . The friction velocity is obtained via a balance between the driving volume force and the wall friction, which includes the interface-adapted flow depth h^{μ} (see (4.1)). In figure 9 the scalar concentration profiles are shown in a defect form, which exploits the prescribed fixed



Figure 8. Double-averaged scalar concentration profiles under different normalisations. (a) Scalar concentration normalised by the concentration difference between the bottom and top of the domain, i.e. $\Delta c = c_{top} - c_{bot}$, and coordinate z normalised by the sphere diameter D, such that the top domain boundary is found at z/D = 3, z/D = 5 or z/D = 10 for L, M and S cases, respectively. (b) Normalisation of concentration profile like (a), but z normalised by the flow depth h. Accordingly, the bottom domain boundary is found at z/h = -1.67, z/h = -1 or z/h = -0.5 for L, M and S cases, respectively. (c) Concentration profile normalised by $c_{top} - \langle \overline{c} \rangle_{(z=0)}$, whereas the double-averaged concentration at z = 0 is a reference. The coordinate z is normalised by h.



Figure 9. Defect representation of the dimensionless double-averaged concentration field. The concentration c_{top} is prescribed at the top domain boundary. The dimensionless vertical coordinate ζ accounts for the drag-based interface position μ_z .



Figure 10. Effective scalar diffusivity profile in the free-flow region. The effective diffusivity Γ_{eff} is normalised by the molecular diffusivity Γ_c . The dimensionless vertical coordinate ζ accounts for the drag-based interface position μ_z .

concentration value c_{top} at the clearly defined top domain boundary. The distance above the sediment is given relative to the flow depth under consideration of the interface position at $z = \mu_z$. Above a certain distance from the bed surface, the dimensionless scalar defect profiles for cases with similar Re_τ collapse well, indicating an outer-layer similarity of the scalar field.

4.3. Effective diffusivity

The observed similarity under consideration of the total scalar flux also hints at a similarity of the effective scalar diffusivity among cases with similar Re_{τ} . Therefore, figure 10 provides profiles of the effective diffusivity, which is set in relation to the molecular diffusivity of the scalar. This ratio of Γ_{eff}/Γ_c can be interpreted as a local Sherwood number for a differentially thin slice at a certain z position. Near the sediment-water interface, the profiles appear to group roughly according to the nominal permeability Reynolds numbers, as high values of Re_K are correlated with higher values of Γ_{eff}/Γ_c . In the free-flow region the expected grouping according to Re_{τ} is recognisable, whilst differences become most visible in the peak values around $\zeta \approx 0.5$.

To investigate the scaling behaviour in detail, figure 11(*a*) shows the effective diffusivity at the drag-based interface as a multiple of the molecular scalar diffusivity. The values are plotted over the interface-adapted permeability Reynolds number Re_K^{μ} . In addition, the dashed reference line represents the values predicted by the model of



Figure 11. Scaling of the effective diffusivity Γ_{eff} at the drag-based interface at $\zeta = 0$, i.e. $z = \mu_z$, and in the centre of the free-flow region, i.e. $\zeta = 0.5$. The effective diffusivity is normalised by the molecular scalar diffusivity Γ_c . The adapted Reynolds numbers Re_{τ}^{μ} and Re_{τ}^{μ} account for the drag-based interface. In (*a*) the relation according to Voermans *et al.* (2018) is given as a reference (dashed line). This relation includes a transition from a 'dispersive' to a 'turbulent' regime at $Re_K \approx 1$, which is marked in grey.

Voermans *et al.* (2018). The model provides separate expressions for the dispersive regime $(Re_K < 1)$ and the turbulent regime $(Re_K > 1)$, which we evaluate for Sc = 1. Whereas the model prediction captures the macroscopic trend reasonably well, it underpredicts the numerically obtained effective diffusivity for low Re_K . According to the model of Voermans *et al.* (2018), the diffusive regime with $\Gamma_{eff}/\Gamma_c = 1$ is only reached for $Re_K < 0.02$. In contrast to that, our data points suggest that $\Gamma_{eff}/\Gamma_c \approx 1$ is already observed for case S-150. As discussed later in § 5, this observation can be linked to different Schmidt numbers. Figure 11(*b*) shows the scaling behaviour of the effective diffusivity in the centre of the free-flow region, i.e. at $\zeta = 0.5$. The value of Γ_{eff}/Γ_c increases linearly with respect to the interface-adapted friction Reynolds number $Re_{\tau}^{\mu} = u_{\tau}^{\mu}h^{\mu}/\nu$. From that, one can deduce that $\Gamma_{eff}(\eta = 0.5) \approx 0.1 u_{\tau}^{\mu} h^{\mu}$, which means that the effective diffusivity in the free-flow region scales with the same interface-adapted velocity and length scales as the velocity field (v.Wenczowski & Manhart 2024).

For modelling, the turbulent Schmidt number $Sc_t = v_t/\Gamma_t$ is a relevant parameter, as it represents the ratio between turbulent effective viscosity $v_t = \langle \overline{u'w'} \rangle / \langle \partial \overline{u} / \partial z \rangle$ and the turbulent effective diffusivity $\Gamma_t = \langle \overline{c'w'} \rangle / \langle \partial \overline{c} / \partial z \rangle$. As shown in figure 12, the turbulent Schmidt number has a nearly constant value of slightly less than unity over large parts of the free-flow region, which agrees with previous studies (e.g. Schwertfirm & Manhart 2007; Pirozzoli, Bernardini & Orlandi 2016). However, Sc_t deviates considerably from unity in regions influenced by the boundary conditions that are of different types for the scalar and the velocity field. In the region directly below the crests of the topmost spheres, i.e. near 0.5 < z/D < 1.0, the turbulent Schmidt number decreases. For the cases with high Re_K , it drops as low as $Sc_{t,min} \approx 0.55$, which qualitatively agrees with the findings of Chandesris *et al.* (2013), who considered a critically more porous bed with $\theta = 0.875$.

4.4. Scalar transport processes

The previous section has shown that the effective diffusivity of the scalar exceeds the molecular diffusivity by far, which implies that other non-Fickian transport processes



Figure 12. Turbulent Schmidt number Sc_t within the free-flow region. The dimensionless vertical coordinate ζ accounts for the drag-based interface position μ_z .

contribute greatly to the total scalar flux $\langle \overline{J} \rangle_{tot}$. For each case separately, the plots in figure 13 show the relative contributions of turbulent, dispersive and diffusive transport to the total bed-normal scalar flux as a function of z. At the free-slip top boundary of the domain, a thin layer exists where only diffusive scalar transport takes place in the absence of surface-normal fluid motion. Away from this diffusion-dominated layer, turbulent transport is dominant throughout the free-flow region. Around the position of $z \approx 0$, however, the influence of turbulent transport declines drastically with decreasing z, while diffusive and dispersive quickly gain relevance. For the simulated cases with unity Schmidt number, the permeability Reynolds number seems to determine whether diffusive or dispersive transport is dominant. Only for case S-150 with $Re_K \approx 0.4$, diffusive transport dominates over dispersive transport within the complete sediment bed. For $Re_K \approx 0.8$ (e.g. cases M-150 and S-300), the contributions of both processes are approximately equal within the region directly below the sediment bed surface. With increasing Re_K , dispersive transport finally dominates in the layer shortly below the sediment surface. Deeper inside the sediment bed, the contribution of dispersive transport fades out to the benefit of diffusive transport. Finally, diffusive transport is once again exclusively responsible for the scalar flux across the bottom domain boundary.

The plots in figure 13 visualise that the decline of turbulent scalar transport and the increase in dispersive transport with decreasing z happen within a relatively narrow region near the interface. Within this narrow region, the bed-normal scalar transport due to molecular diffusion reaches a local maximum, hinting at the presence of higher vertical concentration gradients. The elevation $z_{(turb=disp)}$, at which the contributions of turbulent and dispersive transport are equally large, coincides fairly well with the position of the drag-based interface, which is found at $z = \mu_z$. As shown by figure 14, both $z_{(turb=disp)}$ and μ_z decrease with increasing Re_K , such that both approach the position of the geometrically defined interface. The grey dashed line is the same in both plots and provides a reference.

Figure 15 focuses on the near-interface region and compares all simulated cases. The grouping of curves corroborates the concept of Voermans *et al.* (2018), according to which Re_K determines the dominant scalar transport processes. With increasing Re_K , turbulent scalar transport can affect progressively deeper regions of the sediment bed.

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Figure 13. Relative contribution of different scalar transport processes to the total superficially averaged scalar flux $\langle \overline{J} \rangle_{tot}^s$ in the bed-normal direction. The dotted lines indicate the geometrically defined interface at z = 0, whereas the dashed lines mark the drag-based interface position $z = \mu_z$ for each case.

Deeper below the interface, however, the contribution of turbulent scalar transport tails out. This observation is contrasted by the dispersive transport, which gains maximal influence in the near-interface region and only decreases gradually in deeper regions. At the largest Re_K of our parameter space, nearly the complete scalar transport at $z/D \approx -1$ is leveraged by dispersive transport. As the contributions of dispersive and turbulent transport increase at the interface, the relative share of transport due to molecular diffusion decreases at progressively higher Re_K .



Figure 14. Transition between turbulent and dispersive transport at the interface. The position $z_{(turb=disp)}$ marks where the dispersive scalar flux equals the turbulent flux, i.e. $\langle J \rangle_{turb}^s = \langle J \rangle_{turb}^s$, and is plotted over Re_K . Similarly, the position μ_z of the drag-based interface is plotted over Re_K . The dashed line marks a common trend.



Figure 15. Influence of the permeability Reynolds number Re_K on the relative contributions of different scalar transport processes to the total scalar flux $\langle J \rangle_{tot}^s$ in the bed-normal direction. The curves group according to Re_K . The vertical coordinate z is normalised by the sphere diameter D. Note that the normalisation of a flux by $\langle J \rangle_{tot}^s$ corresponds to a normalisation by $(u_t^{\pi} c_{\tau})$.

In figure 15 the impact of different processes was evaluated in terms of their relative contribution to the total scalar flux. This representation may yield the impression that the sub-interface dispersive scalar transport is as effective as the turbulent transport in the free-flow region. Figure 16 corrects this impression by providing the process-specific effective diffusivities, which result from a comparison to the diffusive scalar transport. Above the sediment bed, the scalar field is well mixed, such that hardly any vertical concentration gradient is present, and the turbulent scalar transport achieves a higher effective diffusivity. In contrast, dispersive transport acts below the interface, where comparatively strong vertical scalar concentration gradients prevail, which exposes a lower effective diffusivity associated with the process. The near-interface turbulent effective diffusivity profiles collapse well for cases with similar Re_K . In comparison, differences between the dispersive effective diffusivity profiles are larger. A possible reason could be that specific geometrical properties of the generated sediment beds have more impact on the dispersive transport.

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Figure 16. Process-specific effective diffusivity profiles for turbulent and dispersive scalar transport in the near-interface region. The effective diffusivity is normalised by the molecular diffusivity and the vertical coordinate z by the sphere diameter D. The profiles tend to group according to Re_K .

4.5. Distribution of scalar transport processes in space

Dispersive transport requires a correlation between the spatial variations of the time averaged bed-normal velocity field and the scalar concentration field, whereas turbulent scalar transport requires a correlation of the temporal fluctuations of the two fields. The scatter plots in figure 17 visualise the quality of these correlations at the position z = 0 of case M-500. Regions of downwelling time-averaged fluid motion through the interface are characterised by $\overline{w} < 0$. The samples in the third and fourth quadrant of figure 17(a) show that \overline{c} is close to zero under these conditions, with only a slight tendency towards positive values. This suggests that downwelling motion at the geometrically defined interface transports fluid with a nearly uniform scalar concentration from the well-mixed freeflow region into the sediment bed. In contrast, the scalar concentration in the upwelling flow $(\widetilde{w} > 0)$ varies over a much wider range. The scalar concentration in the freeflow region seems to impose an upper limit for positive \overline{c} (see first quadrant). In some upwelling regions, however, \overline{c} has negative values of high amplitude, as shown by the circles in the second quadrant. At these sampled locations, fluid with scalar concentrations closer to cbot is transported upwards through the interface. A reason could be that individual nearly vertical flow paths exist that cross regions of high vertical concentration gradients and advect fluid from deeper layers upwards. For turbulent transport resulting from temporal fluctuations, however, similar observations cannot be made. As shown in figure 17(b), the negative correlation between w' and c' becomes mainly visible from a few points in the second and fourth quadrant. These observations suggest that dispersive and turbulent transport behave differently, which we will investigate further by analysing their distribution in space.

Figure 18 shows the local contributions to turbulent, dispersive and diffusive transport within an arbitrarily chosen vertical slice through case M-500. Above $z/D \approx 2$, the turbulent scalar transport seems to occur nearly uniformly distributed in space, which suggests that this region is well mixed. Only at a few individual spots, turbulenttransport takes place within the pore space below the bed surface. In contrast, several local hotspots of increased bed-normal turbulent scalar transport are found directly above the sediment–water interface, e.g. at $x/D \approx 14$ or $x/D \approx 58$ in figure 18(*a*). The observations made in



Figure 17. Correlations between the bed-normal velocity w and the scalar concentration c. Correlated spatial variations (a) are responsible for dispersive scalar transport. Correlated temporal fluctuations (b) are required for turbulent scalar transport. Each point represents a sample taken at a random position within the plane z = 0 of case M-500. The red colour indicates a positive contribution and the blue colour a negative contribution to the scalar transport.

the arbitrarily chosen slice suggest that hotspots of turbulent scalar transport above the interface occur where upwelling fluid motion contributes strongly to enhanced dispersive transport below the sediment–water interface. In figure 18(b), two such locations are marked by arrows. In their appearance, these locations resemble chimneys, which release the scalar quantity. Continuing in this analogy, the transition from dispersive to turbulent transport near the interface represents the outlet of the sub-interface chimney, from which the released scalar is immediately advected downstream within the free-flow field. Due to this downstream advection, a strong vertical concentration gradient prevails at the chimney outlet, which fosters the local diffusive scalar transport. In figure 18(c), two such near-interface locations with local maxima of diffusive transport are marked by arrows.

The insight from the local contributions to turbulent, dispersive and diffusive transport facilitates the interpretation of the double-averaged flux values, previously presented in figure 13. Accordingly, the sharp near-interface transition between dispersive and turbulent transport coincides with the outlets of the sub-interface chimneys. The enhanced



Figure 18. Local contributions to the turbulent, dispersive and diffusive scalar transport within an arbitrarily chosen x-z-plane of simulation case M-500. The values are normalised by the absolute value of the superficially averaged total scalar flux $\langle J \rangle_{tot}^s$. Coordinates in the x- and z-direction are given in x/D and z/D, respectively, where D is the sphere diameter.

diffusive transport at the chimney outlets explains the local maximum in the share of the diffusive scalar transport, which accompanies the transition between dispersive and turbulent transport. The abrupt transition at the chimney outlets also implies that there is hardly any spatial overlap between dispersive and turbulent scalar transport hotspots. Rather, one process replaces the other such that the local vertical scalar flux is continued across the interface.

4.6. Interaction at the interface

The previous sections have shown that different scalar transport processes are active in the near-interface region. In the following, we aim to describe their interaction both qualitatively and quantitatively. For the qualitative investigation, we consider the arbitrarily chosen vertical slice through case M-500, for which different quantities are provided in figure 19. Figure 19(a) shows the time-averaged scalar concentration field. Even with a strongly nonlinear colour map, hardly any concentration differences become visible in the well-mixed free-flow region. Strong scalar concentration surfaces in this region are not even approximately parallel to the surface of the sediment bed, but have a



Figure 19. Form-induced production of temporal scalar fluctuations. The mean scalar concentration field (*a*) and an instantaneous scalar concentration field (*b*) are shown within an arbitrarily chosen *x*-*z*-plane of simulation case M-500. The form-induced production (*c*) appears strongly localised with spots of strong intensity near the chimneys, of which one is marked by the dashed box. Coordinates in *x*- and *z*-direction are given in x/D and z/D, respectively, where *D* is the sphere diameter.

strong relief. For cases with lower Re_K , this relief is not as strong, yet still present (not shown). Figure 19(b) shows a realisation of the instantaneous scalar concentration field. The strongly nonlinear colour map emphasises concentration differences in the freeflow region. In particular near the chimney outlets, the interaction between turbulent fluid motion and the scalar concentration field becomes visible and suggests enhanced turbulent mixing at these locations. One such location is marked by dashed boxed in figure 19(b). As formally shown by (2.10) and (2.11) in § 2.4, the form-induced production mechanism creates temporal scalar fluctuations, while reducing the spatial variance in the scalar field. Figure 19(c) corroborates that the marked location acts as one hotspot of forminduced production, while further hotspots are found around the chimneys at $x/D \approx 14$ or $x/D \approx 58$ (not shown). The visualisation by volume rendering uses a logarithmic colour map, as regions of high form-induced production appear strongly localised. Most hotspots of form-induced production are found between the spheres in the topmost layer of the sediment bed. Below that, the local observation suggests that only a few spots of high form-induced production intensity occur primarily in larger pores, which are likely to provide good conditions for turbulent mixing. Apart from those local hotspots, hardly any form-induced production can be detected in large parts of the porous medium.



Figure 20. Production mechanisms of temporal scalar fluctuations: profiles of form-induced production (*a*) and gradient production (*b*) in direct comparison. For normalisation, the friction velocity u_{τ} , the friction scalar concentration $c_{\tau} = \langle \overline{J} \rangle_{tot}/u_{\tau}$ and the sphere diameter *D* are used.

To assess the impact and the scaling behaviour of form-induced production, we evaluate double-averaged profiles. Figure 20(a) shows the profiles of form-induced production intensity, using the sphere diameter, the friction velocity and the friction scalar concentration value for a normalisation with interface-related scales. Except for S-150, all cases exhibit a form-induced production peak, which is found at $z/D \approx 0.5$ for lower Re_K and moves towards $z/D \approx 0.2$ with increasing Re_K . Under the given normalisation, the amplitude of the peak increases with Re_K , causing the curves to group roughly accordingly. Below the peak, the form-induced production declines with increasing depth, whereas the tailing behaviour is similarly determined by Re_K . For cases with high Re_K , the form-induced production introduces temporal scalar fluctuation even at greater depth. Most notably for case L-300, the profile is not fully smooth but exhibits characteristic features. This agrees with the observation that the form-induced production does not occur uniformly in space, but rather concentrates in certain locations. To put the influence of the form-induced production in relation, figure 20(b) shows the gradient production of scalar fluctuations. For all cases with $Re_K > 1$, the peak of the form-induced production is considerably larger than the peak value of the gradient production. A further difference to the form-induced production is that gradient production hardly affects the region z/D < 0, whereas it does have influence in the free-flow region.

5. Discussion

The defect representation of the double-averaged concentration profiles reveals an outerlayer similarity among cases with similar Re_{τ} (figure 9). This similarity shows up under the normalisation $\langle \overline{c} \rangle^+ = \langle \overline{c} \rangle u_{\tau}^{\mu} / \langle \overline{J} \rangle_{tot}^s$, in which the flux compensates for different conditions in the bed and the friction velocity acts as a velocity scale. The similarity under consideration of the flux implies that the ratio between effective and molecular diffusivity, i.e. Γ_{eff}/Γ_c , at a certain vertical position is determined by Re_{τ} or, even more accurately, by the interface-adapted Reynolds number Re_{τ}^{μ} (figure 11). The observations that Γ_{eff} scales with $u_{\tau}^{\mu} h^{\mu}$ and that the turbulent Schmidt number is near unity over large parts of the flow depth agree well with the findings of Pirozzoli *et al.* (2016) for smooth-wall channel flow. It has been observed in v.Wenczowski & Manhart (2024) that also the outer-layer velocity profiles and turbulent fields show similarities at similar Re_{τ} , if the drag-based interface position is used. In our view, those similarities are tightly linked to the observed similarity of the concentration profiles in the outer layer, which is dominated by turbulent transport.

While the free-flow region is dominated by turbulent transport, different scalar transport regimes can be distinguished at the sediment-water interface. According to Voermans et al. (2018), the transition from the diffusive to the dispersive regime takes place at $Re_K \approx 0.02$. For case S-150, which is characterised by $Re_K \approx 0.4$, however, we already observe that molecular diffusion dominates the near-interface scalar transport (figure 15). This discrepancy may be explained by the role of the Schmidt number $Sc = \nu/\Gamma$, which was set to unity in the present study. To avoid jumps in the predicted effective diffusivity between the diffusive regime $(D_{eff}/\Gamma = 1 \text{ for } Re_K < 0.02)$ and the dispersive regime $(D_{eff}/\Gamma = 1.6 Re_K^2 Sc \text{ for } Re_K > 0.02)$, however, Voermans et al. (2018) implicitly assumed that $Sc = O(10^3)$, which is realistic for dissolved substances in water. To close the comparability gap, we refer to the Péclet number, which allows us to judge if a process is dominated by advection ($Pe \gg 1$) or diffusion ($Pe \ll 1$). For Sc = 1 and \sqrt{K} as the characteristic length scale, we obtain a permeability Péclet number $Pe_K = Sc Re_K = 1$ already for $Re_K = 1$. In fact, cases M-150 and S-300 show nearly equal shares of diffusive and dispersive transport at the interface (figure 13). For $Sc = O(10^3)$, critically lower values of Re_K suffice to reach $Pe_K = O(1)$. This suggests that the permeability Péclet number Pe_K is a more robust parameter to predict the transition between the diffusive and the dispersive regime, which avoids implicit assumptions concerning the Schmidt number. In fact, O'Connor & Harvey (2008) considered Pe_K in their categorisation of the interfacial transport regime.

In the near-interface region, dispersive transport declines rapidly and turbulent transport increases rapidly, if one moves upward in the positive z direction. As a result, one transport process replaces the other over a vertical distance of only approximately one sphere diameter. Thus, if one wishes to determine which process dominates the scalar transport across the sediment-water interface, the actual definition of the interface becomes relevant. Voermans et al. (2018) referred to a geometrical interface definition based on the inflection point of the porosity profile. For progressively higher Re_K , our data shows that turbulent transport becomes responsible for larger shares of the scalar transport across this geometrically defined interface, which supports the notion of a transition from the dispersive to the turbulent regime around $Re_K \approx 1-2$ (figure 15). In v.Wenczowski & Manhart (2024), we had deduced the interface position from the drag distribution on the porous medium. The present study indicates that the transition between dispersive and turbulent transport follows approximately the position of the drag-based interface (figure 14). Accordingly, no obvious transition between the dispersive and the turbulent regime can be observed at the drag-based interface. Once Pe_K is large enough such that the transition from the diffusive to the dispersive regime has taken place, the relevant question according to our data is not whether the interface region is dominated by turbulent or dispersive transport, but rather at which depth the dispersive transport takes over. Our data suggest that this depth is linked to how deep the streamwise momentum of the free flow entrains into the sediment bed.

To investigate the interaction between the dispersive and the turbulent scalar transport in the interface region, we referred to the form-induced production mechanism, which produces temporal scalar fluctuations $\langle \overline{c'c'} \rangle$, while it reduces spatial in-plane variations in the scalar field $\langle \tilde{c} \ \tilde{c} \rangle$. For the turbulent kinetic energy, a similar form-induced production mechanism is known, which produces temporal velocity fluctuations $\langle \overline{u'_iu'_i} \rangle$ at the expense

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of spatial variations in the velocity field $\langle \tilde{u}_i \ \tilde{u}_i \rangle$. For the turbulent kinetic energy, however, form-induced production plays a minor role in comparison to shear production for $Re_K < 3$ (e.g. Fang *et al.* 2018; Shen *et al.* 2020). That is in strong contrast to the scalar form-induced production, which already acts as the primary source of scalar fluctuations for cases with $Re_K > 1$ (figure 20). The critically different role of form-induced production is likely linked to the different boundary conditions on the sphere surface: For the velocity field, the Dirichlet-type no-slip boundary condition prescribes $u_i = 0$ on the sphere surfaces, such that velocity variations can only occur on the length scale \sqrt{K} of the pore space. For the scalar field, however, the zero-flux (adiabatic) Neumann-type boundary condition on the sphere surface allows the development of spatial variations of \bar{c} on larger length scales (figure 19*a*). Particularly in regions with upwelling fluid motion, fluid with scalar concentrations typical of deeper regions can reach the interface. These upwelling regions resemble chimneys and seem to contribute greatly to the dispersive scalar transport (figure 17). The upper end of these chimneys is reached near the surface of the sediment bed, where turbulent fluid motion mixes the scalar field in the bed-parallel direction.

All before-mentioned aspects underline that the form-induced production, i.e. the transfer of spatial variations into temporal fluctuations of the scalar field due to turbulent transport acting against local in-plane scalar gradients, plays a critical role for the transition between dispersive and turbulent scalar transport, as hypothesised by Voermans *et al.* (2018). This allows us to connect different observations: with increasing Re_K , turbulent fluid motion entrains deeper into the pore space (see, e.g. Voermans *et al.* 2017; v.Wenczowski & Manhart 2024), form-induced production peaks at a lower position (figure 20) and the transition between dispersive and turbulent scalar transport also happens deeper below the crests of the sediment bed (figure 14). Furthermore, the form-induced production mechanism explains why the transition between turbulent and dispersive transport occurs within a thin layer of approximately one sphere diameter (figure 13). By enhancing the temporal fluctuations for the turbulent scalar transport, which coincides with a turbulent Schmidt number of $Sc_t < 1$ at the interface (figure 12).

6. Conclusion

We conducted pore-resolved DNS of turbulent flow over mono-disperse random sphere packs. The flow simulation was coupled with the solution of the advection-diffusion equation for a passive scalar at a Schmidt number of Sc = 1. Fixed scalar concentration values at the bottom and top of the flow domain were prescribed to induce a bed-normal scalar flux, whereas the sphere surfaces were impermeable to scalar fluxes. After a careful convergence study, eight cases were analysed and act as sampling points arranged within a parameter space spanned by friction Reynolds numbers $Re_{\tau} \in [150, 500]$ and permeability Reynolds numbers $Re_K \in [0.4, 2.8]$. The ratios between flow depth and sphere diameter are $h/D \in \{3, 5, 10\}$ and the dimensionless roughness heights lie within $k_s^+ \in [20, 200]$, indicating either transitionally or fully rough conditions.

The free-flow region is dominated by turbulent scalar transport. The effective scalar diffusivity in this region scales with the friction velocity and the flow depth. Also, the dimensionless scalar concentration defect profiles collapse in the outer layer for cases with similar Re_{τ} , as the quantity $(c_{top} - \langle \overline{c} \rangle)^+$ implicitly accounts for the double-averaged scalar flux. Near the interface, the influence of turbulent scalar transport declines rapidly, whereas the impact of dispersive scalar transport increases. The position where both transport processes contribute equally to the total bed-normal scalar flux is found near the point where the sediment bed absorbs most momentum from the free-flow region,

i.e. the drag-based interface position described in v.Wenczowski & Manhart (2024). The normalised effective diffusivity at the drag-based interface scales reasonably well with the square of Re_K , which supports the model of Voermans *et al.* (2018) for the prediction of this parameter. At a constant Schmidt number Sc = 1, Re_K also determines the relative contributions of different scalar transport processes and, thus, the near-interface effective diffusivity profiles associated with individual processes. We argue, however, that the permeability Péclet number Pe_K is better suited to predict whether diffusive or dispersive transport is dominant, such that Pe_K can also help to compare studies with different Schmidt numbers. With increasing depth below the surface of the sediment bed, the influence of dispersive transport declines, such that molecular diffusion is exclusively responsible for the vertical scalar flux. A steep gradient in the double-averaged scalar concentration indicates that the deeper region of the sediment bed poses a high resistance to the scalar flux.

Even in the absence of a macroscopic bed topography, locally upwelling or downwelling time-averaged fluid motion results from grain-scale irregularities in the sediment bed surface. Downwelling flow through the interface transports fluid with a nearly homogeneous scalar concentration downwards from the well-mixed turbulent free-flow region. In contrast, upwelling motion can transport fluid with strongly varying scalar concentration through the interface. This is possible as mean flow paths within the sediment bed cross layers with strong scalar gradients. Locations where strong upwelling motion advects the scalar field from deeper regions to the interface resemble chimneys and appear to have a major contribution to the dispersive scalar transport. At the same time, the occurrence of those chimneys is linked to strong spatial variations in the scalar concentration field below the sediment bed surface.

Form-induced production of temporal scalar fluctuations takes place when turbulent scalar transport acts against scalar gradients resulting from in-plane concentration variations. As a result, temporal scalar fluctuations are introduced, while spatial variations in the scalar concentration field are removed. Thus, the form-induced production mechanism weakens the basis for dispersive scalar transport, while it creates favourable conditions for turbulent scalar transport. With increasing Re_K , turbulent motion can entrain into the sediment bed more easily, such that a near-interface form-induced production peak increases, while also progressively deeper regions are affected. Accordingly, the role of form-induced production explains why the transition between dispersive and turbulent scalar transport happens at progressively lower positions with increasing Re_K . Furthermore, form-induced production explains the sharp transition between turbulent and dispersive transport processes at the interface.

While we emphasised the role of the form-induced production mechanism, the discussion of the complete budgets for temporal scalar fluctuations and spatial scalar variations would have exceeded the scope of the present paper. Nonetheless, the evaluation of those budgets is likely to advance the understanding of the temporal and spatial variability of hyporheic scalar fields, which is of high importance for the organisms in this ecologically relevant region.

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REFERENCES

- BATTIN, T.J., BESEMER, K., BENGTSSON, M.M., ROMANI, A. & PACKMANN, A.I. 2016 The ecology and biogeochemistry of stream biofilms. *Nat. Rev. Microbiol.* 14 (4), 251–263.
- BOANO, F., HARVEY, J.W., MARION, A., PACKMAN, A.I., REVELLI, R., RIDOLFI, L. & WÖRMAN, A. 2014 Hyporheic flow and transport processes: mechanisms, models, and biogeochemical implications. *Rev. Geophys.* 52 (4), 603–679.
- BREUGEM, W.P., BOERSMA, B.J. & UITTENBOGAARD, R.E. 2006 The influence of wall permeability on turbulent channel flow. J. Fluid Mech. 562, 35–72.
- BRUNKE, M. & GONSER, T. 1997 The ecological significance of exchange processes between rivers and groundwater. *Freshwater Biol.* 37 (1), 1–33.
- CHANDESRIS, M., D'HUEPPE, A., MATHIEU, B., JAMET, D. & GOYEAU, B. 2013 Direct numerical simulation of turbulent heat transfer in a fluid-porous domain. *Phys. Fluids* **25** (12), 125110.
- CHANDLER, I.D., GUYMER, I., PEARSON, J.M. & VAN EGMOND, R. 2016 Vertical variation of mixing within porous sediment beds below turbulent flows. *Water Resour. Res.* 52 (5), 3493–3509.
- CHEN, C-Y., FYTANIDIS, D.K. & GARCIA, M.H. 2024 A unifying model for turbulent hyporheic mass flux under a wide range of near-bed hydrodynamic conditions. *Geophys. Res. Lett.* 51 (6), e2023GL105807.
- ELLIOTT, A.H. & BROOKS, N.H. 1997 Transfer of nonsorbing solutes to a streambed with bed forms: theory. *Water Resour. Res.* **33** (1), 123–136.
- FANG, H., HAN, X., HE, G., DEY, S. 2018 Influence of permeable beds on hydraulically macro-rough flow. J. Fluid Mech. 847, 552–590.
- FINN, J. & APTE, S.V. 2013 Relative performance of body fitted and fictitious domain simulations of flow through fixed packed beds of spheres. *Intl J. Multiphase Flow* 56, 54–71.
- GIMÉNEZ-CURTO, L.A. & LERA, M.A.C. 1996 Oscillating turbulent flow over very rough surfaces. J. Geophys. Res.: Oceans 101 (C9), 20745–20758.
- GRANT, S.B., STEWARDSON, M.J. & MARUSIC, I. 2012 Effective diffusivity and mass flux across the sediment-water interface in streams. *Water Resour. Res.* 48 (5). https://agupubs.onlinelibrary. wiley.com/doi/10.1029/2011WR011148
- HARVEY, J.W., BÖHLKE, J.K., VOYTEK, M.A., SCOTT, D. & TOBIAS, C.R. 2013 Hyporheic zone denitrification: controls on effective reaction depth and contribution to whole-stream mass balance. *Water Resour. Res.* 49 (10), 6298–6316.
- HEYMAN, J., LESTER, D.R., TURUBAN, R., MÉHEUST, Y.& LE BORGNE, T. 2020 Stretching and folding sustain microscale chemical gradients in porous media. *Proc. Natl Acad. Sci.* 117 (24), 13359–13365.
- JACKSON, P.S. 1981 On the displacement height in the logarithmic velocity profile. J. Fluid Mech. 111, 15–25.
- KARRA, S.K., APTE, S.V., HE, X. & SCHEIBE, T.D. 2023 Pore-resolved investigation of turbulent open channel flow over a randomly packed permeable sediment bed. J. Fluid Mech. 971, A23.
- KRAUSE, S., HANNAH, D.M., FLECKENSTEIN, J.H., HEPPELL, C.M., KAESER, D., PICKUP, R., PINAY, G., ROBERTSON, A.L. & WOOD, P.J. 2011 Inter-disciplinary perspectives on processes in the hyporheic zone. *Ecohydrology* 4 (4), 481–499.
- KRAUSE, S. 2017 Ecohydrological interfaces as hot spots of ecosystem processes. Water Resour. Res. 53 (8), 6359–6376.
- LAI, J., LO, S. & LIN, C. 1994 Effects of hydraulic and medium characteristics on solute transfer to surface runoff. *Water Sci. Technol.* 30 (7), 145–155.
- MANHART, M. 2004 A zonal grid algorithm for DNS of turbulent boundary layers. *Comput. Fluids* **33** (3), 435–461.
- MANHART, M., TREMBLAY, F. & FRIEDRICH, R. 2001 MGLET: a parallel code for efficient DNS and LES of complex geometries. *Parallel Computational Fluid Dynamics 2000* (ed. C.B. Jenssen, H.I. Andersson, A. Ecer, N. Satofuka, T. Kvamsdal, B. Pettersen, J. Periaux & P. Fox), pp. 449–456. North-Holland.
- HEIDI, P. 2014, Aquatic interfaces: a hydrodynamic and ecological perspective. J. Hydraul. Res. 52 (6), 744–758.
- MIGNOT, E., BARTHELEMY, E. & HURTHER, D. 2009 Double-averaging analysis and local flow characterization of near-bed turbulence in gravel-bed channel flows. J. Fluid Mech. 618, 279–303.
- NAGAOKA, H. & OHGAKI, S. 1990 Mass transfer mechanism in a porous riverbed. Water Res. 24 (4), 417-425.
- NIKORA, V., GORING, D., MCEWAN, I. & GRIFFITHS, G. 2001 Spatially averaged open-channel flow over rough bed. J. Hydraul. Engng 127 (2), 123–133.

- O'CONNOR, B.L. & HARVEY, J.W. 2008 Scaling hyporheic exchange and its influence on biogeochemical reactions in aquatic ecosystems. *Water Resour. Res.* 44 (12). https://agupubs.onlinelibrary. wiley.com/doi/full/10.1029/2008WR007160
- PACKMAN, A.I., SALEHIN, M. & ZARAMELLA, M. 2004 Hyporheic exchange with gravel beds: basic hydrodynamic interactions and bedform-induced advective flows. J. Hydraul. Engng 130 (7), 647–656.
- PELLER, N. 2010 Numerische simulation turbulenter strömungen mit immersed boundaries. Phd thesis, Technical University of Munich (TUM), Germany.
- PELLER, N., DUC, A.L., TREMBLAY, F. & MANHART, M. 2006 High-order stable interpolations for immersed boundary methods. *Intl J. Numer. Meth. Flow* 52 (11), 1175–1193.
- PIROZZOLI, S., BERNARDINI, M. & ORLANDI, P. 2016 Passive scalars in turbulent channel flow at high Reynolds number. J. Fluid Mech. 788, 614–639.
- RICHARDSON, C.P. & PARR, A.D. 1988 Modified Fickian model for solute uptake by runoff. J. Environ. Engng 114 (4), 792–809.
- SAKAI, Y., MENDEZ, S., STRANDENES, H., OHLERICH, M., PASICHNYK, I., ALLALEN, M. & MANHART, M. 2019 Performance optimisation of the parallel CFD code MGLET across different HPC platforms. In Proceeding of the Platform Advanced Scientific Computing Conference, PASC '19 6, pp. Association for Computing Machinery.
- SCHWERTFIRM, F. & MANHART, M. 2007 DNS of passive scalar transport in turbulent channel flow at high Schmidt numbers. Intl J. Heat Fluid Flow 28 (6), 1204–1214.
- SHEN, G., YUAN, J. & PHANIKUMAR, M.S. 2020 Direct numerical simulations of turbulence and hyporheic mixing near sediment–water interfaces. J. Fluid Mech. 892, A20.
- SHEN, G., YUAN, J. & PHANIKUMAR, M.S. 2022 Quantifying the effects of bed roughness on transit time distributions via direct numerical simulations of turbulent hyporheic exchange. *Water Resour. Res.* 58 (4), e2021WR030503.
- THOM, A.S. 1971 Momentum absorption by vegetation. Q. J. R. Meteorol. Soc. 97 (414), 414-428.
- UNGLEHRT, L. & MANHART, M. 2022 Onset of nonlinearity in oscillatory flow through a hexagonal sphere pack. J. Fluid Mech. 944, A30.
- VOERMANS, J.J., GHISALBERTI, M. & IVEY, G.N. 2017 The variation of flow and turbulence across the sediment–water interface. J. Fluid Mech. 824, 413–437.
- VOERMANS, J.J., GHISALBERTI, M. & IVEY, G.N. 2018 A model for mass transport across the sedimentwater interface. Water Resour. Res. 54 (4), 2799–2812.
- WARD, A.S. 2016 The evolution and state of interdisciplinary hyporheic research. WIREs Water 3 (1), 83–103.
- V.WENCZOWSKI, S. & MANHART, M. 2024 Turbulent flow over random sphere packs an investigation by pore-resolved direct numerical simulation. J. Fluid Mech. 1001, A29.

WILLIAMSON, J.H. 1980 Low-storage Runge-Kutta schemes. J. Comput. Phys. 35 (1), 48-56.

WOESSNER, W.W. 2017 Hyporheic zones. In *Methods in Stream Ecology*. vol. 1, Third edition (ed. RICHARD HAUER F. & LAMBERTI G.A.) pp. 129–157, Academic Press.